On Low Power Self Organizing Sensor Networks

A dissertation submitted in partial satisfaction of the requirements for the degree Doctor of Philosophy in Electrical Engineering

by

Katayoun Sohrabi

2000
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The dissertation of Katayoun Sohrabi is approved.

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2000
DEDICATION

This dissertation is dedicated to my loving parents.
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when the possibility of working with self-organizing wireless networks presented itself, something just clicked inside and I saw the light, so to speak.

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ABSTRACT OF THE DISSERTATION

On Low Power Self Organizing Sensor Networks

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This dissertation presents the problem of building a wireless sensor network. Low radio range, potentially high node density, and limited energy reservoirs at each sensor node, in addition to the need for small size, impose stringent requirements for low energy and low complexity on algorithmic and hardware design.

Designing efficient wireless communications for sensor networks requires understanding of the propagation medium. In a sensor network, antenna heights are typically low, since sensor nodes are most likely deployed near surfaces, i.e. on the ground or floor. We present the first characterization of near ground RF channel at the 800 MHz-1GHz band. Our experiment indicates that a fourth power law is a suitable model for characterizing the path loss.

Then we propose a method for network link layer self-organization. The Self-organizing Medium Access Control for Sensor-nets (SMACS) enables a wireless nodes to form a connected multi-hop network. To reduce energy consumption,
radio communication between the nodes must be scheduled, and not contention based. However, traditional methods of scheduling node activities, such as the various well known “link activation” and “node activation” algorithms require some form of network-wide time synchronization. They also require nodes to have information about radio topology of the network in order to avoid packet collisions. The key innovative mechanism of SMACS is that, by use of a hybrid TDMA/FH method which we call non-synchronous scheduled communication, it enables links to be formed and scheduled concurrently throughout the network without the need for costly exchange of global connectivity information or time synchronization.

We also introduce a mechanism for code synchronization on point to point links in wireless sensor networks. The Transmitter Aided Code Acquisition (TACA) method, enables frequency hopping for a packet network, where packet lengths are short. It uses randomly assigned long codes, specific to transmitters, to control frequency hopping on links. The transmitter inserts a sequence of tones between packets, conveying in coded form, the value of the hopping pattern’s phase. Only the intended receiver(s) will be able to decode this information. Simulation and analysis results for performance of TACA will be given.
Chapter 1

Sensor Networks

Now that the nervous system of the cyberspace has been put in place, in the form of the Internet, the next step is to form an electronic skin around the earth. This will be realized by means of instrumenting our world [1], and possibly other worlds in our solar system [2], with many wireless sensor nodes, and then connecting them to the Internet [3].

One of the building blocks of this electronic skin is the Wireless Integrated Network Sensor or WINS [4]. A single WINS node combines microsensor technology, low power signal processing, low power computation, and low power, low cost wireless networking capability in a compact system. These components are needed to support the basic capabilities of the sensor node which are:

1. Sensing or/and actuation
2. On board signal processing
3. Communications capability (RF, IR, Optical)

The node is responsible for the sensing task and processing the data collected
by its local sensor(s). The nodes must also perform collaborative signal processing
tasks on the pool of data gathered by some local neighborhood of nodes. The
sensor data may also need to be transported across the sensor network to reach
a certain information sink in the sensing arena.

Wireless sensor networks will be able to replace or enhance traditional wired
sensor technology as stand alone systems in disaster recovery, inventory control,
home security, manufacturing, and a myriad of other applications. They may
also be used in novel ways which we are just beginning to grasp today. For
example sensor networks may be used to monitor vital signs on patients and
soldiers. A variety of temperature, moisture, blood pressure, heart rate monitor
sensors, and GPS locators may be worn or placed on the body of a person which
will form a personal area network. A local central processing node may track
the data collected by the sensors, and send information to remote monitoring
posts. Another very exciting application for sensor networks is the role they
can play as the enabling technology for smart spaces [5] [6] [7] [8]. Individual
items in the specific space may be instrumented by means of tags or sensors to
form a local area network. The higher layer of the network stack will then be
designed to make possible interaction between the instrumented components in
an autonomous manner.

Imagine an environment such as a grocery store. A context for this environ-
ment can be the example of a person shopping in the store. The customer picks
up items from grocery racks and puts them in her basket. When finished, she
walks out of the store passing a sensing portal on her way without the need for
explicit checkout. The tags on grocery items are able to detect being picked up
by the customer. The shopping basket is outfitted with wireless sensors which
are networked to the store’s central inventory control system. The items sold by weighed are measured in the basket and priced. The total cost of the items is deducted from customers’s bank account when she leaves the store.

This model illustrates the interaction of a variety of data/information/sensor networks together.

- The Body Area Network, BAN, of the customer, comprising of her local life sign sensors and her personal identifier which upon entering the store identifies her and signals the beginning of a potential transaction period. This is a possible application for wearable computers [9, 10].

- Sensor network instrumentation of the store itself and tagging of products in the store and the shopping cart. This enables pricing and automatic inventory control.

- The secure data network which facilitates the financial transaction between the customer’s bank account and the store.

1.1 State of the ART

The following list includes representatives of various wireless sensor concepts, or ideas related to them up to date:

- UCLA’s LWIM program [11] addressed the sensor integration and basic wireless networking issues for sensor networks. The AWAIRS [12] project addressed some higher layer problems such as array signal processing, beam-forming, collaborative signal processing, and sophisticated self-assembly
and routing issues for the wireless network and data collection methodologies.

- Piconet [13] which was developed at Olivetti and Oracle Research Laboratory (now AT&T Research Laboratories UK), is an ad-hoc wireless network which uses low-level radio and networking protocols. Its goal is to use very simple FM modulation, and short datagrams to relay data between every day objects. Unlike LWIM and AWAIRS networks which are multihop, the early version of Piconet is a single hop network.

- The Active Badge system [14] was also developed at AT&T Research Laboratories UK. It is designed to locate individuals indoors. A person wears an active badge which can be located by the system. The badge transmits a unique infra-red signal every 10 seconds. Each office within a building is equipped with one or more networked sensors which detect these transmissions. The location of the badge (and hence its wearer) can thus be determined on the basis of information provided by these sensors.

- The sensor dust concept [15] proposes to use corner cubed reflectors to enable directed optical communications between very small MEMS sensor motes. Individual nodes are millimeter scale sensing and communication platforms. These networks can consist of hundreds to thousands of dust motes and a few interrogating transceivers. Each mote consists of sensors, a power supply, analog and digital circuits, and a communication transceiver. The motes are built from integrated circuit and micromachining processes for low cost, low power consumption, and small size.
The Factoid system [16] is a collection of hand held systems similar to key-less entry objects. They exchange information with their environment as they come in contact with other factoids. The only I/O device on the factoid is a 900MHz radio with a range of 30 feet. There is no power switch, as the Factoid is always turned on. The device fits on a keyring using not much more space than a key. The interesting challenge is the ordering and extraction of information from the data depository generated by an individual’s factoid.

In addition to these systems DARPA’s SensIT program [17] and MURI 2000 [18] projects support ongoing research efforts related to various layers of sensor networks.

1.2 Design Challenges for Sensor Networks

The different form factor, operating environment, traffic type, energy source, delay, throughput, and robustness requirements, and the potential for a very large number of nodes make sensor networks inherently different from existing data networks. For this reason the sensor network must be engineered from the ground up in many aspects. The challenges may be grouped under three major categories:

- Hardware: this category includes the entire range of design activities related to the hardware platforms which comprise sensor networks. MEMS sensor technology is an important aspect of this category [19]. Digital circuit design and system integration for low power consumption is also in
this category [4]. Design of a low power sophisticated RF front end and associated control circuitry is also an important issue here.

- Wireless networking: engineering of physical, MAC, and networking layers of the system falls in this category. The signalling, modulation, source and channel coding must be designed to fit to the unique requirements of sensor networks. Channel access methods must be devised to be able to support hundreds to tens of thousands of terminals in the network. Due to small form factor and sensing tasks, new antenna designs which are suitable to near surface and other types of new propagation media must be found. Network self-organization and energy saving routing algorithms must also be designed for wireless sensor networks. The problems which are investigated in this work all fall in this category.

- Information Technology: The information technology design aspect for sensor networks aims to create effective and new capabilities for efficient extraction, manipulation, transport and representation of information derived from sensor data. This category deals with design issues for layers above the lower three ISO stack layers. At the time of writing of this document, most of the solutions in this category are related to the routing problem.

USC/ISI’s SCADDS project [20] aims to use scalable coordination architectures along with directed diffusion techniques and adaptive fidelity algorithms to manage and extract information. In this approach the data is addressed, and not at the node which generated it. MIT’s SPIN protocol [21] uses data negotiation and resource-adaptive algorithms. Nodes running SPIN assign a high-level name to their data, called meta-data, and perform
meta-data negotiations before any data is transmitted. This assures that these is no redundant data sent throughout the network. In addition, SPIN has access to the current energy level of the node and adapts the protocol it is running based on how much energy is remaining.

The underlying challenge of engineering wireless sensor networks is that, in order to really save energy a good solution must consider the entire protocol stack and the hardware.

### 1.3 Original Accomplishments

The work which will be presented here is concerned with wireless networking issues for sensor networks. In this presentation we start with the physical layer and work our way up to the link layer. At the physical layer, we introduce novel results for channel propagation measurements for ground-lying antennas. This is a situation which is encountered in sensor networks, where the nodes must be placed near surfaces. After that we focus on two distinct but related questions: how to maintain the individual links in the network and how to start up a network. The first problem approaches the code acquisition for a bursty slow frequency hopping point to point link in a wireless sensor network. To solve the last problem we explore mechanisms for self-organization at the link layer which is directly tied to Medium Access Control design.

**Near Ground Channel Propagation Measurement**

Prior to publication of our channel measurements, no models were reported in the literature which dealt with characterizing propagation phenomena where the
antenna heights are below one meter. This situation, is however, precisely the condition for radio propagation in sensor networks. Frequency domain channel propagation measurements in the 800 MHz-1GHz band were performed with ground-lying antennas. The range of path-loss exponent and shadowing variance for indoor and outdoor environments were determined. It was found that the range of these values roughly agree with those measured for higher elevation antennas. However, the coherence bandwidth was found to vary significantly with distance and in various settings. The details of channel measurement results are given in Chapter 2.

**Transmitter Aided Code Acquisition for slow frequency hopping**

In the second part of this dissertation the problem of code synchronization for bursty, slow frequency hopping communications is described. The limitations of existing solutions with regard to this issue will be given, and our solution will be discussed in detail. The main thrust of the proposed solution is that the transmitter must aid the receiver in acquiring the code. To do this the transmitter inserts certain extra signals in its transmission stream which will act as *hooks* to align the receiver’s code phase with the transmitter phase.

The problem of code generation and acquisition for the wireless sensor network is unique, because of low energy and low complexity requirements. Fortunately with the advent of highly sophisticated, low energy radios, it is possible to do wideband, slow frequency hopping. The question is how to enable robust code synchronization. We propose to do this by having the transmitter embed markers in its stream which lead to the location of the code phase. The details of the TACA method, and its ability to maintain code synchronization under
various network topologies, and traffic conditions will be given in Chapter 3.

