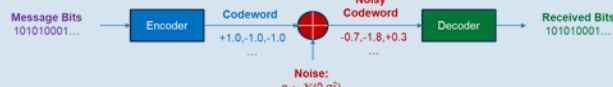


## Introduction and Background

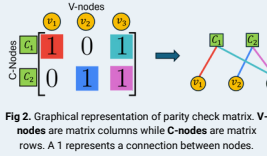
Satellites need **reliable** and **fast** communications to meet requirements set forth by the Space Development Agency (SDA) standard [1]

### Why LDPC

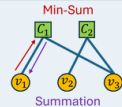
- Problem:** Noise over the communication channel can corrupt transmitted data
- Low Density Parity Check (LDPC)** is an error correcting code applied to the transmitted data in order to recover noisy messages using a decoder



### LDPC Codes



- Parity Check:** Method where additional bits called **parity bits** are added to determine integrity of original message
- Specific parity checks are defined by a **parity check matrix**
- Parity check matrix can be represented by a graph
- V-nodes** represent codeword bits and **C-nodes** represent parity checks



- Message passing algorithm:** Decoder works by passing messages back and forth in between **C-nodes** and **V-nodes**
- C-nodes typically uses the **Min-Sum algorithm** to process information from V-nodes [2]

### FPGA



Fig 4. The ZCU106 FPGA board used for the experiment

- LDPC decoders are typically implemented on **customizable chips made up of logic tables called Field-Programmable Gate Array (FPGA)**
- More flexible than digital circuits
- Runs faster than general purpose processors

### Current Limitations

- The SDA standard uses the **5G NR parity check matrix**
- The **5G NR Parity Check Matrix** is divided into **384x384** **circulants** (shifted identity matrices) [3]
- Circulant property allows decoders to perform **384 parallel computations**
- However, this over parallelization **occupies too much chip area** and **large chip area consumes too much power**

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Fig 5. An example of a circulant

### Objective

Design a smaller and more power efficient LDPC decoder for the 5G NR standard on an FPGA that maintains the target data rate of 2.05 Gigabits per second (Gbps)

## Materials and Methods

### Design Changes



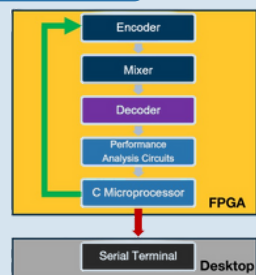
### Circulant Splitting

- Split 384x384 circulants into 32x32 sub-circulants to **reduce parallelization and chip area**
- Smaller chip area **reduces power consumption** at the **cost of lower data rate**
- Fig 6a. shows that splitting a circulant into smaller matrices doesn't result in sub-circulants
- Fig 6b. and Fig 6c. show how columns and rows are rearranged to create sub-circulants
- Reordered columns means **decoder must reorder codeword bits**

### Other Optimizations

- Pipelining** splits the decoding process into stages, increases throughput
- Min-Star** algorithm is used instead of the Min-Sum algorithm, which gives better decoding performance at the cost of a slight increase in computational complexity

### Experimental Setup



- 4800 codewords are randomly generated from the **encoder** and sent to the **mixer**
- Mixer** adds noise to codeword and produces probabilistic representations for each bit
- Decoder** takes in **noisy codeword** and attempts to output correct message bits
- Performance Analysis Circuits** keep track of bit and codeword errors based on output of decoder
- C Microprocessor** collects bit and frame error data and repeats steps 1-5 until 75 codeword errors are detected
- Data collected by the **C Microprocessor** is displayed via **Serial Terminal** on a desktop

## Parameters

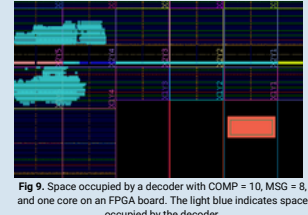
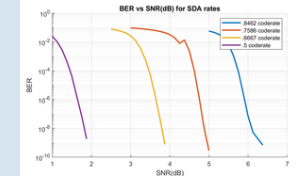
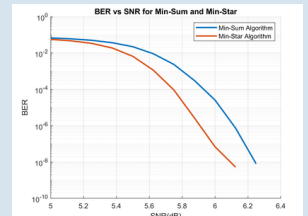
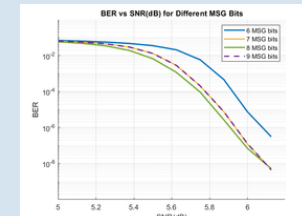
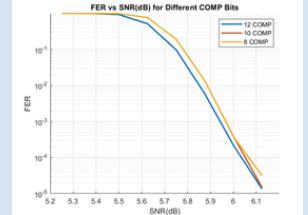
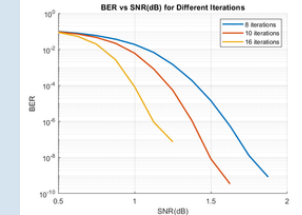
### Changed

- COMP bits:** Number of bits used to represent V-nodes
- MSG bits:** Number of bits used for Min-Star
- Max iterations:** Max times messages are sent in decoding
- Code rate:** Ratio of number of message bits to total number of bits sent
- SNR(Signal to Noise ratio):** How much noise is added to the signal

### Measured

- Frame error rate (FER):** How often a codeword is incorrect. Measures **decoding performance**
- Bit error rate (BER):** How often a bit is incorrect. Measures **decoding performance**
- Data rate:** How fast the decoder outputs bits. Measures **speed**
- Cores:** Number of decoders that can fit on a single FPGA board. Measures **chip area**

## Results and Discussion



- Increasing iterations improves **decoding performance**, but decreases **speed**
- Increasing COMP and MSG bits improves **decoding performance** with diminishing returns at the cost of **chip area**
- The parameters with the best tradeoff of **decoding performance**, **speed**, and **chip area** is **8 max iterations, 10 COMP bits, and 8 MSG bits**
- A single FPGA board can fit **17 cores**
- The optimized decoder runs at the target data rate of **2.05 Gbps** using the optimized parameters
- Min-Star improves **decoding performance by 0.2 dB of SNR** over Min-Sum

## Conclusion

- Splitting the parity matrix into smaller parts allows the decoder to **occupy less space on the FPGA**. The decreased chip area **lowers the decoder's power consumption at the cost of lower data rate per core**. However, we can place more cores on a single FPGA to recover the data rate
- Pipelining increases data rate of optimized decoder
- Using Min-Star over Min-Sum **improves decoding performance by 0.2 dB of SNR**
- The optimal parameters for the decoder are **10 COMP, 8 MSG, and 8 max iterations**. With these parameters, a single FPGA board can fit **17 cores** to achieve the required data rate of **2.05 Gbps**
- With our decoder, satellites can meet the data rate and reliability requirements of the SDA standard

## Future Work

- Modify stopping condition** of decoding process by either **checking fewer parity bits** or using a **cyclic redundancy check (CRC)**, an error detection method, on the message bits
- Further reduce memory and FPGA resource utilization to fit more decoders on FPGA
- Test data rate and **record power consumption** of optimized decoder on satellite

## References

- [1] Space Development Agency, "Optical Communications Terminal (OCT) Standard Version 3.1.0", 2023, pp. 53
- [2] AMD, "LDPC Encoder Decoder v1.0 Product Brief (PB052)", 2022, pp. 3
- [3] 3GPP, "5G NR; Multiplexing and channel coding (3GPP TS 38.212 version 15.2.0 Release 15)", 2018, pp. 16-18

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