

Information-Reduced Carrier Synchronization of BPSK and QPSK Using Soft Decision Feedback

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Introduction

- This paper addresses the carrier-phase estimation problem under low SNR conditions in a ***soft decision-directed*** LDPC-coded system.
- Two distinct techniques for joint decoding and synchronization :
 1. Modifying iterative detection/decoding algorithms and/or graph structure to include parameter estimation
 2. **Turbo Synchronization**: Pass messages between an independent phase estimation block and an essentially unmodified iterative decoder [Noels05]
- The technique in this presentation falls into this second category.
- We propose a ***soft decision-directed pilotless*** carrier recovery circuit with little modification to either the iterative decoder or the carrier recovery block.

Motivation

- When designing communication systems engineers need to decide whether or not to suppress the transmitted carrier power
- Total power = Carrier Power + Data Power $\rightarrow P_t = P_c + P_d$
 - **Carrier Power**: related to the accuracy of the *carrier synch* process
 - **Data Power**: related to the accuracy of the *data detection* process (in the presence of perfect carrier synchronization).
- System design requires a proper trade off between these power requirements to minimize the *average error probability* of the system [Simon96] .
- Traditional synchronization circuits:
 - **Residual Carrier**: Utilize phase-lock Loops (PLL) to provide an accurate synchronization. (Used in NASA's deep space comm. systems.)
 - **Suppressed-carrier**: Tracking loops such as the Costas loop require a larger SNR to track the carrier with a given accuracy.

Possible Synchronization Circuits

■ Phase-Lock Loop (PLL):

- Use residual carrier information inside the tracking loop to aid synchronization.

- Loop SNR:
$$\frac{1}{\sigma_{\phi_c}^2} = \rho_{PLL} = \frac{P_c}{N_o B_L}$$

- B_L : Loop Bandwidth,

- P_c : Total Carrier Power,

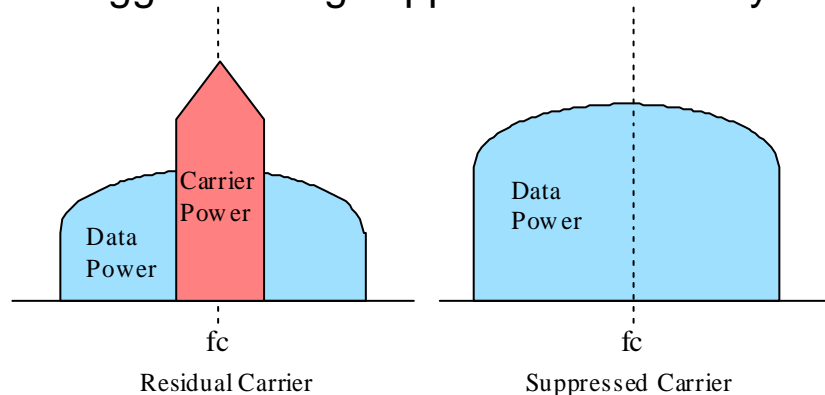
- N_o : Noise PSD

- ϕ_c : Carrier Phase Estimation Error

- There always exists an optimum (in the sense of *minimum average error probability*) split between Data and Carrier power .

- If $m^2 = P_c / P_T$, typical systems require $m^2 \approx 0.1$ or less [Simon96]

- This trend suggests using suppressed-carrier systems, i.e. $m^2 = 0$



Possible Synchronization Circuits

■ Costas Loop

- Can track fully suppressed-carrier signals.
- Loop SNR:

$$\frac{1}{\sigma_{\phi_c}^2} = \rho_C \cdot S_{LC} = \frac{P_t}{N_o B_L} \left(1 + \frac{1}{2R_d} \right)^{-1} = \frac{P_T}{N_o B_L} \left(1 + \frac{N_o}{2P_T T_s} \right)^{-1}$$

B_L : Loop Bandwidth,
 R_d : Input Data SNR,

P_t : Total Power,
 S_{LC} : Squaring Loss,

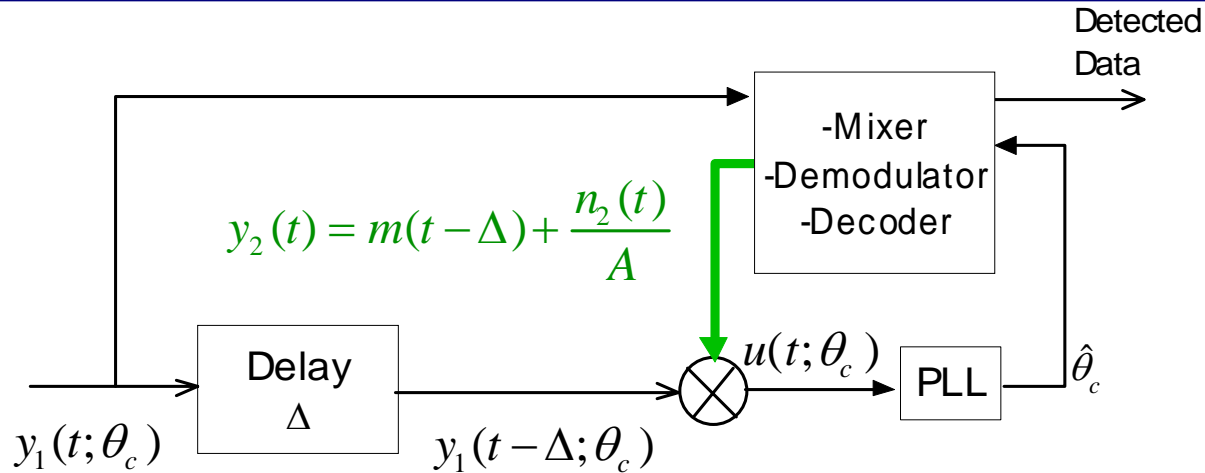
N_o : Noise PSD,
 T_s : Pulse Duration

- Requires significantly larger *loop SNR* than a PLL to be able to track.
 - At low data SNRs, the SL can be large enough to prevent tracking.
- For a fixed input data SNR , SL does not improve with decoder iterations.
- For a wide input data SNR range, Costas loop systems are still more efficient (in the sense of *minimum average error probability*) than PLL circuits.
- **Alternative Circuit:** design a suppressed carrier system for low data SNR that uses a PLL circuit instead of a Costas loop.