**Self-organizing Medium Access Control for Sensor Networks (SMACS)**

The SMACS procedure enables the formation of an infrastructure, on the fly, for sensor networks. The unique aspect of the protocol is its ability to form a connected network, without the need to establish global synchronization throughout the collection of participating nodes. The SMACS procedure is able to build a flat and multihop topology for large network sizes.

The innovative approach of our solution is the Non-synchronous Scheduled Communication (NSC) mechanism, which enables the links to be formed concurrently throughout the network, without the need for complete radio connectivity information. In Chapter 4 detailed background about the self-organization problem for wireless ad-hoc networks will be given. The details of the SMACS procedure and its performance will be given in Chapter 5. The concluding remarks will be given Chapter 6.
Chapter 2

Channel Propagation Measurements

RF propagation conditions for ground-lying antennas are important in wireless sensor networks. The radio environment for this kind of wireless RF transmission consists of small range propagation with very low elevation antennas (less than one meter height). The 900 MHz ISM band is one possible operating frequency band for the wireless sensor network.

The propagation environment impacts the performance of a wireless communication system to a great extent. Prior to this work, no channel models had been introduced in the literature that focused on low antenna heights and limited range. In this chapter, the results of a set of channel measurement experiments aimed at characterizing this type of channel are given. The chapter is organized as follows: first a short description of the channel models and measurement methods for characterizing them will be given. Next the details of our measurement technique are discussed. Finally the channel measurement results for path loss
and channel frequency selectivity are given. The chapter ends with concluding remarks.

## 2.1 Radio Propagation Phenomena

The radio channel degrades the transmitted signal in many ways. These may be categorized under large-scale and small-scale effects. The large-scale phenomena deal with variations of the mean signal level over large distances (compared to the signal wavelength) or large time intervals. The small-scale effects are due to signal variations about the signal mean and are modeled as caused by changes in the local neighborhood of the receiver. The local neighborhood in this case is comparable to the signal wavelength, or time intervals needed to cover comparable distances, in the case of mobile communications.

The major parameter that characterizes large-scale effects is path loss. Path loss refers to the difference between the transmitted power and received power in (dB) \[22\]. This power loss is due to loss of energy density due to spreading of the electromagnetic wave-front reaching the receiver as well as interactions of the signal with the propagation medium. The path loss directly controls the power drain in a transmitter, since it determines radio coverage of the transmitter for various transmit power levels.

The small-scale channel variations may be grouped together under the "fading" heading. Before a digital pulse is transmitted over the channel its energy is confined to a certain time and frequency interval. After passing through the channel, depending on the pulse parameters, and characteristics of the channel the pulse may be dispersed in time or frequency or both.
Frequency dispersion is due to relative motion of transmitter and receiver and appears as Doppler spreading of the transmitted signal. Time dispersion manifests itself in “flat” or “frequency selective” fading. In flat fading, the channel frequency response is flat in amplitude and linear in phase over the bandwidth occupied by the signal of interest. In frequency selective fading, the frequency response of the channel varies over the signal bandwidth. In this case, the channel coherence bandwidth corresponds to the average frequency band over which the frequency response stays constant. A concise treatment of the channel models can be found in [22]. More detailed information about the channel models may be found in [23] and [24].

2.2 Measurement Methods

The radio-channel can be modeled as a randomly time-varying linear filter [25]. In order to characterize the channel, it is sufficient to determine its time-variant impulse or frequency response. There are a number of different identification methods used to determine, or estimate, channel response function over wide frequency bands. These include the following [26]:

1. Swept frequency technique: In this method the channel frequency response is measured directly in the frequency domain. A network analyzer is used to make narrow-band measurements of the channel gain and phase response at discrete frequency points in the bandwidth of interest. For this method to be accurate, the channel must not change over the entire duration of a frequency sweep.
2. Pulse technique: The channel impulse response is measured directly in the time domain. A sequence of extremely wide-band pulses, with inter pulse times larger than the channel’s largest path delay is transmitted. The echoes are recorded. From the arrivals and signal strengths of the received echoes the channel impulse response is determined. This method requires wide-band RF filters at the receiver. This means high energy pulses must be used to overcome the large amount of input noise. Also extremely accurate synchronization between the transmitter and receiver is needed.

3. Sliding Correlator technique: In this method a narrow-band pulse is modulated by a direct sequence PN code. The receiver uses the same code, running at a slightly lower rate. This enables the receiver to resolve and lock onto all the echoes of the single transmitted pulse, up to the resolution power of the receiver, which is one-half of the chip interval. However, since the processed signal at the receiver, after despreading, is a narrow-band signal, better noise rejection and lower transmit powers are possible. Also, less stringent synchronization between the transmitter and receiver is required.

2.3 Our Measurement Setup

Since the sensor nodes do not move and we are interested in characterizing the effect of local geometry on the channel, it is reasonable to assume the channel of interest is slowly time varying. For time-invariant channels frequency domain measurements using the swept frequency method is ideal. In this method the complex frequency responses for the channels are measured directly. From this response, path loss, shadowing parameters, and coherence bandwidth of the
channel for various indoor and outdoor environments will be calculated. Precise definitions of the shadowing parameters and coherence bandwidth will be given shortly.

If we model the channel as a two port linear system, then the $S_{21}$ parameter of this system measured over the frequency band of interest, 800MHz-1GHz for instance, will correspond to the channel frequency response. For a two port device $S_{21}$ is the forward transmission coefficient of the output, and represents the ratio of the output signal to the input signal in complex format. The diagram of Figure 2.1 depicts the concept.

\[
\begin{align*}
\text{Incident} & \quad S_{21} \quad \text{Transmitted} \\
\text{Reflected} & \quad \text{Channel} \\
\end{align*}
\]

\[
S_{21} = \frac{c}{a}
\]

Figure 2.1: Two port model of the channel.

The equipment setup and measurement approach used is very similar to the one used in [27]. Figure 2.2 gives a description of the measurement system. In this setup the laptop is used to remotely control the network analyzer and to provide data storage. At various sites, both indoors and outdoors, the frequency response of the channel was measured at regular intervals of transmitter receiver separation. In each site one or more fixed locations for the transmitter antenna were chosen. A long track starting at the transmitter location was determined along which the receiver antenna would be placed. The receiver antenna was
then placed at regularly increasing distances from the transmitter, and for each such distance $m$ local snapshots of the complex frequency response of the channel were made along a local track. These local snapshots would then be averaged in amplitude to give an average frequency response for the specific separation. The measurements were done in a 200MHz band centered at 900MHz. Each snapshot was a collection of 801 points of received signal amplitude and phase in complex format. Frequency separation was 250KHz. The discone antenna [27] used was designed to operate in the band of interest to us and had height of approximately 15 cm. Antennas were placed directly on the surface in each location, i.e. either on the ground or on the floor at each site. Figure 2.3 gives the amplitude of a sample snapshot.

### 2.3.1 Description of Sites

We were interested in measuring channel behavior in a variety of locations where our communications nodes would be placed. This fact and ease of access and
possibility of transporting our measurement equipment to the sites were important factors in determining the sites. The following list gives short descriptions of the sites for which data are presented in this chapter:

1. Engineering I: multi leveled building. This is an old brick structure, with wide hallways, and large lab-like rooms on either side of hallways. Heavy equipment and machinery are present in some labs.

2. Apartment Hallway: commercial apartment complex. This is a building with wood-frame and narrow hallways. A first floor long hallway was our measurement site.

3. Parking Structure: concrete and steel parking structure on UCLA campus. It has 6 levels and open sides.
4. One-sided corridor: a corridor on the side of a modern multi-floored, steel and concrete building. On one side it is open (similar to a long balcony).

5. One-sided patio: very large patio without roof and having only one wall on the 2nd floor of modern steel and concrete building.

6. Concrete canyon: wide alley between large metal frame 7-8 storied structures which comprise the engineering complex on UCLA campus.

7. Plant fence: a thick growth of leafy plants about 1 m high, used as a fence in a garden.

8. Small boulders: a wall of crushed limestone, similar to a surf-break. Antennas were placed on top of the wall.

9. Sandy flat beach: Santa Monica Beach.


11. Dry tall under-brush: tall grassy fields, with few tall bushes.

2.4 Results

As mentioned earlier, each channel snapshot is a collection of 801 complex data points. Each complex number is the S21 parameter of the channel at a fixed frequency in the frequency band of interest. After correcting for the effect of the amplifier inserted in the signal path, the resulting signal is the channel frequency response over the range 800-1000 MHz. Standard data analysis was performed
on the raw data collected at each location to determine power loss laws of the wireless channel and to characterize channel frequency selectivity.

The model used for power loss is described in [22] and [28] where the path loss at distance $d$ between transmitter and receiver, $PL(d)$, is given as:

$$PL(d) = PL(d_0) + 10n\log_{10}(d/d_0) + X_s$$  \hspace{1cm} (2.1)

This formula deals with average path loss at a given separation between transmitter and receiver at a fixed frequency. The reference distance $d_0 = 1$ m and $X_s$ is a Gaussian random variable, when the relationships are taken to be in (dB). The goal of the experiment is to estimate values for $n$ and variance of $X_s$.

Linear regression is used to fit our raw data to this model for each frequency point in the bandwidth of interest. The values of parameters of interest, namely the path loss exponent, $n$, path loss at the reference distance, $PL(d_0)$, and shadowing variance, $\sigma^2$, were found for the entire measurement bandwidth. Over the 200MHz band there are some variations in these parameters. The data given in Table 2.1 and Table 2.2 give the dynamic range of these parameters over the measurement bandwidth. In Table 2.3 the mean of each parameter over the entire bandwidth is given. For example, the power loss exponent for Parking Structure at some frequency $f_x$ will have a value between 2.7 and 3.4 depending on the value of the frequency, and a mean of 3.0. Generally, the path loss exponent agrees with results obtained for other types of channels. The interesting part however, is the fact that the onset of channel behavior is at much closer ranges compared to other channels. The results for 1m path loss values indicate this point.

The relatively small value for the shadowing parameter is mostly due to the fact that our measurements were done in Line of Sight (LOS) conditions. The
Table 2.1: Ranges for power loss exponent and shadowing variance over the measurement band

<table>
<thead>
<tr>
<th>Location</th>
<th>Path Loss Exponent</th>
<th>Shadowing Variance (dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Engineering I</td>
<td>$1.4 &lt; n &lt; 2.2$</td>
<td>$5.7 &lt; \sigma^2 &lt; 13.0$</td>
</tr>
<tr>
<td>Apartment Hallway</td>
<td>$1.9 &lt; n &lt; 2.2$</td>
<td>$3.0 &lt; \sigma^2 &lt; 11.0$</td>
</tr>
<tr>
<td>Parking Structure</td>
<td>$2.7 &lt; n &lt; 3.4$</td>
<td>$2.4 &lt; \sigma^2 &lt; 17.0$</td>
</tr>
<tr>
<td>One-sided Corridor</td>
<td>$1.4 &lt; n &lt; 2.4$</td>
<td>$4.0 &lt; \sigma^2 &lt; 16.0$</td>
</tr>
<tr>
<td>One-sided Patio</td>
<td>$2.8 &lt; n &lt; 3.8$</td>
<td>$1.0 &lt; \sigma^2 &lt; 9.2$</td>
</tr>
<tr>
<td>Concrete Canyon</td>
<td>$2.1 &lt; n &lt; 3.0$</td>
<td>$4.8 &lt; \sigma^2 &lt; 20.0$</td>
</tr>
<tr>
<td>Plant Fence</td>
<td>$4.6 &lt; n &lt; 5.1$</td>
<td>$2.8 &lt; \sigma^2 &lt; 5.0$</td>
</tr>
<tr>
<td>Small Boulders</td>
<td>$3.3 &lt; n &lt; 3.7$</td>
<td>$8.8 &lt; \sigma^2 &lt; 18.2$</td>
</tr>
<tr>
<td>Sandy Flat Beach</td>
<td>$3.8 &lt; n &lt; 4.6$</td>
<td>$2.2 &lt; \sigma^2 &lt; 10.0$</td>
</tr>
<tr>
<td>Dense Bamboo</td>
<td>$4.5 &lt; n &lt; 5.4$</td>
<td>$0.4 &lt; \sigma^2 &lt; 46.0$</td>
</tr>
<tr>
<td>Dry Tall Underbrush</td>
<td>$3.0 &lt; n &lt; 3.9$</td>
<td>$4.2 &lt; \sigma^2 &lt; 16.0$</td>
</tr>
</tbody>
</table>

exception is the dense bamboo growth area, where indeed extreme signal absorption and scattering occurs. The unexpected high shadowing in the concrete canyon is probably due to high levels of reflected energy off the walls. Relatively little shadowing is observed in wide-open areas. The power loss exponent, that has a maximum of 5.4, is comparable with power loss exponents in channels with higher antenna heights.

Channel coherence bandwidth (CBW) was also determined for each snapshot. We define the CBW as the -3dB bandwidth of the magnitude of the complex auto-correlation function of the frequency response of the channel. Our definition of the
Table 2.2: Range of path loss at reference distance over the measurement band

<table>
<thead>
<tr>
<th>Location</th>
<th>Path Loss at 1 m (dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Engineering I</td>
<td>$-50.5 &lt; PL(d_0) &lt; -39.0$</td>
</tr>
<tr>
<td>Apartment Hallway</td>
<td>$-38.2 &lt; PL(d_0) &lt; -35.0$</td>
</tr>
<tr>
<td>Parking Structure</td>
<td>$-36.0 &lt; PL(d_0) &lt; -32.7$</td>
</tr>
<tr>
<td>One-sided Corridor</td>
<td>$-44.2 &lt; PL(d_0) &lt; -33.5$</td>
</tr>
<tr>
<td>One-sided Patio</td>
<td>$-39.0 &lt; PL(d_0) &lt; -34.2$</td>
</tr>
<tr>
<td>Concrete Canyon</td>
<td>$-48.7 &lt; PL(d_0) &lt; -44.0$</td>
</tr>
<tr>
<td>Plant Fence</td>
<td>$-38.2 &lt; PL(d_0) &lt; -34.5$</td>
</tr>
<tr>
<td>Small Boulders</td>
<td>$-41.5 &lt; PL(d_0) &lt; -37.2$</td>
</tr>
<tr>
<td>Sandy Flat Beach</td>
<td>$-40.8 &lt; PL(d_0) &lt; -37.5$</td>
</tr>
<tr>
<td>Dense Bamboo</td>
<td>$-38.2 &lt; PL(d_0) &lt; -35.2$</td>
</tr>
<tr>
<td>Dry Tall Underbrush</td>
<td>$-36.4 &lt; PL(d_0) &lt; -33.2$</td>
</tr>
</tbody>
</table>

complex auto-correlation function follows that of [29]. For each site, the CBW was calculated for all the snapshots at a specific distance, and averaged. The average CBW was then plotted as a function of distance. Based on our observations, it was found that in general, the average CBW tends to decrease with distance between transmitter and receiver. An intuitive explanation for this phenomenon is that, as the separation is increased, a larger portion of the transmitted energy that arrives at the receiver will have been reflected or scattered on its way, and therefore there is higher possibility of destructive interference at some frequencies. This destructive interference results in appearance of nulls in the amplitude of the
channel frequency response, which then contributes to smaller CBW calculated for each snapshot. Needless to say, the specific behavior of channel selectivity is closely related to the geometry of the measurement environment and the physical properties of the reflecting surfaces in the vicinity of the transmitter and receiver antennas. Figure 2.4 shows these results.

Note that CBW does not follow the same trend in hallways. Unlike open areas, in hallways we see a roughly oscillating relationship with increasing distance for average CBW. Hallways provided another interesting phenomenon also. It was found that the power loss exponent in long, enclosed spaces is smaller than those
In general, it was observed that the channel CBW drops with distance, with the exception of hallways. It was observed that in hallways, some type of periodic waveguide effect was present. This is mostly due to the fact that the observations were made under LOS conditions in our experiments, where generally lower values of coherence bandwidth were observed. The path loss exponent is usually close to 4. The shadowing variance values observed in our experiments are generally lower than those observed elsewhere.

2.5 Conclusion

The channel measurement experiments indicate that the path loss exponent for ground-lying antennas, in the 800-1000 MHz band, on average ranges between 2.2 and 2. The lower range belongs to hallways in indoor environments. Outdoors, the path loss exponent is generally closer to 4. The shadowing variance values observed in our experiments are generally lower than those observed elsewhere. This is mostly due to the fact that the observations were made under LOS conditions. In general, it was observed that the channel CBW drops with distance, with the exception of hallways. It can be described as a result of a wave-guide like effect. The same principle may also be responsible for the CBW behavior observed in open spaces.
dependency with distance exists.
Chapter 3

Frequency Hopping and Code Synchronization for Sensor Networks

3.1 Introduction

In this chapter the problem of code synchronization for a very slow frequency hopping multiple access system, such as the one encountered in a wireless sensor network, will be investigated. Unlike other low power and small range radio networks such as Bluetooth, here we have a peer to peer network. There are no local or global master nodes, therefore, each individual point to point link must assign its own code and maintain code synchronization.

First we will give a brief overview of various code synchronization methods in conventional spread spectrum systems. Then issues related to modeling the multiple access interference in a wireless network which uses spread spectrum...
signaling will be discussed. In the remainder of the chapter the mechanism of transmitter aided code acquisition (TACA) will be described and its performance investigated.

3.1.1 Code Acquisition Problem

Code synchronization issues are investigated in depth in part 4 of [30]. The material in this section is a brief summary of some of the topics covered in [30]. For both the DS and FH spread spectrum signals, the code synchronization problem consists of determination of the proper phase of the spreading sequence which spreads the incoming signal.

To synchronize the local code phase with that of the incoming signal, the receiver must search some area of phase uncertainty, which is usually divided into cells, cell by cell. Based on the outcome of the search process, the receiver will then decide whether the correct cell, and hence code phase synchronization, is reached or not. Therefore, the two components needed for code synchronization are the following:

- Search Strategy: a method of progression for moving amongst the cells in the ambiguity region
- Detector Structure: A mechanism for inspection of a single cell to decide whether it corresponds to the correct phase

The various parameters which determine the type of the detector structure are outlined in [30]. The various search strategies may be categorized under parallel, serial, and sequential estimation search classes. Under the parallel search, all the cells in the region of ambiguity are inspected simultaneously. The cell which
has the highest detection decision variable will be chosen as the correct phase cell. This approach is in reality, for the case of moderate to large code lengths, impractical. Therefore the cells must be inspected in a serial fashion.

It is also possible to estimate the internal state of the code generator of the hopping pattern, based on a short period observation of the incoming signal. This method is useful when highly predictable m-sequences are used to generate the code. Once the current state of the code generator mechanism is known, it is possible to generate the exact replica of the code locally, and hence the code synchronization problem is solved [31]. The family of RASE and RARASE [32] code synchronization methods, which use sequential estimation techniques, are examples of this approach.

The most popular and simplest synchronization mechanism which can be designed is a non-coherent, single dwell time, active detector, which uses the serial search strategy. The simple sliding correlator search method [33] is the most popular implementation. A variation of this scheme is given in Figure 3.1 for a frequency hopping system. In this method, the local frequency generator runs at a rate slightly faster or slower than that of the incoming signal. Oftentimes, in order to aid the synchronization task, the transmitter includes a known pattern at the beginning of the transmission. Or, the receiver attempts to determine the synchronized state when a specific segment of the code has been observed. In this case, rather than searching the code phase space actively, the receiver attempts to determine when a specific code segment has been observed, and hence a specific code phase is reached. The matched filter structure is used as a trap to catch the specific pattern when it arrives. The details of a matched filter synchronization scheme having four stages are shown in Figure 3.2.
Figure 3.1: A sliding correlator mechanism for FH spread spectrum.

Figure 3.2: Matched filter code acquisition method.
Finally there exist hybrid code acquisition methods, which combine the serial and matched filter search schemes. For example, banks of parallel matched filters may be used to search for a specific preamble which is transmitted at the beginning of the transmission, or are dispersed throughout the data portion of the transmission. Once a preamble is acquired, a serial search mechanism will kick in to verify and further synchronize the code. Examples are the multi-level search methods of [34] and [35]. At the beginning of each communications burst, the receiver must acquire a short pattern, by means of a matched filter. When this occurs, the receiver will switch to serial search, by using one of the available $C$ correlators, to verify that code acquisition has indeed occurred.

The two-level acquisition method has the drawback that its acquisition preamble is readily observable by eaves-droppers and is thus not secure. It is possible to get around this problem by means of introduction of yet another level of synchronization as described by [35]. In this method, there are two codes. One is the short PN code (SPNC) which acts as a preamble. The actual data is transmitted using a long PN code (LPNC). Information about the phase of the long PN code is transmitted over the short PN code. A bank of matched filters are used to detect acquisition of the preamble. Once this is done, the received signal is demodulated to receive information about the actual phase of the LPNC. This information is then fed to one of the active correlators on-board to verify that indeed code synchronization is achieved with the LPNC.

In summary, serial search methods, are less complex, but are slower. Matched filter methods, are partially parallel search methods, which are able to achieve faster code synchronization, but their cost, particularly for long codes, could be
prohibitive, in terms of required hardware. Finally, there are hybrid synchronization methods which are able to provide relatively fast performance, without the very high cost of long matched filtering.

None of these methods alone are quite suitable for our sensor nodes, since they are either too complex, or require long transmission lengths to acquire.

### 3.1.2 Spread Spectrum for Multiple Access

Spread Spectrum techniques were first used as physical layer signaling techniques. Because of their anti-jam capabilities, they can be used as means of multiple access for wireless networks. As described in chapter 5 of [30], there are two distinct types of multiple access wireless networks which use spread spectrum. They are:

- **Point-To-Point (PTP):** Many independent pairs of spread-spectrum radios which are spatially separated communicate simultaneously.

- **Multipoint-To-Point (MTP):** Many single spread spectrum radios that are distributed in space attempt to communicate with a single and fixed radio.

Examples of the former are many tactical land-mobile radio networks such as [36]. The systems belonging to the latter type are encountered in CDMA systems such as described by [37] and the IS-95 CDMA system. In all cases we would like to take advantage of the anti-jam capability of spread-spectrum techniques to support as many simultaneous transmissions as possible in the limited space/bandwidth available to network.

For these systems, characterizing the self interference generated by the multiple access traffic is of significant importance, since in general, it is the interference
which is the limiting factor in terms of system performance. For the wireless sensor network under consideration here, the multiple access interference has direct impact on the performance of the code synchronization maintenance, as will be described in later sections in this chapter.