Information-reduced carrier-synchronization (IRCS)

- Use a ***soft estimate*** of the instantaneous data symbol (and thus of the instantaneous phase modulation) to reduce the amount of randomness (information) in the signal being processed in the carrier loop. [Simon97]
- LDPC symbol estimates “wipe-off ” modulated symbols in a ***decision directed*** loop to ***enhance the carrier information*** such that a classic PLL can provide increasingly accurate phase estimates over LDPC iterations.
- Latency penalty: tracking improves with increased iterations
- System complexity: No significant modifications to the current residual carrier recovery techniques used for BPSK/ QPSK modulation in NASA's deep-space network.

IRCS BPSK System Description



- BPSK Modulation:
$$m(t) = \sum_{k=-\infty}^{\infty} d_k p(t - kT_s)$$

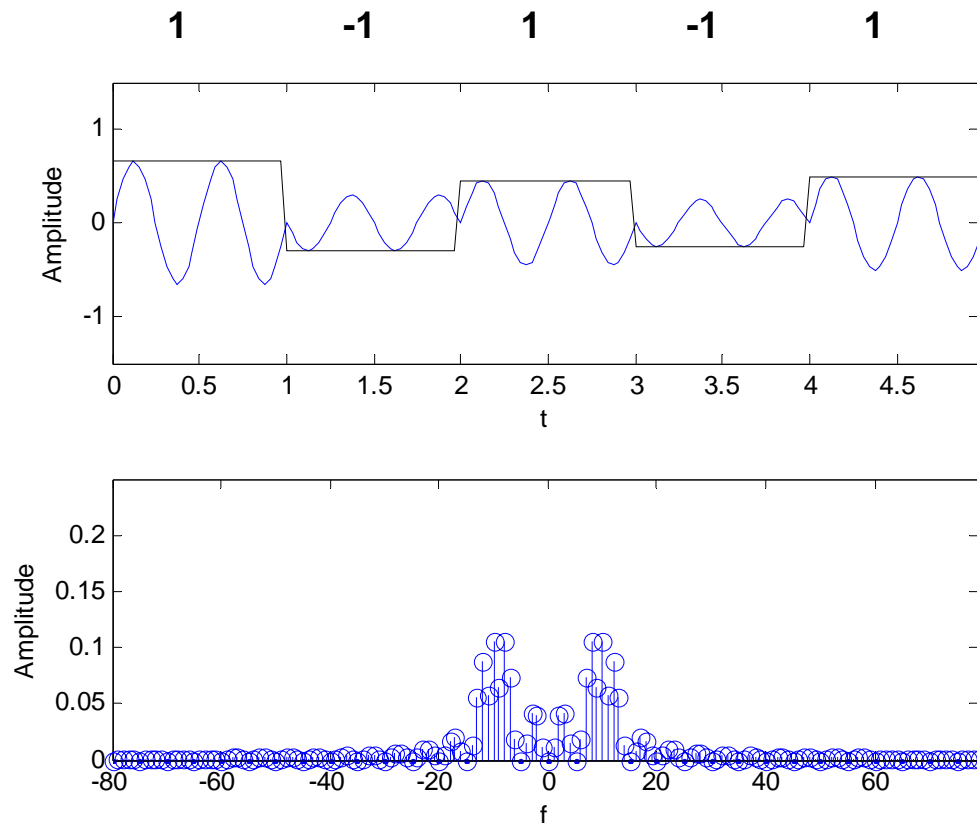
- Signal Input:
$$y_1(t; \theta_c) = \sqrt{2P} \sin(\omega_c t + \theta_c) + n_1(t)$$

- AWGN Noise:
$$n_1(t) = \sqrt{2} \left[N_{c1}(t) \cos(\omega_c t + \theta_c) - N_{s1}(t) \sin(\omega_c t + \theta_c) \right]$$

- IR Signal:
$$u(t; \theta_c) = \sqrt{2P} \sin(\omega_c t + \theta_c) + [\text{Noise terms}]$$

Carrier Detection Process

- Assume $N=5$ transmitted BPSK symbols
- Sample transmitted waveform = $[1, -1, 1, -1, 1]$
- Plot shows received waveform *affected by symbol-wise noise*

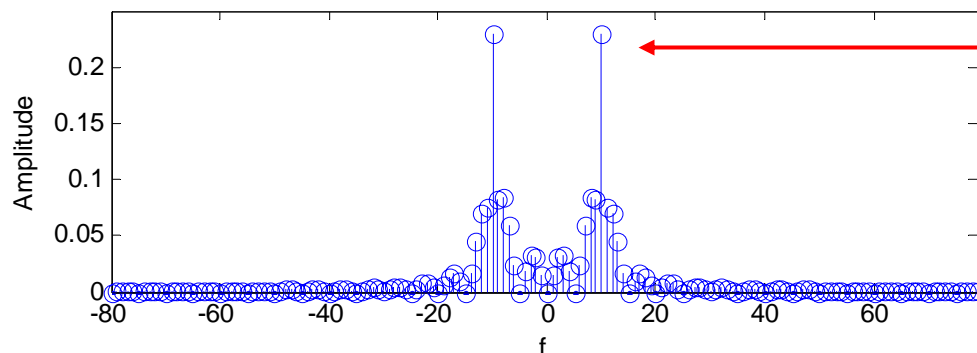
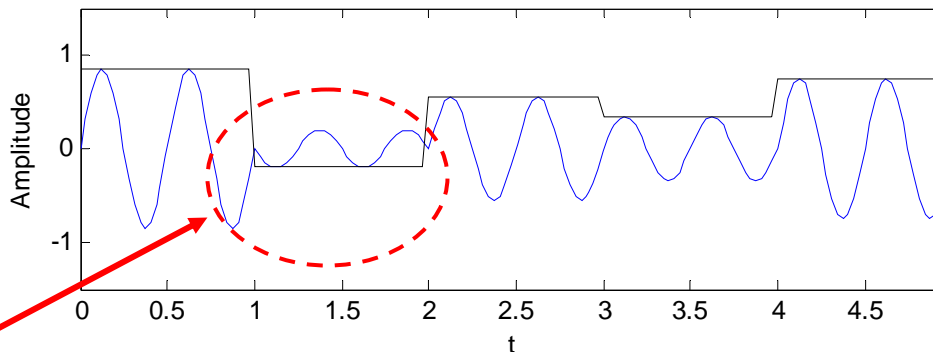


Carrier Detection Process

- Modulation is removed by multiplying the received waveform by soft-estimated symbols from the decoder
- Symbol Information randomness is reduced
- Plot shows “IR” waveform after the first iterations

■ **Soft Symbol information may still be incorrect**

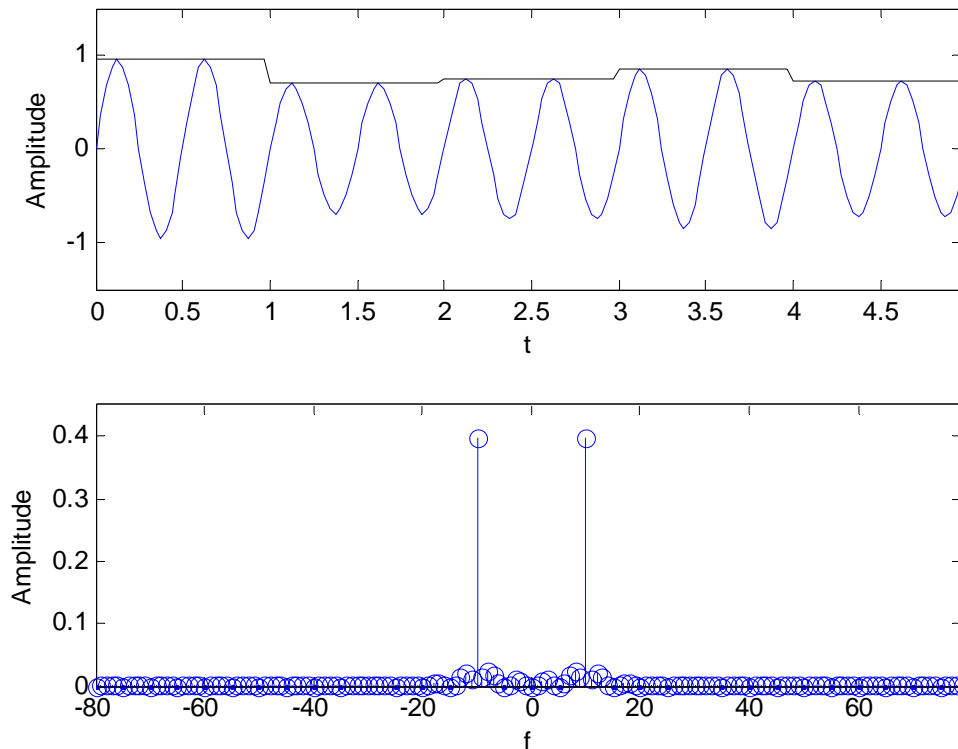
■ **Incorrect information has low reliability**



Unmodulated frequency spectrum begins to show the presence of a carrier tone.

Carrier Detection Process

- As the number of iterations increase, soft-symbol estimation becomes more accurate.
- Frequency spectrum has a distinctive tone that a PLL based circuit can now track.



Proposed Synchronization Circuit

■ Information Reduced Carrier Synchronization (IRCS)

- Can track fully suppressed-carrier signals
- Loop SNR:

$$\frac{1}{\sigma_{\phi_c}^2} = \rho_{IRCS} \cdot S_{LIRCS} = \frac{P_T}{N_o B_L} \left(1 + \frac{\sigma^2}{A^2} \right)^{-1} = \left|_{\text{LDPC}} \frac{P_T}{N_o B_L} \left(1 + \frac{2}{A} \right)^{-1} \right.$$

- B_L : Loop Bandwidth,
- S_{LIRCS} : Squaring Loss,

P_T : Total Power,
 A : Estimated Signal Amplitude

- The ratio $\frac{A^2}{\sigma^2}$ represents the decoder soft-estimate data SNR.
- *Symmetry condition*: For decoding of LDPC and turbo codes $\sigma^2=2A$. [Chung01]
- Decoder data SNR increases with iterations causing:
 - $S_{LIRCS} \rightarrow 1$
 - Loop SNR approaches PLL performance using the total transmitted power for carrier estimation

Loop SNR Summary

■ PLL:

$$\frac{1}{\sigma_{\phi_c}^2} = \rho_{PLL} = \frac{P_c}{N_o B_L}$$

- Loop SNR exhibits No squaring loss
- Utilizes carrier power for carrier estimation

■ Costas Loop: $\frac{1}{\sigma_{\phi_c}^2} = \rho_C \cdot S_{L_C} = \frac{P_t}{N_o B_L} \left(1 + \frac{1}{2R_d} \right)$

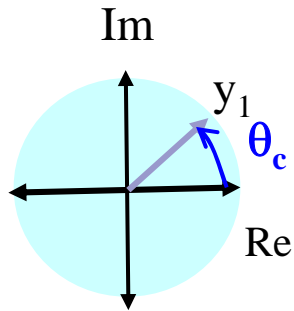
- SL is independent of the iteration process, for a given SNR.
- Suppressed carrier scenario

■ IRCS:

$$\frac{1}{\sigma_{\phi_c}^2} = \rho_{IRCS} \cdot S_{L_{IRCS}} = \frac{P_T}{N_o B_L} \left(1 + \frac{2}{A} \right)^{-1}$$

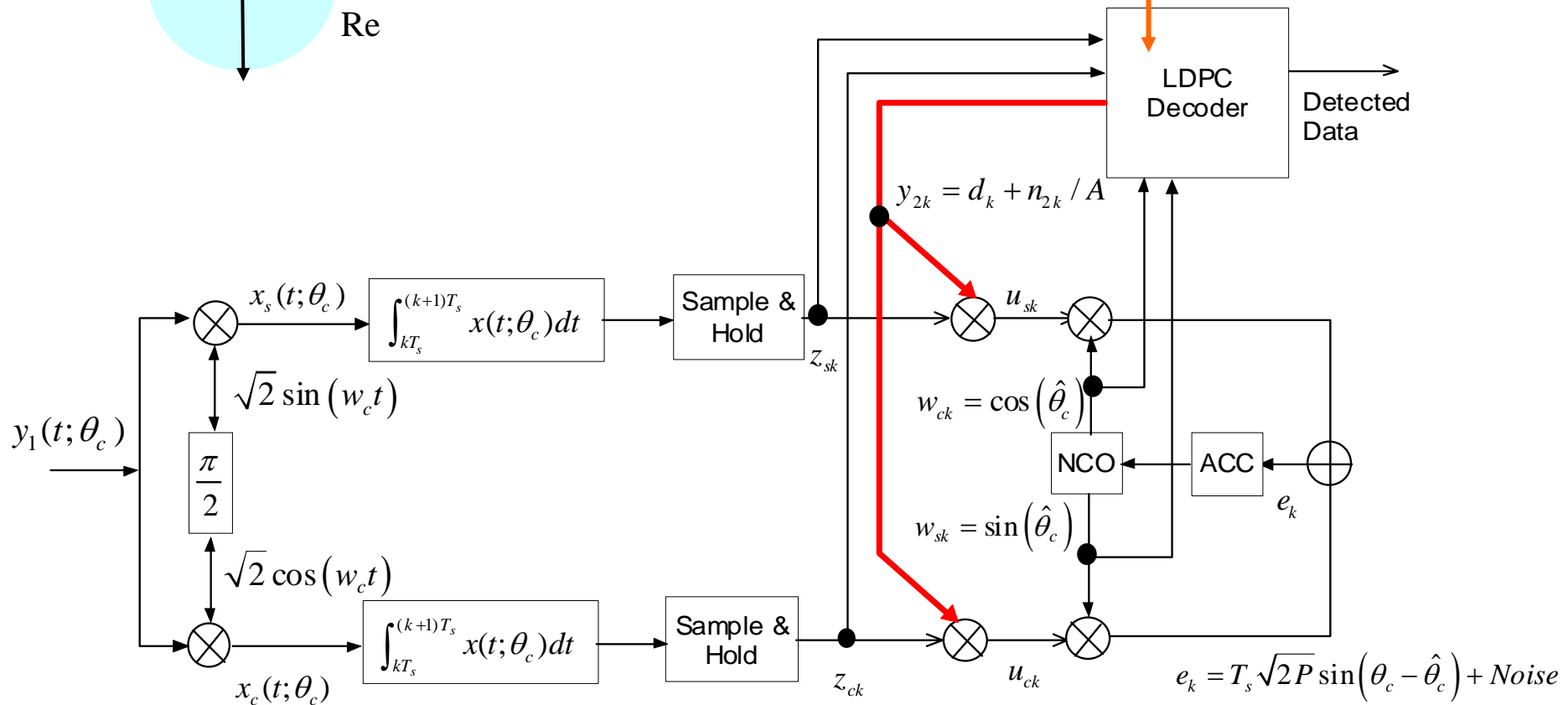
- SL approaches unity as the number of LDPC iterations increase
- Suppressed carrier scenario