A large body of work is dedicated to characterizing multiple access interference for both the MTP and PTP systems. Interference modeling has been studied for packet radio systems, in order to determine probability of packet capture at a given receiver. The packet capture phenomenon in these systems refers to the ability of the receiver to lock onto and successfully receive one of the many simultaneous packets arriving at the receiver.

The focus of our survey is frequency hopping systems which use RS codes either as hopping patterns, or as channel codes. Also systems which use independent i.i.d. hopping patterns are of interest. In order to model the interference accurately, a number of key assumptions about the system to be modeled must be made. To do this the following questions must be answered:

1. Are the packets synchronized?

2. Are the codes hop synchronized?

3. Are the received powers at the receiver(s) fixed or variable?

4. What is the spatial distribution of the nodes?

5. What sort of hopping pattern is used?

6. How is a hit event defined?

7. How are individual symbol hits in a packet defined?
8. Do we tolerate symbol erasures?

9. How do we determine whether a symbol is erased?

10. How is a packet collision defined?

The use of RS codes as hopping patterns for frequency hopping systems was first proposed in [38]. Each node is assigned a transmission hopping pattern, which is one of the codewords of an \((n, k)\) RS code. Each packet is therefore transmitted over \(n\) hops. The hopping frequencies are chosen from a set of \(q\) alphabet symbols (or frequencies), with \(n = q - 1\).

In most cases error-and erasure decoding is used at the receiver to decode the received packet. Given that there are \(s\) erased symbols and \(t\) symbols in error, the codeword will be decoded if \(s + 2t \leq d_1\), where \(d_1 \leq d_{\text{min}}\) is the bounded distance [39] and \(d_{\text{min}}\) is the minimum distance of the code. If \(s + 2t > d_1\) the received word is declared undecodable (or erased).

We define \(P_{wt}\), \(P_{we}\), and \(P_{wc}\) to be the probability of a RS codeword decoding error, erasure, and correct decoding, respectively. We also define \(p_t\) and \(p_e\) to be the code symbol error and erasure probabilities. The objective is to determine \(P_{wt}\) and \(P_{we}\) given the detector structure and interference model in the network. If the code symbol error and erasure events in a codeword are independent and remain fixed over all symbols, then good tight bounds for \(P_{wt}\) and \(P_{we}\) are known [39].

However in many models of FH systems, the symbol error and erasure events are not independent [40]. The reason is that the multiple access interference and other channel degradations, which cause symbol hits and thus lead to errors and erasures, may extend over multiple contiguous symbols. This phenomenon occurs
under fading conditions and in networks with non-synchronous hopping. This effect is pronounced for the packet structures with short lengths and limited or no interleaving. In [40] a procedure for calculation of symbol error probability for a FH system with fixed mean received power and fading and shadowing is proposed. This probability is calculated for deterministic and i.i.d hopping patterns with binary FSK signaling for non-synchronous hopping epochs and packet arrivals.

In [41] total packet error probability is found for the case of non-synchronous packet arrival and hopping. Power levels are fixed, and any time overlap is assumed sufficient to constitute a hit. Time domain analysis is done by enumerating all possible overlap conditions and averaging hit probabilities.

The ideas are extended further in [42]. Here again the packets and the hopping on each packet is non-synchronous with other packets. The level of interference a symbol experiences is different from symbol to symbol in a packet. Time overlap alone is not enough to declare a symbol hit, instead the total received energy will be used to determine whether a hit occurs or not. The hits on code-word symbols are not independent, therefore joint probability distributions for hits on the entire packet must be determined. Here a moment generating function approach is used.

In all these schemes, the unifying approach is that, combinatorial arguments are used to enumerate all the possible hits conditions. Once this is done, the average symbol and word error and erasure probabilities are found by averaging over all hit variations.
3.2 Transmitter Aided Code Acquisition

In our sensor network nodes are distributed randomly and uniformly in the plane with density $\lambda$. The network connection topology is flat; that is, it is a true peer to peer network, with all nodes behaving similarly. The multiple access network is a point to point network, i.e. it is a collection of independently operating links.

Each node transmits and receives packets from neighbors according to its local schedule. A node’s time horizon is broken into contiguous, uniform length periods. Each period is called a SUPER FRAME. The length of a SUPER FRAME is fixed to $T_{frame}$ for all nodes, and is fixed throughout the network. A typical frame structure appears in Figure 3.3. This SUPER FRAME belongs to a node which has five established links, each with a transmit and receiver slot. The SUPER FRAME repeats in time.

We assume the channel assignment for each node is a random process which
leads to random location of transmission and reception slots in the node’s SUPER FRAME. We assume that all nodes have $N_j$ neighbors, therefore $2N_j$ slots are assigned in the SUPER FRAME. We also assume the slot assignment process is identically and independently operating on each node. Different nodes have different SUPER FRAME epochs. A single packet takes up a single slot duration. Packet length, $T_p$ is fixed. There are $N_s$ slots in a SUPER FRAME and therefore $T_{frame} = N_s T_p$.

In the sensor network, each link uses very slow frequency hopping. In this mode, a single packet is sent over a fixed frequency. The hopping pattern in effect controls the carrier frequencies of packets. The hopping pattern on each link is controlled by the transmitter. Each new packet is transmitted on a different carrier frequency.

Each pair of nodes exchange information about the specific pattern and the starting phase they will use during transmissions, when they first find each other and establish a link. The goal of each receiver is then to stay synchronized, for each incoming link, to the hopping pattern of the transmitter for that link. This is also the objective of the TACA scheme. So in a sense, TACA is a phase tracking scheme, rather than an initial code acquisition mechanism.

The traditional code synch mechanisms which were described at the beginning of this chapter are all unsuitable to be used in the sensor network paradigm. The difficulty with them is that packet sizes are too small, and hopping rate is too slow. The short packet length, and the fact that single hops per packet are used, make it impossible to perform code synchronization on a packet by packet basis, as is done in many mobile packet radio systems. It is also not possible to do serial searches on a sequence of packets directly, because that means many packets will
be lost before code synch finishes. Parallel searches are also not possible due to their need for extra hardware, and high levels of complexity.

Unlike the traditional methods where the entire burden of code acquisition and synchronization is carried by the receiver, in the TACA scheme the transmitter aids the receiver in maintaining code synchronization. This is done by inserting a series of special signals in between the sequence of packets, which we call marker words. Included in the marker word is information about the code phase at the time the marker word is received.

Since the phase information is transmitted over the air, it has to be conveyed in a fashion that only the intended users understand it. We want the hopping pattern itself to appear as random as possible, such that an unauthorized receiver, which may have very capable equipment, is unable to predict the phase from the sequence itself. For example, a RARASE type receiver won’t work. This means that the code sequence should be as unpredictable as possible. Truly random sequences have the property that a very long segment of them is needed in order to be able to predict future values based on the history of the sequence. Therefore such random sequences will be good candidates for our hopping patterns.

The remainder of this chapter is organized as follows. First a description of some methods of code generation will be given. Then a detailed description of the TACA will be followed by sections on the performance of TACA. The ability of TACA to maintain code synch in a network environment and also for a single link under partial band jamming will be investigated. The salient points of TACA and insights into the performance of it will be summarized in the conclusion section.
3.3 Hopping Code Generation

In many cases a pseudo-random sequence is used as a hopping pattern. A pseudo-random-sequence generator is a deterministic function that takes a randomly generated seed number of length $k$, and produces a sequence of bits of length $l$, where this new sequence "looks" random [43].

**Definition:** Let $k$ and $l$ be positive integers such that $l \geq k + 1$. Then a $(k, l)$-pseudo-random bit generator is a function:

$$f : (Z_2)^k \rightarrow (Z_2)^l$$

(3.1)

where $(Z_2)^k$ is the space of all binary $k$-tuples. It is difficult to give an exact definition of the "randomness" of a sequence. According to the situation where a random sequence is used, various indicators or properties that are consequences of randomness may be specified. Then one would like to generate a pseudo-random-sequence that exhibits a specific set of those properties. For example, in the case of our spread spectrum system, we would like to have a pseudo-random-sequence which is unpredictable. That is, it mimics the predictability property of true random sequences.

One measure that is a good indicator of the unpredictably of a sequence is the linear complexity of that sequence [44]. The linear complexity of a binary sequence $\{s_n\}$ of length $N$ is the length of the shortest linear feedback shift register (LFSR) that can generate the sequence using its first $A$ digits. The linear complexity profile of a sequence generator is the graph of the sequence’s linear complexity as a function of its length. Massey [45] has given an efficient algorithm for synthesis of such a LFSR. It is a fact that for truly random binary sequences of length $l$ the linear complexity is a random variable which stays close
to $l/2$ [46].

Although there are clearly non-random sequences that have good linear complexity for a specific length, in general families of sequences that have good linear complexity profiles (i.e. have good linear complexity for all lengths) and induce uniform distribution on their alphabet space are considered unpredictable [44].

Three different categories of pseudo-random-sequence generators have been considered. In the following sections the degree of unpredictability, and also the computational cost of running these generators are compared to find a suitable sequence generator for our system.

### 3.3.1 The Blum-Blum-Shub Generator

This is a method of generating random-bits that is based on the problem of distinguishing quadratic residues and non-residues in a finite field. A brief listing of definitions and facts is given in Appendix A. The method of random bit generation is as follows:

Let $N$ be a Blum integer with prime factors $p$ and $q$. Let $QR(N)$ be the set of quadratic residues modulo $N$. A seed $s_0$ is chosen from $QR(N)$. For $i \geq 1$, define

$$s_{i+1} = s_i^2 \mod N \quad (3.2)$$

Then at each iteration the least significant bit of $s_i$ will be a random bit. The sequence of these bits will be a pseudo-random sequence. Note that there are $(p - 1)(q - 1)/4$ distinct quadratic residues. Therefore this sequence will have a period of at most $(p - 1)(q - 1)/4$.

For very large values of $N$ and unknown factors $p$ and $q$, given the sequence
up to state \( i \), it is impossible to predict the next bit in polynomial time, with probability of correctness greater than 0.5 \([43]\). As long as the factorization is unknown, the generated bit sequence will be unpredictable. For this reason, large values of \( N \) must be chosen. This will then result in the generators performing a large number of calculations per iteration to generate a single bit. However it is possible to take more than one bit at each iteration. It has been shown that if the number \( N \) is represented by \( n \) bits, then at each iteration \( \log(n) \) least significant bits will be random.

In this method at each iteration a large number must be squared. Then the modulo operation must be performed to obtain the \( \log(n) \) bits. We need at least a 64 bit operation to get modest sequence lengths. Another disadvantage is the problem of finding and storage of enough of seed values to accommodate generation of large numbers of distinct sequences.