BPSK Digital Circuit Implementation



**LDPC LLR
Inputs:**

$$Q_k = \frac{2}{\sigma_{LLR}^2} (z_{sk} w_{ck} + z_{ck} w_{sk}) \quad \text{where} \quad \sigma_{LLR}^2 = \frac{(\sqrt{P}T_s)^2}{2 \frac{E_s}{N_o}}$$



$$x_c(t; \theta_c) = \sqrt{PT_s} m(t) \sin(\theta_c) + \text{Noise}(t; \theta_c)$$

$$x_s(t; \theta_c) = \sqrt{PT_s} m(t) \cos(\theta_c) + \text{Noise}(t; \theta_c)$$

$$z_{ck} = d_k \sin(\theta_c) + \text{Noise}$$

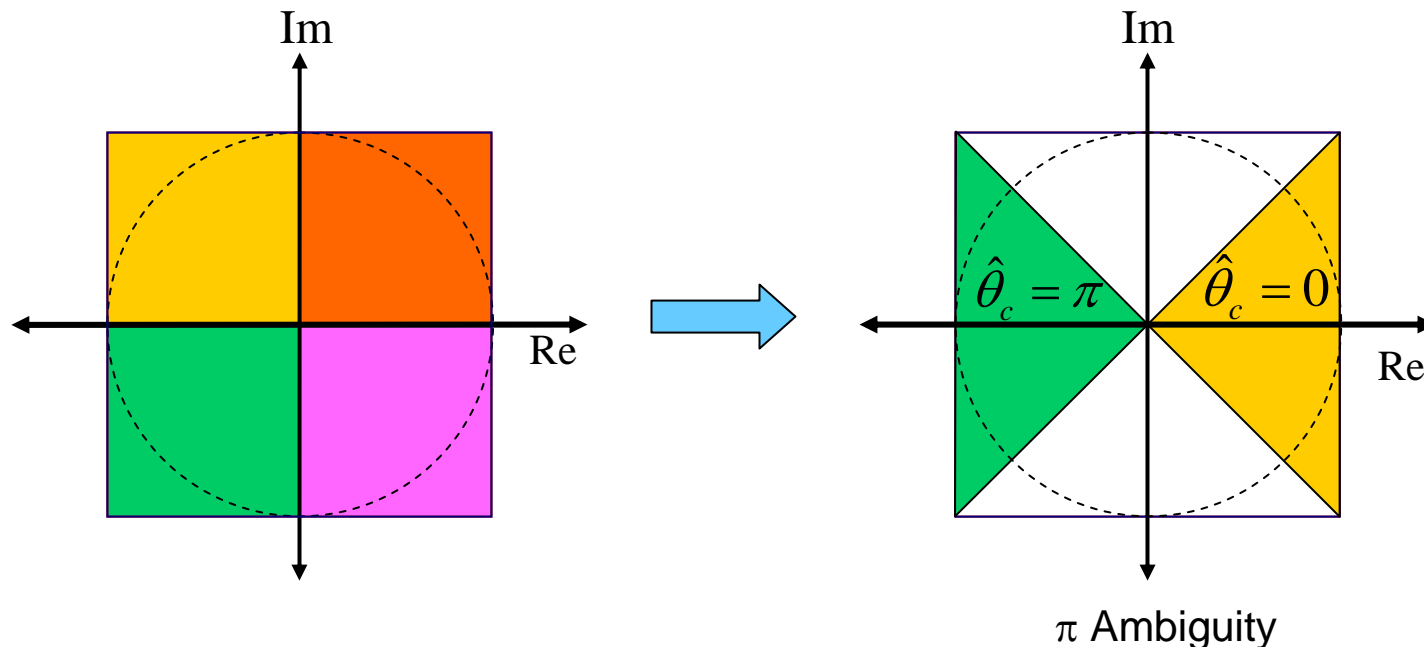
$$z_{sk} = d_k \cos(\theta_c) + \text{Noise}$$

$$u_{ck} = A \sin(\theta_c) + \text{Noise}$$

$$u_{sk} = A \cos(\theta_c) + \text{Noise}$$

BPSK : Algorithm Initialization

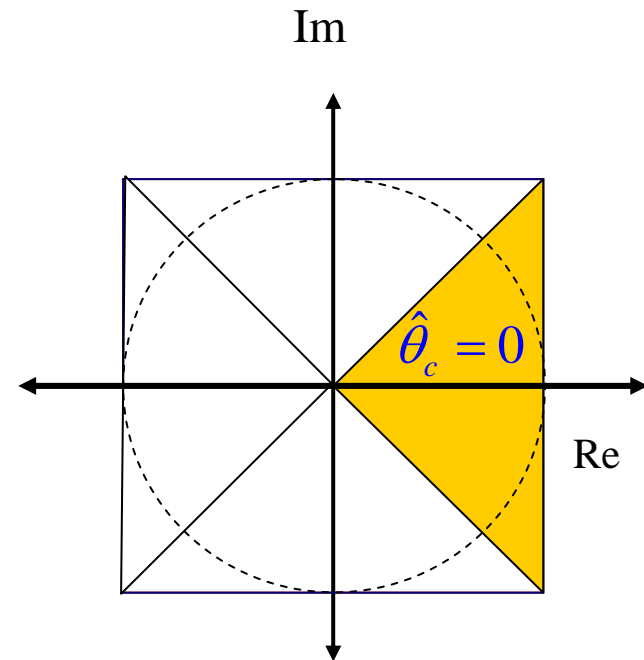
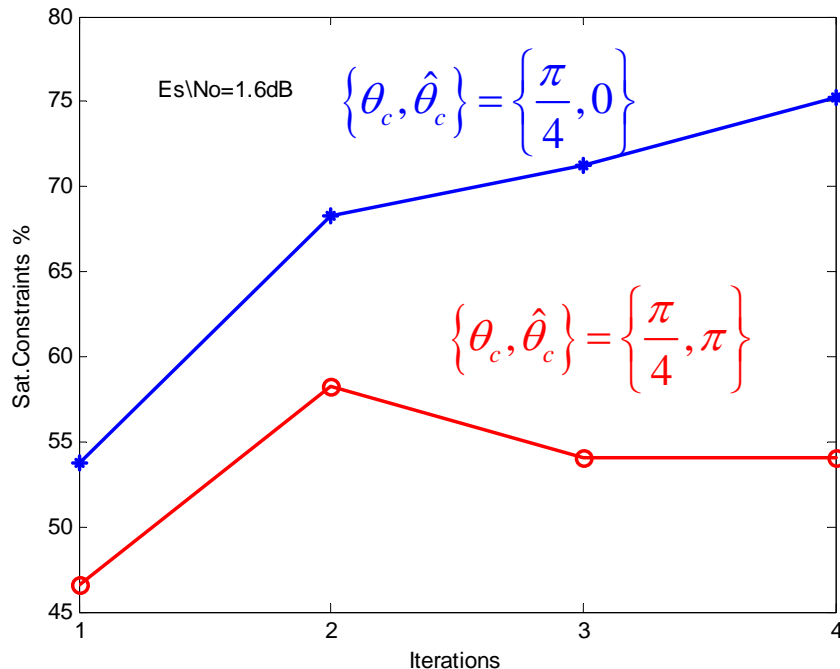
- **Step 1:** Resolve initial phase ambiguity
- Measure average power across a single codeword of the signals z_c and z_s .
 - Choose component with *higher power* to initialize the phase estimation process
 - An error of 180 degrees may remain



BPSK : Pilotless Phase Ambiguity Correction

■ Step 2: Remove possible 180° offset

- Run a single PLL pass
- Run up to 4 LDPC iterations and choose the orientation that produces the maximum **percentage of satisfied constraints** on **odd degree check nodes** (even degree checks remain satisfied after a π rotation of its inputs)



BPSK Main Decoding Algorithm

■ Step 3:

For i=1 to **Max_Iterations**

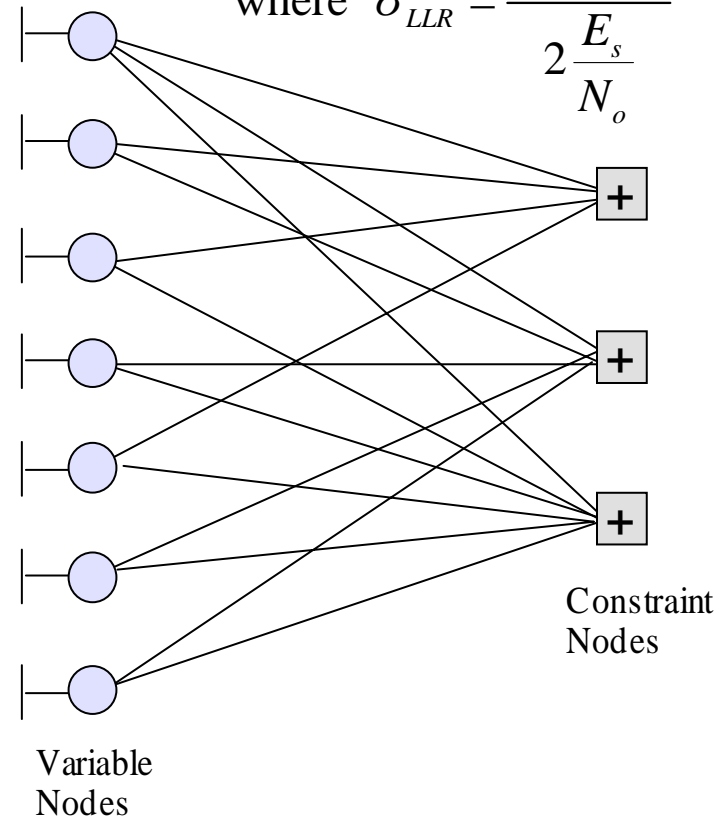
1. Estimate Carrier Phase Offset
2. For j=1 to **LDPC_iter**
 - Update Variables
 - Update Constraints
3. Update Variables
4. Go to 1

■ Performance plots in the next slides are shown for $LDPC_iter = \{1, 2\}$

■ BER/FER performance starts to degrade for cases where phase estimates are computed after a higher number of decoder iterations.