### 3.3.2 Discrete Chaotic Maps

A discrete map is the mathematical model that describes the state space of a dynamical system as a function of time. The following is the general form of a discrete map:

\[
\zeta_{n+1} = \tau(\zeta_n), \quad \zeta_n \in I, \quad n = 0, 1, 2, \ldots
\]  

(3.3)

where \( \zeta_n = \tau^n(\zeta_0) \) and \( I \) is an interval for one dimensional maps. There are a number of different families of these maps that exhibit chaotic behavior in certain regions of their parameters. One such map which is of interest here is the Logistic map, with \( \tau(x) = r x(1-x) \) and \( x \in I = [0, 1] \). For \( r \in [3.57, 4] \) this map exhibits chaos \([47]\).
An orbit is defined as the sequence \( \{ \zeta_n \}_{n=0}^{\infty} \). Note that this orbit is a sequence of real valued numbers. Although this sequence is generated by means of a deterministic rule, it will behave in a random manner in the chaotic regions [48]. A fairly straightforward method has been proposed for generating pseudo-random bit sequences from these real valued orbits [49]. It works as follows: take \( \zeta_0 \in [0, 1] \) at random. Using the Logistic map, with the given \( r \) value, generate an orbit. At each iteration the corresponding random bit \( z_n \) is obtained as follows:

\[
    z_n = \begin{cases} 
        1, & \zeta_n \geq 0.5 \\
        0, & \zeta_n < 0.5 
    \end{cases} \tag{3.4}
\]

Analysis done in [49] indicates that the sequence of bits generated in this manner possesses very good random properties. To generate a bit sequence of period \( N \), one only needs to generate the orbit up to its \( N^{th} \) iteration.

### 3.3.3 Feedback Shift Registers

A shift register structure with feedback is depicted in Figure 3.4.

![Figure 3.4: Shift register structure with feedback.](image)

\[
    f(x_0, x_1, \ldots, x_{n-1}) 
\]
Each stage $x_i$ is a storage element containing an $M$-ary value. At each iteration the function $f$ generates a new output. When the elements are binary values and the function $f$ can be described as

$$f(x_0, x_1, \cdots, x_{n-1}) = c_0x_0 \oplus c_1x_1 \oplus \cdots \oplus c_{n-1}x_{n-1}$$

(3.5)

where each $c_i$ is a binary value and summation is modulo 2, then the structure is called a binary Linear Feedback Shift Register (LFSR). The theory governing the behavior of these structures is well known [50]. Although these structures are simple to implement, as random bit generators they possess poor linear complexity. That is, they generate highly predictable bit sequences. Introduction of non-linear functions, or combination of more than one shift register are some known methods for increasing the linear complexity without increasing the length of the registers. However in most cases, the hardware cost is not acceptable. Also, sequences with long periods may not result.

### 3.3.4 Comparison of Sequence Generators

The three generators we have considered so far may be categorized from complex to simple, in terms of their implementation, and unpredictable to predictable. The linear complexity profile of these three schemes is provided in Figure 3.5. The BBS generator is provably the most unpredictable of the three. Note that for the chaotic sequence we have only the evidence of statistical tests. The LFSR and the various versions of it are the most predictable methods. On the other hand, when implementation is of concern, both BBS and chaotic bit generators require arithmetic processing for each iteration, while the LFSR can be implemented directly in hardware. The discrete chaotic map is able to provide random behavior.
Figure 3.5: Linear complexity profile of three different pseudo-random bit generators.

using 32 bit operations, while the BBS needs at least double precision. The given sequence for BBS has only length 950. To obtain sequences with longer period numbers which need more than 64 bits must be used. Therefore it appears that the chaotic map would be an acceptable choice, because it has relative ease of implementation and good random behavior.

3.4 Description of TACA

Ideally we would like to have a distinct code for each transmission link. That is if node $n_i$ maintains links with $N_n$ different immediate neighbors, then it would have that many different hopping patterns. In the case of using a chaotic map as a pattern generator, this would mean using $N_n$ different seeds. In this manner, each receiver node which receives packets from $n_i$ may only depend on its dedicated
stream of packets for code synchronization. The transmitter must also then provide $N_n$ different marker words. This can quickly lead to congestion, especially as the number of nodes in the network increases.

So instead, we assume each transmitter uses one hopping pattern for all its transmissions. Once the receiver nodes of $n_i$ know the total number of transmissions of $n_i$ in a SUPER FRAME, then a single marker word transmission per SUPER FRAME will be sufficient to convey the same level of phase timing information as before. Then it is up to it to inform its recipients of any changes in the number of transmissions per frame, in a timely manner. If each receiver is also informed of all the time epochs when $n_i$ transmits, then it will be able to perform faster serial searches on the hopping pattern, i.e. use transmissions intended for other nodes to search for the correct phase. Note that this extra exchange of information is cost free, since it must be done to establish the link in the first place. This also will reduce energy consumption at the transmitter.

We model the process of phase generation as a finite state machine (FSM). There is a one-to-one relationship between the states of the FSM and code phase. So when the hopping pattern is in phase location $S_n$ the corresponding FSM state is $S_n$. For a long code, the total number of states of the FSM is large.

When a node $n_i$ forms a link with another node for the first time, it will initiate its FSM to some randomly chosen state. It will also inform the other node of this initial phase. Then each time this node transmits a packet, it will change its internal state from current $S_m$ to $S_{m+1}$ with $S_{m+1} = S_m + a$, and $a$ some positive integer. When other nodes form links with $n_i$ at later times, they are informed of the internal state of $n_i$’s FSM at that time and of the method which governs state transitions for it, i.e. the value of $a$. The objective of the
code maintenance scheme is to enable the receiver nodes to estimate correctly the internal state of \( n_i \)'s FSM at the time when they are due to receive a packet from \( n_i \).

Given that node \( n_i \) is currently in its \( k^{th} \) SUPER FRAME, it will encode the value of \( S_m \) it will have at the time it transmits its first packet in the \( k+1^{st} \) SUPER FRAME. It will use an \((n, k)\) Reed Solomon code to encode this information. It will then send this codeword as the marker word during the current SUPER FRAME.

There are \( N_T \) tones set aside throughout the entire network for marker word coding, with \( N_T \leq q \), where \( q = n + 1 \) is the RS code alphabet size. When a reduced alphabet size is used, then the single marker word will be extended to have a length \( L = \omega n \), where \( \omega = \lceil \log_2(q)/\log_2(N_T) \rceil \). The transmitter sends each of the \( L \) tones, or channel symbols, of the marker word at randomly chosen time \( t_l \), \( l = 1, 2, \ldots, L \) during its frame. The only restriction made on marker symbol times is that they are chosen to not collide with transmission and reception slots of interested nodes. The diagram of Figure 3.3 illustrates this concept.

### 3.5 Analysis of TACA

The goal of the TACA method is to maintain code synchronization. So the metric of interest is the length of time it takes to lose code synchronism. However, to determine this, the conditions of loss of code phase lock must be defined explicitly. Once this is in place, then we may proceed to characterize time to lose lock.

Before defining the lock loss event, however, we will give background information about the general detection structures for our system. Namely the packet
capture mechanism, and marker symbol detection mechanisms.

3.5.1 Packet Capture Mechanism

The code synchronization mechanism is concerned only with the ability to determine the correct carrier frequency of the packets. Although it is possible for a packet whose carrier frequency is estimated correctly be dropped, due to collisions with other packets and/or jamming, the code synchronization system views that packet as correctly captured. In our context, we define a captured packet as a packet whose carrier frequency is estimated correctly at the receiver, regardless of the reliability of its contents.

Each packet is comprised of two sections, a preamble and a body, as shown in Figure 3.6. The receiver uses the preamble to perform frequency and symbol synchronization. Given that the receiving node is tuned to the proper frequency, its ability to actually capture the frequency of the incoming packet depends on the signal to interference ratio seen during the reception of the preamble.

![Packet structure](image)

Figure 3.6: Packet structure.

The difficulty in determining this ratio is the non-stationary nature of the
interference in the PTP network. In our model, packet transmission times are not synchronized with each other. Therefore the actual interference levels may vary with time. The capture model we use here is based on the total received interfering energy. We define a packet’s frequency to be captured when the total received interfering energy incident on the receiver’s input \((E_I)\) is less than a fraction \(\theta\) of the desired packet’s preamble energy \(E_s\). Interference includes the sum of additive noise, jamming, and multiple access interference elements.

Throughout the remainder of this chapter, we assume that the probability of packet capture events are i.i.d. for all packets and denote it by \(P_c\). The packet length is \(T_p\) and fixed and preamble length is \(\tau_p\).

### 3.5.2 Marker Word Error and Erasure Events

The receiver has a single energy detector, which has a tunable carrier frequency. To determine the actual tone which was sent during one channel symbol interval of length \(\tau_m\), the receiver will tune its frequency to all \(N_T\) tones serially and measure the received energy for duration of dwell interval \(\tau_d\). Figure 3.7.b illustrates this idea. During each dwell interval the receiver acts as an independent energy detecting branch. The output of the \(i^{th}\) interval is \(m_i\). Using Viterbi’s ratio threshold test (RTT) [51] on the set of \(m_i\)’s the receiver decides on the condition of the given marker tone, i.e. whether the tone is detected or erased. The mechanisms which may lead to making a decision error on a single tone are shown in Figure 3.7.a.

For an \((n, k)\) linear \(q-ary\) code, with independent error and erasures on code symbols and with errors-and-erasures decoding [39], the probability of codeword decoding error, \(P_{wts}\), codeword erasure, \(P_{we}\), and correct decoding, \(P_{wc}\) are derived
Interfering Tone $f_i$

Tagged Marker Tone $f_1$

Interfering Tone $f_2$

Interfering Tone $f_3$

Energy Detector

Branch energy

Input

$e^{-j2\pi f_i}$

a) Marker tone interference

b) Branch metric calculation for a single marker symbol

Figure 3.7: Detection process for a single marker tone.
in [52]. They are given below for the case of a RS code with $q = n + 1$:

$$P_{wc} = \sum_{j=0}^{d} \sum_{i=0}^{n-j} a_{ij} P_{ji}$$  \hfill (3.6)

$$P_{we} = \sum_{j=0}^{n} \sum_{i=0}^{n-j} F_{ji} P_{ji}$$  \hfill (3.7)

$$P_{wt} = 1 - P_{wc} - P_{we}$$  \hfill (3.8)

with:

$$T_{ji} = \binom{n}{j} \binom{n-j}{i} (n)^{j}$$  \hfill (3.9)

and

$$F_{ji} = T_{ji} - a_{ji}$$  \hfill (3.10)

If code symbol errors are i.i.d as well as erasure events, and given that code symbol error and erasure probabilities are $P_{st}$ and $P_{se}$ respectively, then the expression for [52]'s $P_{ji}$ becomes:

$$P_{ji} = \left( \frac{P_{st}}{n} \right)^{j} (P_{se})^{i} (1 - P_{st} - P_{st})^{n-j-i}$$  \hfill (3.11)

The value of $a_{ji} = T_{ji}$ for $2j + i \leq d$, and zero for $i > d$. For the case where $2j + i > d$ and $i \leq d$, we have:

$$a_{ji} = \sum_{m=0}^{d-2j} \sum_{i_1=0}^{i} \sum_{i_2=0}^{i-1-m} \sum_{i_3=0}^{i_2} A_{j+m} \binom{n-j-m}{i-i_1} \binom{j+m}{i_1} \binom{j+m-i_1}{i_2} \binom{j+m-i_1-i_2}{i_3} (n-1)^{i_3}$$  \hfill (3.12)
where $d_1$ is an integer with $d_1 < d_{\text{min}}$, and $(x)^+ = \max(0, x)$.

From a practical point of view, it is desirable to have a marker alphabet size that is as small as possible, because this reduces the burden of marker symbol detection at the receiving node. After all, given a received signal and limited observation time, it is easier to decide between two possible hypotheses than four hypotheses, for example. On the other hand, to generate an $(n,k)$ codeword, using an alphabet size which is smaller than $q = n + 1$ requires more channel uses.