$$Q_k = \frac{2}{\sigma_{LLR}^2} (z_{sk} w_{ck} + z_{ck} w_{sk})$$

$$\text{where } \sigma_{LLR}^2 = \frac{(\sqrt{P}T_s)^2}{2 \frac{E_s}{N_o}}$$

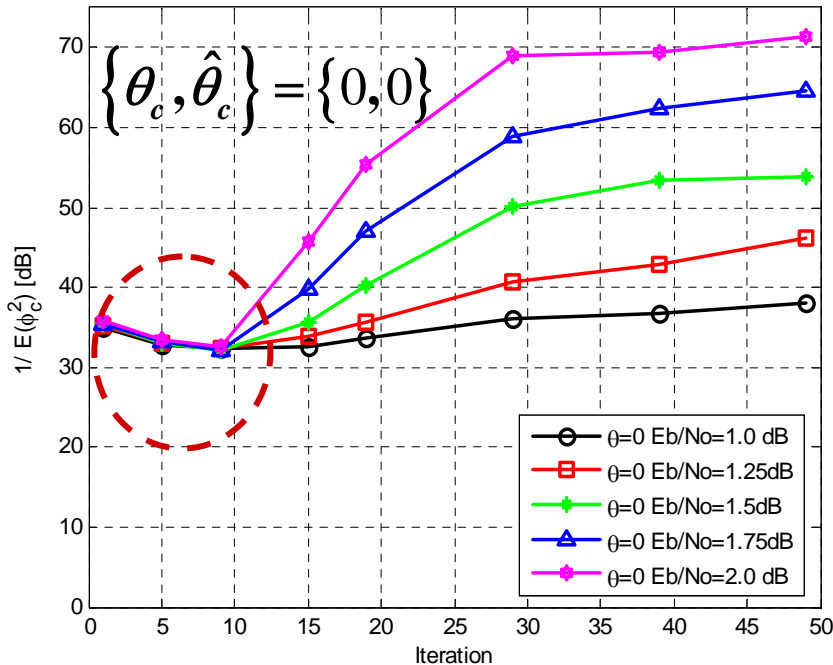


Experimental Results: Loop SNR

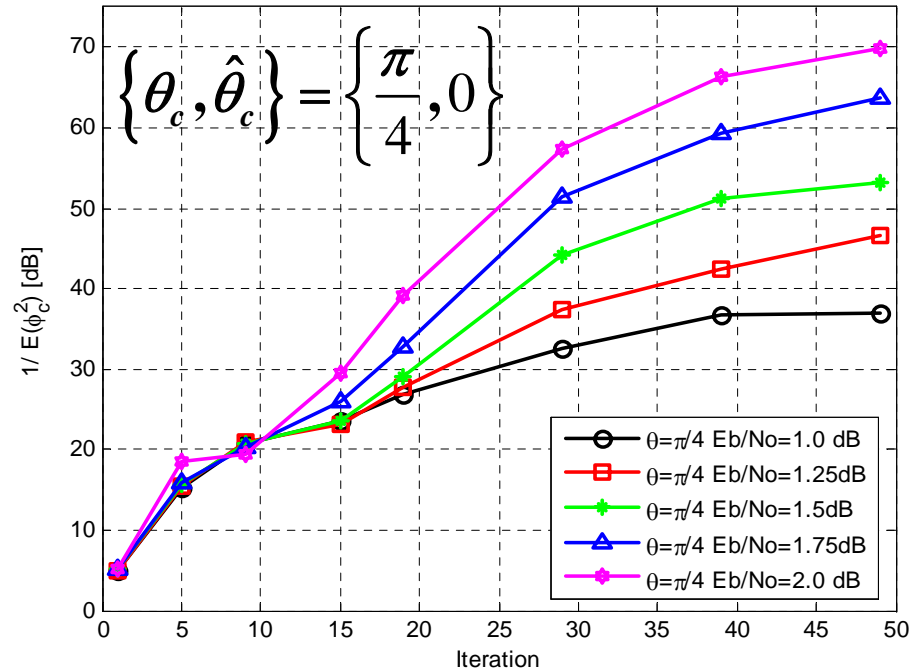
- Plot shows loop SNR vs Iterations. $\theta_c=0^\circ$ and $\theta_c=45^\circ$