For a reduced alphabet size which requires $\omega$ channel symbols to represent a single code symbol, the code symbol error and erasure probabilities, given that code symbol error and erasure events are independent from symbol to symbol, are related to the channel symbol error and erasure probabilities as given below:

$$
P_{se} = \sum_{i=1}^{\omega} \sum_{j=0}^{\omega-i} \binom{\omega}{i} \binom{\omega-i}{j} p_e^i p_t^j p_c^{\omega-i-j}$$

(3.13)

$$
P_{sc} = p_c^\omega$$

(3.14)

$$
P_{st} = 1 - P_{se} - P_{sc}$$

(3.15)

Where $p_e$, $p_t$, and $p_c$ are raw channel symbol event probabilities.

The raw channel symbol event probabilities, are functions of the detector structure, the value of RTT ratio, $\gamma$, and the interference levels, which in turn are functions of node density, transmit powers, and the channel access mechanism. These are factors which are not easily quantified in a single frame-work. For example, no exact closed from expressions for error and erasure rates for systems using more than two tones and multiple interfering packets under FSK exist.
Therefore we will use simulation to empirically estimate values of $p_c$, $p_t$, and $p_e$. Then using the expressions given above marker word error, erasure, and correct decoding probabilities may be found.

### 3.5.3 Lock Loss Event

A search lock strategy is the collection of logical steps that control the operation of the code synchronizer. Particularly the definition of the conditions, which lead to declaration of a loss of code phase lock, is very important in the overall performance of the code maintenance procedure. For the TACA the diagram of Figure 3.8 give the details of our Loss of Lock (LL) condition.

---

**Figure 3.8**: Search-Lock strategy for TACA.
Let the transmitting node be $n_t$ and receiver $n_r$. During the $k^{th}$ frame $n_r$ was able to determine correctly the carrier frequency of the incoming packet from $n_t$. The packet’s frequency will not be captured during frame $k + 1$ with probability $1 - P_c$. When this happens, node $n_r$ will listen, during frame $k + 2$ for $n_t$’s marker tones. At the end of frame $k + 2$ one of the following cases will be true:

- $n_r$ was able to capture the packet from $n_t$ based on previous estimate of hopping pattern’s phase. In this case the marker information is disregarded.

- $n_r$ was not able to capture the packet from $n_t$, and received a marker word which was erased, with probability $P_{we}$. Node $n_r$ will wait until frame $k + 3$ when it will attempt to capture $n_t$’s packet based on the old phase estimate. If not successful, then $n_r$ will declare a LL condition.

- Node $n_r$ was not able to capture packet, and the marker word was not erased.
  - This word is decoded to a wrong code word with probability $P_{wt}$. In frame $k + 3$, when $n_r$ attempts to receive a packet based on the erroneous marker information, it will fail. At this point $n_r$ will declare a LL condition.
  - The marker word is decoded to a correct code word with probability $1 - P_{wt} - P_{we}$. Then during frame $k + 3$ the receiver node will have a correct estimate of the phase. This correct phase will lead to a successful packet capture with probability $P_c$. Otherwise, the packet frequency will not be captured, and an LL will be declared with probability $1 - P_c$. 

50
The TACA search lock strategy may be modeled as a discrete Markov chain as shown in Figure 3.9. The absorbing state is the LL state. The transition probabilities on each branch are taken from Figure 3.8 and each transition takes one frame duration. $P_{\text{Markov}}$ is the transition matrix of this chain, given below:

$$
\begin{bmatrix}
1 & 0 & 0 & 0 & 0 & 0 \\
0 & P_c & 1 - P_c & 0 & 0 & 0 \\
0 & P_c & 0 & (1 - P_c)P_{\text{we}} & (1 - P_c)P_{\text{wt}} & (1 - P_c)(1 - P_{\text{wt}} - P_{\text{we}}) \\
1 - P_c & P_c & 0 & 0 & 0 & 0 \\
1 & 0 & 0 & 0 & 0 & 0 \\
1 - P_c & P_c & 0 & 0 & 0 & 0
\end{bmatrix}
$$

(3.16)

Figure 3.9: Markov chain model of TACA.

We define time to lose lock ($T_{LL}$) as the time it takes to move from state $S$ to $L$ in our Markov chain. Following the analysis method of [53] we are able to determine the mean of $T_{LL}$ as follows:

$$
T_{LL} = 1 - \frac{-P_c^3 + P_{\text{wt}}P_c^3 - 2P_{\text{wt}}P_c^2 + 3P_c^2 - 3P_c + P_{\text{wt}}P_c + 1}{1 - P_c^2 + P_{\text{wt}}P_c^2 + 2P_c - P_{\text{wt}}P_c - 1} + \frac{1}{-P_c + P_{\text{wt}}P_c + 1}
$$

(3.17)

The mean time to lose lock is depicted in Figure 3.10. This curve gives the mean number of SUPER FRAMES it takes to lose lock after a link is established.
Figure 3.10: Comparison of TACA and non-TACA mean time to lose lock

For purposes of comparison the mean time to lose lock for another search lock scenario which we call non-TACA is also shown in this figure. In the non-TACA scheme, no attempt to maintain code-synch is made. That is if a node is unable to capture the frequency of an incoming packet for two consecutive frames, a lock loss is declared. Using similar analysis methods, the mean time to lose lock for non-TACA is found to be

\[ T_{LL}' = \frac{1}{1 - 2P_c + P_c^2} + \frac{1}{1 - P_c} \]  

(3.18)

We would like to know, in practical terms, at what regions of this surface will a typical sensor network operate? That is what are some typical values for \( P_c \) and \( P_{wt} \).
3.5.4 Partial-band Jamming Performance

In this mode, we investigate the ability of a single link to withstand hostile and intentional jamming in the form of partial band jamming. We assume the network is comprised of a single transmitter and a single receiver. The entire hopping band, $W$, is jammed by a white noise source having power spectral density $J_0$.

Under partial band jamming, the jammer will only cover a portion $\rho$ of the entire bandwidth. The jammed frequencies will then see a noise power density of $J_n = J_0/\rho$ with probability $\rho$. We assume jamming power is the only type of noise present. The aim is to determine the probabilities of packet capture $P_c$ and marker word error $P_{wt}$ in this environment.

Packet Capture

As before, a packet’s preamble is deemed captured, when the interfering energy input to the receiver over the preamble interval, $\tau_p$, is less than a fraction $\theta$ of the received signal’s energy. The probability of this occurring conditioned on the values of $r_0$ and $f_0$ is

$$P_{pp} = \text{Prob}(J_n \tau_p B < \frac{P_t \theta C(f_0) \tau_p}{r_0^4})$$

(3.19)

where $B$ is the detection bandwidth, $C(f_0) = (\frac{e}{3\pi f_0})^2$ the propagation factor at frequency $f_0$, and $r_0$ the distance between transmitter and receiver.

Given that $r_0$ has distribution density $f_{r_0}(x) = \frac{2x}{R_{\text{max}}^2}$ for $x \in [0,R_{\text{max}}]$, after averaging over $r_0$, and conditioned on the value of $f_0$, and assuming that the
frequency and distances are independent, we have:

\[
P_{pp} = \int_0^4 \frac{\rho B J_n}{8J_n} \frac{2x}{R_{max}} \, dx
\]

\[
= \frac{1}{R_{max}^2} \left( \frac{c}{4\pi} \right) \frac{1}{f_0} \sqrt{\frac{P_l \theta}{BJ_n}}
\]

Assuming all carrier frequencies in the band are uniformly distributed and equally likely to be chosen, then if \( Q \) such frequencies exist, we will have:

\[
P_{pp} = \frac{1}{R_{max}^2} \left( \frac{c}{4\pi} \right) \frac{1}{f_0} \sqrt{\frac{P_l \theta}{BJ_n}} \left( \frac{1}{Q} \sum_{i=1}^Q \frac{1}{f_i} \right)
\]

The probability of packet capture is then given by \( P_c = (1 - \rho) + \rho P_{pp} \). This probability as a function of \( \rho \) and \( J_0 \) is given in Figure 3.11.

\[
\]

Figure 3.11: Dependence of packet capture probability on jamming parameters.

It can be seen from Figure 3.11 that the effect of the second term on \( P_c \) is negligible, and \( P_c \approx 1 - \rho \).
Marker Tone Interference

Although from the diagram of Figure 3.10 it is clear that $P_{wt}$ does not affect the mean time to lose lock significantly, we will outline a method for determining $P_{wt}$ for purposes of completeness.

The received signal energy is $E_s$ at a distance of $r_0$ between the transmitter and receiver. We can write $E_s = \frac{P_t C(f_0) r_0^2}{r_0^4}$. But for now we will leave it as $E_s$. Also each branch output is the normalized metric

$$m_i = \frac{\text{branch energy}}{4E_s/J_n} \quad (3.22)$$

If a tone and jamming noise are both present at the input to a branch, the output is distributed as a non-central chi-square random variable, and when there is only noise, the output is centralized chi-square distributed [30]. If a branch is not jammed, its output is zero, in absence of signal tone. The only noise present is the jamming noise, with characteristics as described above. Viterbi’s threshold ratio test is used to determine whether a tone is correctly detected, in error, or erased, as before. The threshold is represented by $\gamma$. Without loss of generality, we assume the tone with index one is transmitted. Wanted are the tone error, $p_t$, and erasure, $p_e$, probabilities.

When both branches $i$ and 1 are jammed, we define $P_s(\gamma)$ as:

$$P_s(\gamma) = \text{Prob.}(m_i > \gamma m_1)$$

$$= 1 - \text{Prob.}(m_i \leq \gamma m_1)$$

$$= \int_0^\infty \left( \int_0^{\gamma y} e^{-x} dx \right) e^{-\alpha} e^{-y} I_0(2\sqrt{y\alpha}) dy$$

$$= \frac{1}{1 + \frac{\gamma}{\alpha}} e^{-\alpha} I_1(\gamma)$$

$$= \frac{1}{1 + \frac{\gamma}{\alpha}} e^{-\alpha} \frac{e^{-y}}{y \alpha}$$

$$= \frac{1}{1 + \frac{\gamma}{\alpha}} e^{-\alpha} \frac{e^{-y}}{y \alpha}$$
With \( \alpha = \frac{E_s}{\sigma_0} \), we define \( P_n(\gamma) \) as:

\[
P_n(\gamma) = \text{Prob.}(m_i \geq \gamma m_1) \quad i \neq 1
\]

\[
= \int_{\frac{E_s}{4\gamma m_1}}^{\infty} e^{-x} \, dx
\]

\[
= e^{-\frac{E_s}{4\gamma m_1}}
\]  

(3.24)

The condition for \( P_n(\gamma) \) occurs when the transmitted tone is not jammed, but the \( i^{th} \) branch which does not contain the tone is jammed.