$$\text{Loop SNR} = \frac{1}{\sigma_{\phi_c}^2}$$

1 Loop Update every 2 LDPC Iterations



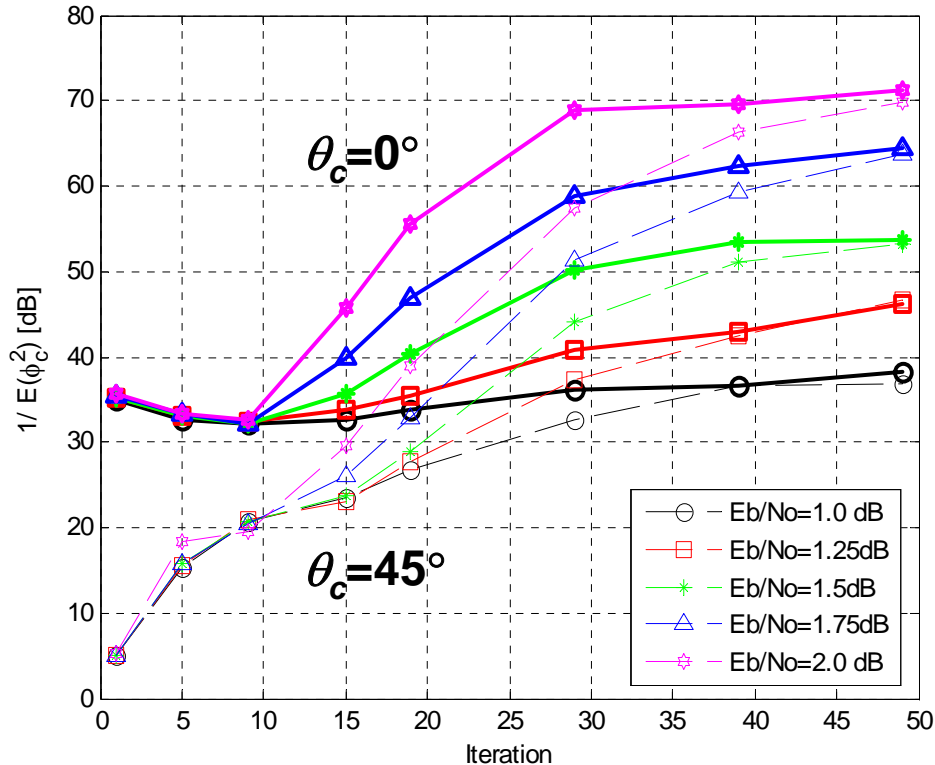
1 Loop Update every 2 LDPC Iterations



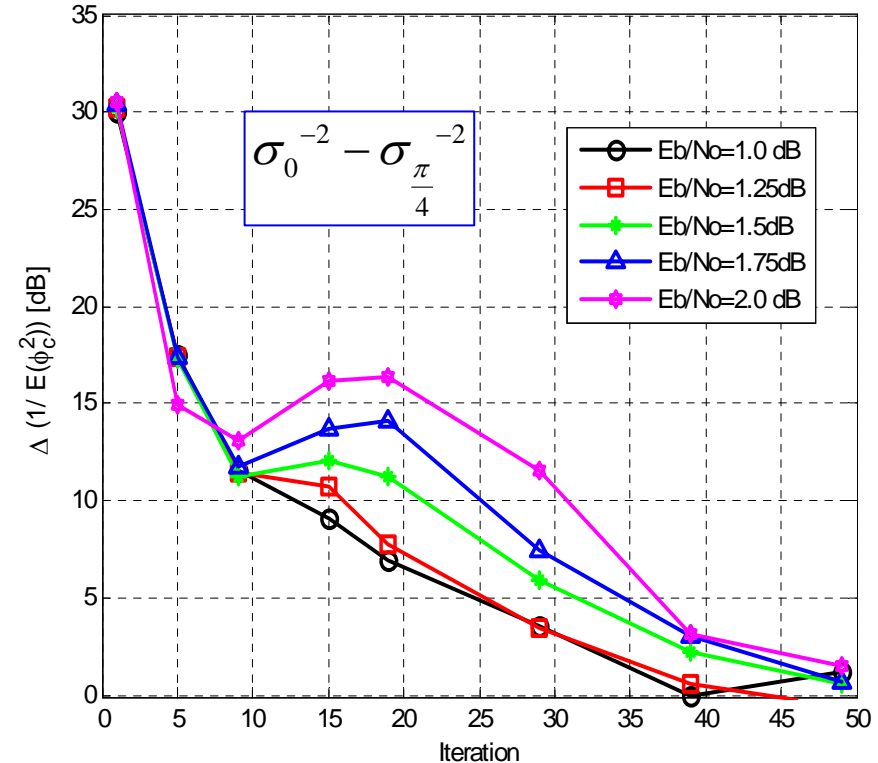
- Note the curious performance for the $\theta_c = 0^\circ$ case.
- In this region the initially correct PLL's phase estimate is affected by poor initial LDPC soft-symbol estimates.
- Both LDPC estimates and loop-SNR dramatically improve after the 10th iter.

Experimental Results: Loop SNR

1 Loop Update every 2 LDPC Iterations

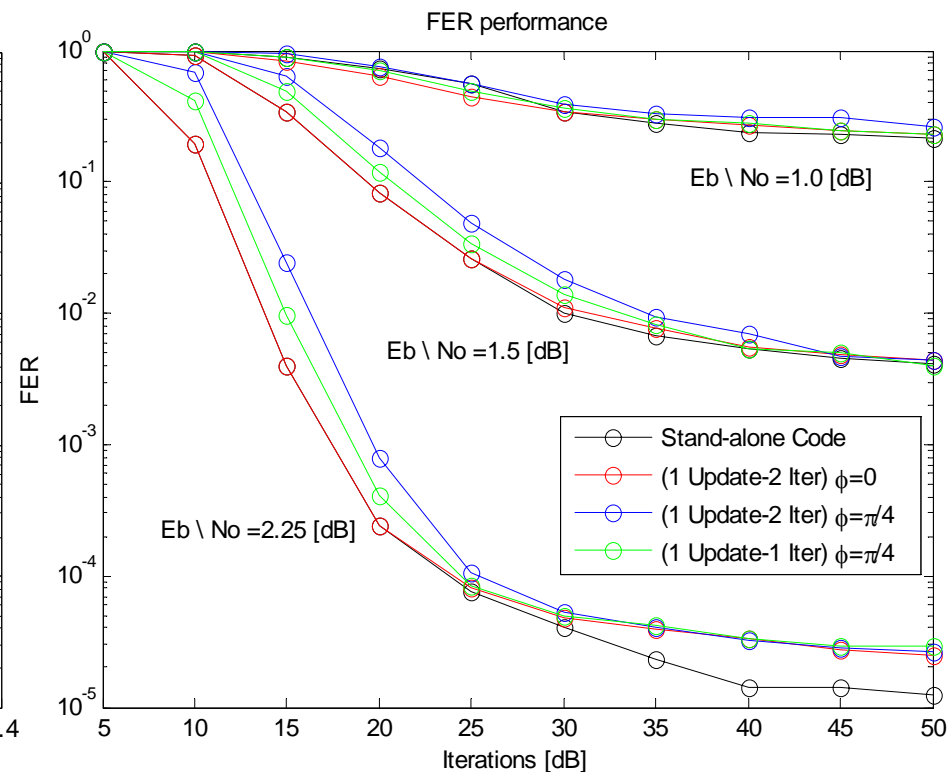
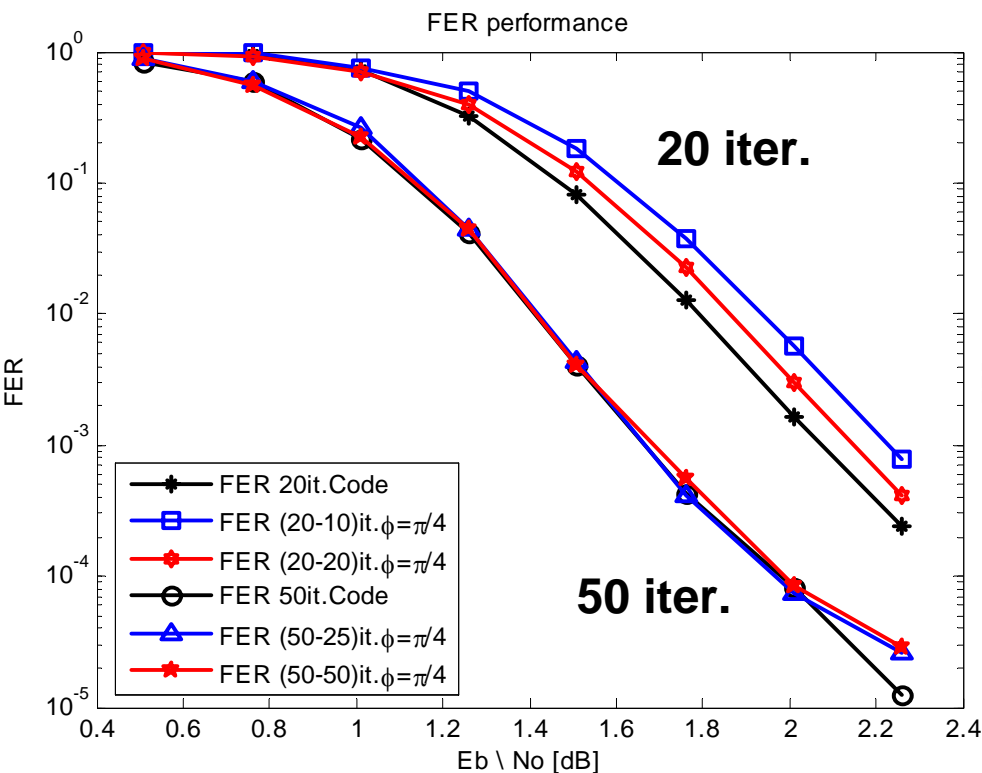


Loop SNR Difference



- ❑ Steady State is reached after 50 iterations
- ❑ As we will see in the next slide this means that
 - ❑ Some loss occurs with a reduced number of iterations.
 - ❑ After 50 iterations, a small marginal degradation in loop-SNR remains

BPSK Frame Error Rate Performance



20 Iterations

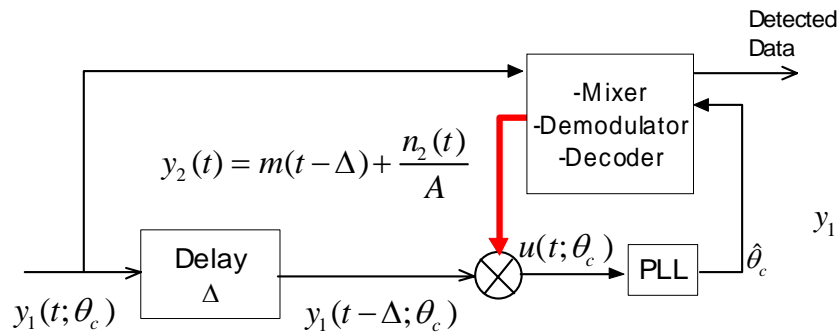
- ❑ Loop did not reach Steady State
- ❑ Performance loss at a FER of $1e-3$ is
 - ❑ 0.15dB with a (20-10) = (1 Loop update every 2 LDPC iterations) scheduling
 - ❑ 0.07dB in the (20-20) = (1 Loop update every 2 LDPC iterations) scheduling

50 Iterations

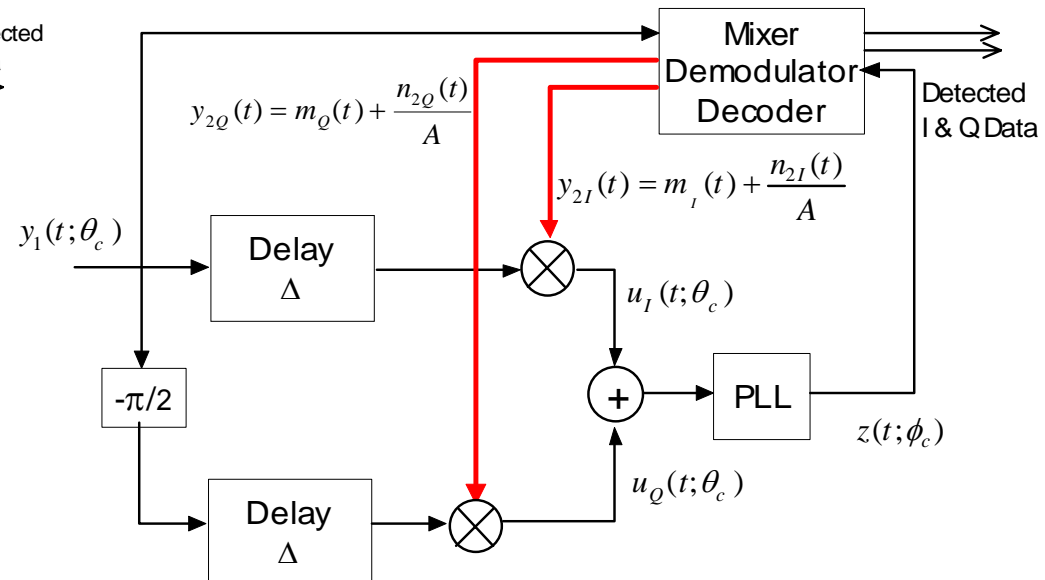
- ❑ Loop in Steady State
- ❑ Small performance difference after 50 iterations due to loop-SNR marginal degradation

QPSK Analog Circuit Description

BPSK



QPSK



- The QPSK IRCS carrier recovery circuit follows the same principles as its BPSK counterpart
- Symbol feedback is now done for the real and imaginary signal components

Squaring Loss (SL) for QPSK systems

- Recall the BPSK SL expression:

$$S_L \triangleq \left(1 + \frac{\sigma^2}{A^2}\right)^{-1} = \left(1 + \frac{2}{A}\right)^{-1}$$

- For our QPSK system :

$$S_L \triangleq \left(1 + \frac{(1 + R_d)\sigma^2}{A^2}\right)^{-1} = \left(1 + \frac{2(1 + R_d)}{A}\right)^{-1}$$

where the noise variance factor $(1 + R_d)$ (R_d : Input Data SNR) comes from the presence of a quadrature (signal x noise) term. [Simon06]

- The penalty in performance due to the R_d term becomes insignificant for low symbol SNR scenarios.
- No 4th order (signal x noise) or (noise x noise) in the loop as in QPSK Costas or hard-decision IRCS loops.

Conclusions

- We have demonstrated a method for improving the carrier synchronization function for iterative BPSK using soft output information from an LDPC decoder .
- Motivation is to overcome the performance loss due to a noisy signal reference at low SNRs, characteristic of suppressed carrier loops such as the Costas loop.
- Steady state operation is reached after around 45 LDPC iterations.
- Performance degradation with respect to the perfect phase information case, in steady state and with a proper loop update schedule, is smaller than 0.1dB.

References

- M. Simon and S. Million, “Residual versus Suppressed-Carrier Coherent Communications” *TDA Progress Report*, vol. 42-127, Nov. 15, 1996.
- N. Noels, V. Lottici, A. Dejonghe, H. Moeneclaey, M. Luise, and M. Vandendorpe, “A theoretical framework for soft-information-based synchronization in iterative (turbo) receivers,” *EURASIP Journal on Wireless Communications and Networking*, vol. 2005, pp. 117–129, 2005.
- M. Simon and V. A. Vilnrotter, “Iterative information-reduced carrier synchronization using decision feedback for low SNR applications,” *TDA Progress Report*, vol. 42-130, Aug. 15, 1997. [Online]. Available: [http://tmo.jpl.nasa.gov/progress report/42-130/130A.pdf](http://tmo.jpl.nasa.gov/progress%20report/42-130/130A.pdf)
- M. Simon and A. Tkacenko, “An iterative information-reduced QPSK carrier synchronization scheme using decision feedback for low SNR applications,” *TDA Progress Report*, vol. 42-164, Feb. 15, 2006. [Online] Available: [http://tmo.jpl.nasa.gov/progress report/42-164/164H.pdf](http://tmo.jpl.nasa.gov/progress%20report/42-164/164H.pdf)
- S. Chung, T. Richardson, and R. Urbanke, “Analysis of sum-product decoding of low-density parity-check codes using a Gaussian approximation,” *IEEE Trans. Inform. Theory*, vol. 47, pp. 657–670, Feb. 2001.