To fully determine \( p_t \) and \( p_c \) all the possible combinations of tone jamming and not jamming, for \( N_T \) tones must be enumerated, and then total probabilities may be found. For the case of \( N_T = 4 \), the channel symbol error rate, \( p_t \) may be written as:

\[
p_t = 3\rho^4 P_s\left(\frac{1}{\gamma}\right)\left(\frac{\gamma}{\gamma + 1}\right)^2 + 6\rho^3(1 - \rho)P_s\left(\frac{1}{\gamma}\right)\left(\frac{\gamma}{\gamma + 1}\right)
\]

\[
+ 3\rho(1 - \rho)^2 P_s\left(\frac{1}{\gamma}\right) + 3\rho^2(1 - \rho)P_n\left(\frac{1}{\gamma}\right)\left(\frac{\gamma}{\gamma + 1}\right)^2
\]

\[
+ 6\rho(1 - \rho)^2 P_n\left(\frac{1}{\gamma}\right)\left(\frac{\gamma}{\gamma + 1}\right) + 3\rho(1 - \rho)^3 P_n\left(\frac{1}{\gamma}\right)
\]  

(3.25)

Probability of correct channel symbol detection is:

\[
p_c = \rho^4 (1 - P_s(\gamma))^3 + 3\rho^3(1 - \rho)(1 - P_s(\gamma))^2 + 3\rho^2(1 - \rho)^2(1 - P_s(\gamma))
\]

\[
+ \rho(1 - \rho)^3 + \rho^3(1 - \rho)(1 - P_n(\gamma))^3 + 3\rho^2(1 - \rho)^2(1 - P_n(\gamma))^2
\]

\[
+ \rho(1 - \rho)^3(1 - P_n(\gamma)) + (1 - \rho)^4
\]  

(3.26)

Once these values are known, marker symbol error, erasure, and correct decision probabilities are found, and then marker word error probability is found using 3.6, 3.7, and 3.8. The marker word error probability thus found will have a form such as \( P_{wt}(\rho, J_0/f_0) \) and will be a function of \( \rho \) and \( J_0 \) after the values of \( P_t \) and \( \gamma \) are fixed. This probability is however, still conditioned on the values of marker tone frequency \( f_0 \), which we assume are uniformly distributed over \( N_T \).
tones. It will also be conditioned on transmitter-receiver distance \( r_0 \). To remove these conditional dependence we must perform the following:

\[
P_{wt} = \int_0^{R_{\text{max}}} \left( \sum_{i=1}^{N_T} \frac{1}{N_T} P_{wt}(\rho, J_0/x, f_i) \right) \frac{2x}{R_{\text{max}}^2} dx
\]  

(3.27)

### 3.6 Simulation of TACA

In order to determine TACA’s performance under self-interference, the behavior of the network must be simulated in order to determine packet capture probabilities, \( P_c \), and marker word error probability \( P_{wt} \).

#### 3.6.1 Calculation of \( P_c \)

The location of a single transmit or receive slot in a node’s SUPER FRAME is highly dependent on that of other slots. We have \( N_j \) packets assigned for a single node in a frame. We have the restriction that packets may not overlap in time with each other, and that they must be separated from each other according to some minimum interval which we call a guard interval \( \Delta \). Then given that the first slot’s location is chosen uniformly in the frame, the locations of consequent slots will be dependent on the location of slots which came before.

For this reason, to model the assigned slots of a single node, we must model the entire frame for that node. Our simulation model follows a topology setup according to that given in Figure 3.12.

In each simulation run, for a tagged receiver node, the total number of potential interfering nodes, \( J \), which may lie in the disk of radius \( R_{\text{inter}} \) centered at the location of the tagged node is determined. For each interfering node, a sequence of transmitting slots (i.e. a transmission schedule) is determined independently.
For the tagged node, using the same mechanism, a sequence of packet preambles is generated. These are the preambles of the packets which are expected to arrive at the tagged node from its established neighbors which reside inside the disk of radius $R_{\text{max}}$ around the receiver. We call these preambles the tagged preambles, since they belong to the good packets. Once the timing of interfering and tagged packets are known, each packet will be assigned a random frequency chosen uniformly from the pool of $Q$ carriers. For each tagged preamble, the total interfering energy incident at the receiver, plus additive white gaussian noise is measured for the duration of the preamble. If the interference is larger than a fraction $\theta$ of the energy of the tagged preamble, the packet is declared lost. Otherwise, it is captured. Figure 3.13 gives the simulated packet capture probabilities for two values of node density. For these curves we have $P_t = 1\text{mW}$, $R_{\text{max}} = 10\text{m}$, $R_{\text{inter}} = 20\text{m}$, $T_{\text{frame}}/T_p = 160$, $\tau_p = T_p/14$, $\theta = 0.1$. It is clear that as the traffic
or node density is increased, packet capture probability declines. For $\lambda = 0.04$, the slight increase in packet capture probability is anomalous, and is related to an implementation detail of the simulator.

### 3.6.2 Calculation of $P_{wt}$

The simulation setup for calculation of marker word error probabilities is slightly different from that of the packet capture model. Because the marker tones are very narrow, we may model them as being independently located in the SUPER FRAME, for a single node. See Appendix B for details. If we represent a marker tone’s starting time location in a frame by $b_l$ with $l = 1, 2, \cdots, L$, and $L = \omega n$, then the joint distribution function of $b_l$s is

$$
\varphi(b_1, b_2, \cdots, b_L) \approx (f(b_1))^L
$$

(3.28)
where \( f(b_1) = \frac{1}{T_{frame}} \). Each node chooses its marker tone locations independently of other nodes, and at random. We define a time hit to occur when another node’s marker tone has a non-zero time overlap with a marker at a tagged node. So it is possible to simulate the time and frequency hit events of a single tone, as opposed to the entire frame, as was done with the packets. This leads to significant savings in simulation time and complexity. We assume the marker tone frequency is chosen uniformly from the \( N_T \) possible choices. It is also assumed that tone frequencies of a single word are chosen independently. This assumption may not be true, but since for RS codes, alphabet repetition statistics are not known (only code weight distribution is known [39]), then this assumption is as good as any other assumption at this point.

Therefore it suffices to simulate the time and frequency hits for a single tone, and generate error and erasure statistics based on those events. The diagram of Figure 3.12 describes the simulation model. The tagged receiver and transmitter pair are a distance \( r_0 \) from each other. This distance is a random variable which is distributed according to \( f_{r_0}(x) = \frac{2x}{R_{max}} \), for \( x \in (0, R_{max}] \). The tagged tone frequency, \( f_0 \) is chosen at random from the set \( \{f_1, \ldots , f_{N_T}\} \). The number of interferers within \( R_{inter} \) radius of a tagged receiver node is found as \( K = \lfloor \lambda \pi R_{inter}^2 - 2 \rfloor \), where \( \lambda \) is the node density, and the tagged transmitter and receiver are not counted as interfering nodes.

Since the duty cycle of marker tones in the frame is \( L \tau_m/T_{frame} \), then the probability that an interfering node has a time overlap with the single tagged tone interval is \( \phi_c = 2L \tau_m/T_{frame} \). The probability of having a time and frequency collision is then \( \phi_{cc} = \phi_c/N_T \). The total number of nodes which will hit the tagged tone, \( J \), are chosen according to \( P_J = \binom{K}{J} \phi_{cc}^J (1 - \phi_{cc})^{K-J} \).
Once the value of $J$ is known, random node distances (and therefore random received power levels) are determined. The channel is modeled as a $4^{th}$ power lossy channel.

The node density, $\lambda$, marker word length, $L$, transmit power level $P_t$ and the propagation model, are the factors which affect the tone symbol error, erasure, and correct decoding probabilities.

We have seen that the marker word error probability, $P_{w}t$, affects the overall time until lock is lost. Values of $P_{w}t$ for different conditions are given in Figure 3.14. As can be seen, as the node density, $\lambda$, increases the marker word error probability is generally increased. Also, at the lower node density, the alphabet size has a more pronounced effect on the overall marker word error probability. At lower levels of node density we are able to observe the effect of reducing the dwell interval duration on the marker word performance. As the number of tones is increased, and while a symbol duration is kept constant, probability of error for a single symbol is increased, and that is why codeword error probability is increased as tone count is increased. At higher node densities, the marker symbol errors rise as a result of higher interference levels, and for that reason, alphabet size does not affect the marker word error rates as much.

Using the simulated values of $P_c$ and $P_{w}t$, we are able to determine estimates of the mean time to lose lock, $T_{LL}$, for the TACA scheme. Results are presented for $\lambda = 0.04$ and 0.025, and alphabet sizes of $N_T = 2, 4, 16$. In each condition, the value of $T_{LL}$ is determined for various traffic loads. This is modeled as the number of assigned slots in each SUPER FRAME for the nodes. For simplicity we have kept the number of slots fixed for all nodes. Figure 3.15 gives these results for TACA case.
We see that as the interference levels increase $T_{LL}$ is decreased. This may occur either as the node density is increased, i.e. $\lambda$ becomes larger, or as the traffic level is increased, i.e. $N_j$ increases. This suggests that the network must be kept as sparse as possible, i.e. power control on links must be used.

### 3.7 Conclusion and Future Work

We have seen that, although the scheme is able to handle a network environment well, it is susceptible to intentional partial band jamming. This is expected because the scheme is designed to enable a very large network of nodes to work together, and it was not optimized for operation under jamming.

The packet capture probability is the important factor in the robustness of
Figure 3.15: Mean time to lose lock under TACA.

TACA. To make it impervious to hostile jamming, better packet capture mechanisms must be used. One obvious, but non-trivial approach is the move to higher hopping rates. The higher rate will afford better diversity benefits to the packet capture mechanism. For example, the entire packet preamble may be repeated over two distinct frequencies. Or perhaps the preamble may be transmitted with higher power levels. However faster hopping rates require higher energy and more sophisticated radios and will take us into a higher energy scale.

The key design issue here is that, because we have a very slow hopping frequency hopping system, and because our data rates are low, there is usually a lot of time to search a given cell (candidate hopping pattern phase, which is really a single carrier frequency). By the same token, search rates are very slow, and instead of losing multiple symbols while searching, we are prone to losing multiple packets while searching. Therefore, our search strategy must reflect this. As a
result, our philosophy is to avoid search situations as much as possible, which leads to spending effort in keeping synch, rather than acquiring it when it is lost.

If we were to employ a number of parallel receiver front ends (frequency synthesizers and multipliers), then instead of using TACA, one would use the following scheme. Each time a lock loss event is declared, where the lock loss is defined according to some criterion, for example when two consecutive packet are lost due to their frequency not being captured, then all the parallel receivers would tune their frequencies to one of the frequencies within the region of ambiguity which is created, due to the lock loss event. Then a maximum likelihood criterion could be used to choose the decision of one of the branches as the proper frequency. Compared to TACA, this multiple receiver approach has the high cost of redundant hardware, and possibly higher energy consumption. The advantage is the ability to reacquire the hopping code phase quickly, and possibly over the course of a single packet preamble, and no marker word would be needed. In this method, rather than maintaining the code phase, we reacquire when code synch is lost. Using multiple receivers could prove useful, in combatting intentional jamming as well. Performing a maximum likelihood estimation on the frequency of the incoming packet everytime a packet is expected to arrive, could improve the probability of packet capturei, in situations with low signal to interference levels.

Similarly, if we were to use a straightforward serial search to reacquire the lost hopping phase, we could increase the length of the preamble on all packets, proportional to the average time needed to search the region of ambiguity resulting from the phase loss. In this manner, each transmitting node would have to augment all its packet lengths by some amount, which could lead to higher
energy costs. However, in a noise environment, where there is a high probability of packet loss at all times, this may also prove useful. As future work, this method may be compared to TACA, in detailed simulation or analysis, to determine energy consumption tradeoff and robustness under different types of interference.

It is also possible to incorporate time hopping into TACA as follows. We may group the marker tones together, to build a monolithic marker word. The transmitter node may then move the transmission epoch of this marker word around, in different SUPER FRAMES, to avoid interference.

Future work in this direction may also include determination of the robustness of all the above mentioned schemes when using imperfect clocks and oscillators. Also the extent of energy savings of the schemes must be measured under realistic conditions. These studies will be highly dependent on the hardware implementation.
Chapter 4

Self Organization Background

4.1 Fundamentals of Medium Access Control

The Medium Access problem arises when many users need to share a single transmission medium concurrently, as shown in Figure 4.1. Two major approaches may be adopted. In one method the nodes will use the medium at random, without any explicit coordination with others. In the second approach the nodes decide to establish a form of organization amongst themselves, and then follow a schedule, in time or frequency or both, to access the channel.

4.1.1 Random Access Schemes

In random access schemes there is no order imposed on the times nodes attempt to use the channel. When a node has a packet to send, it will send it. This packet may collide with another packet at the intended receiver. This idea is the basis of the ALOHA [54] scheme. There are refinements possible to this scheme. The transmitting node may first listen to the channel, and send a packet only if
it is not being used. This leads to the Carrier Sense Multiple Access (CSMA) scheme. This will greatly reduce the probability of collisions between packets. In wired media, all the nodes which are attached to the channel are able to detect channel activity, regardless of their physical location. In wireless systems, due to limited range of radios, and other transmission methods, some nodes may become hidden from others. In order to have a successful packet transmission collisions must be avoided at the intended receiver. The CSMA method the other hand, is only able to determine channel activity at the vicinity of the transmitter. This leads to the *Hidden Terminal* problem, illustrated in Figure 4.2. For example, if node A intends to transmit to node B, it will not be able to determine activities
of node C, which will have an effect on node B’s receptions. To get around this,

![Diagram of hidden terminal problem]

Figure 4.2: Hidden terminal problem

the intended receiver, in this case node B, must transmit a busy tone to indicate existence of activity in its vicinity. The MACAW algorithm which uses four messages for each packet transmission addresses this problem [55]. The protocol uses a Request To Send, RTS, message to initiate transmission. If the receiver is free, it will send a Clear To Send, CTS, message. The transmitter will transmit its DATA, along with a short Data Sending, DS, packet. The receiver then will send an Acknowledgement, ACK, packet to complete the transaction.

4.1.2 Organized Access Schemes

In organized access schemes the channel is sectioned off into separate sub-channels. The separation may be in time which leads to TDMA schemes. Nodes transmit
over the entire bandwidth, but in bursts. Another approach is to partition the bandwidth into smaller sub-channel, and each node will operate on the sub-band at all times. This leads to FDMA method. It also possible to separate transmissions in the "Code Space". Each code, is a unique assignment of transmission energy in the time and frequency domain, such that many nodes will be able to access the entire bandwidth concurrently. Spread Spectrum techniques are examples of Code Division Multiple Access schemes. Spread Spectrum techniques will be described in more detail in subsequent chapters. Figure 4.3 illustrate these concepts.
4.2 Ad-Hoc Networks and Self-Organization

An ad-hoc network is one which has no fixed infrastructure. In such a network the nodes themselves must determine connectivity and form links and schedule transmissions. In the early studies focused on multi-hop ad-hoc networks in late 1970’s and early 1980’s two main approaches to the link layer protocols were dominant. One was based on “random access” schemes such as ALOHA [54] or CSMA and their variants [56, 57]. This approach is very simple algorithmically but could not in any form guarantee any quality of service. The second approach has a more structured view of the link layer. It determines connectivity of the network and based on it establishes a form of schedule in the network; i.e. separate channel uses in an organized manner to provide conflict free transmission for all the nodes involved. We call this approach the Self Organization method. The early classical solutions for self-organization of wireless ad-hoc networks are described in detail in the survey paper by Robertazzi and Sarachick in [58]. The paper by Cidon and Sidi [59] also contains a comprehensive overview of the variations of the channel assignment problem for self-organizing networks.

The problem of self-organization for ad-hoc networks is challenging [60]. The difficulty lies in the fact that the network connectivity is not precisely known (because of movement of nodes for example). And also, even when the connectivity is completely known, the problem of assigning conflict free AND efficient schedules to the network is very hard [61]. Therefore the major obstacles which must be overcome to solve the self-organization problem in mobile ad-hoc networks are

- connectivity (topology) discovery
- channel assignment (separation of link or node activities in time, frequency,
or code domain) to avoid conflicts, subject to some efficiency criterion.

- maintenance of connectivity

The problem of routing is also an important issue which has received considerable attention. However since it lies out of the scope of this work we will direct the reader to other sources for further information.

4.2.1 Related Work

The self organization problem for ad-hoc wireless networks was first studied in the context of military tactical communication networks such as the HF ITF network and others [62, 63]. Here nodes are mobile, complex radio transceivers which possess relatively high transmit powers, practically unlimited energy reserves, and the objective is to be able to form and maintain network connectivity in the face of node mobility without interruption of service. The total number of nodes or at least its upper bound is assumed to be known. It is also assumed that a network wide slot synchronization is already in place.

The Linked Clustering Algorithm (LCA) proposed by Baker, Ephremides, and Wieselthier [64, 65] solves this problem by forming a hierarchical network topology consisting of a backbone network among local masters (clusterheads) and a local area network, among nodes in the vicinity of the local master (a cluster), and relays or gateway nodes which connect clusters together. The algorithm has two phases: first exchange of messages over an existing TDMA frame to determine connectivity. After the connectivity, cluster heads, gateways, and ordinary nodes are determined, the known topology will be used to assign a schedule of transmission/reception slots to links using the Link Activation Algorithm (LAA),
which is only capable of avoiding primary conflicts. The membership in the clusters and choices of cluster heads and gateways change as network connectivity changes. Therefore LCA and LAA algorithms are run periodically to track these changes.

Many ad-on modifications of this basic approach are proposed to make it more distributed. For example, in the Distributed Evolutionary Algorithm (DEA) [66], the idea is that once the nodes possess the same connectivity information, they will be able to run the same algorithm and come up with the same assignment result. Thus the problem of link or node activation is transformed to the problem of disseminating the network connectivity information to all the nodes in the network. This link assignment method is able to avoid secondary conflicts as well.

Other self-organizing network algorithms include DARPA’s PR-NET [36], LayerNet [67], Self-Organizing Wireless Adaptive Network (SWAN) [68], and MultiCluster Mobile Multimedia Radio Networks (MMMRN) [69].

The MMMRN is based on LCA. It also has mechanisms for providing quality of service which LCA does not. The SWAN protocol uses the data portion of network to change the link assignments gradually, as opposed to breaking down the schedule each time a link goes down, i.e. it is an elastic protocol which changes the schedule gradually. LayerNet is very similar to the DEA, and PR-NET does not use any form of network-wide synchronization. Except for PR-NET all these networks assume some form of slotted TDMA synchronization to be in place and are designed to handle topology variations due to mobility.
4.2.2 Ad-hoc Wireless Networking Standards

The contention based access methods related to ALOHA have been implemented in commercial standards mainly due to their low levels of complexity and ease of implementation. The IEEE 802.11 [70] and the family of HiperLAN [71] standards are examples of this category. Here the mobile nodes are usually portable computing devices outfitted with fairly sophisticated wireless transceivers. Example: a PDA or laptop computer with an IR or RF transceiver, which is used indoors mostly. In the ad-hoc mode of operation, a collection of nodes wish to form a network "on the fly". The 802.11 supports ad-hoc and infrastructure topologies. A Carrier Sense Multiple Access with Collision Avoidance (CSMA/CA) combined with variation of MACAW with four message exchange is used. HiperLAN is a European standard (ETSI) which supports ad-hoc and infrastructure topologies. Uses CSMA/CD and CSMA/CA. HiperLAN2 supports ad-hoc networking.

Industry standards are moving to smaller and less complex wireless paradigms. Standards such as Bluetooth [72] and HomeRF [73] aim to replace the wire in home and office devices. In this fashion they have need to support ad-hoc networks which need to self-organize. HomeRF uses a stripped down version of 802.11 for its physical layer. At the MAC layer it uses Share Wireless Access Protocol standard (SWAP). SWAP uses a hybrid TDMA/CSMA approach with frequency hopping.

The Bluetooth MAC layer is a star network topology, were a Master node is able to have up to seven Slave nodes attached to it to form a Piconet. The Piconet uses a centrally assigned TDMA schedule for channel access. In a Piconet all nodes are synchronized to the Master. However there are provisions for internetworking of Piconets to form Scatternets. The final topology is somewhat
similar to that of LCA, with Masters equivalent to cluster heads, and a *piconet* to a cluster.

The general trend in the development of wireless ad-hoc networks has been from more complex to less complex; the size and form factor have become smaller forcing the energy source to shrink as well. This trend continues for sensor networks.

### 4.3 MAC Organization for Sensor Networks

The new paradigm of sensor networks introduces a number of new operating constraints which are different from those encountered in conventional wired and wireless communication networks. In sensor systems there are many nodes per human user [74]. These systems may also operate in remote locations, where easy access to individual nodes is not possible. This imposes the requirement for un-attended and robust operation under highly variable conditions. This is a situation which is quite unlike operating parameters of conventional wired or wireless communicating devices. The un-attended operation in possibly hostile surroundings requires the nodes to be able to function in close to failing modes. These nodes must also start their operations automatically. This means that each sensor will be functioning in three distinct phases of initialization, normal operation and failing. Therefore procedures which control all aspects of the operation of the node must adapt to its internal state and that of the outside environment. For example, each node may need to vary its clock frequency, transmission duty cycle, transmission power, or sensing intervals as time goes on.

The sensor network is inherently a distributed system. Unlike wireless cellular
systems where a base-station controls the behavior of the users in its associated cell, in a sensor network it is not desirable or even possible to have a single point of control, command, and coordination. However it is still an open question how flat the network topology must be. It is conceivable that at different stack layers, different degrees of topological flatness may exist. For example, at the link layer, the network may be completely flat, with nodes allocating resources and organizing themselves in a totally distributed fashion, based on strictly local information. And yet at the networking layer clusters and cluster-heads may be formed to aid the routing. It may also be more advantageous to have a hierarchical topology, even at the link level, when heterogenous nodes are deployed side-by-side in the same sensing arena. For example when some of the nodes have more advanced equipment on board, such as a GPS transceiver, or more capable signal processing boards and hence more powerful batteries, the network topology could have a more hierarchical flavor, with the more capable node commanding more functions. It can be hypothesized that at higher levels, a more hierarchical architecture must be used to filter data, to manage high volumes of raw data and to perform data fusion functions.

4.3.1 Related Work

There have not been many research efforts concentrated on the problem of MAC design for sensor networks. The work described in [75, 76] describes MAC for large, scalable packet radio networks and [77] investigates a number of channel access schemes for Radio Frequency Tags (RF-Tags).

Shepard [75] has studied the problem of management of the radio channel for a packet radio network with a very large number of nodes. Although that problem
is concerned with nodes which will cover a metropolitan area and is not focused on a low energy or low complexity solution, the ideas propose to achieve scalable and decentralized operation. These are attributes which are of great importance in a sensor network and are related to this work. Network-wide coordination and synchronization are given up in favor of strictly local scheduling. In addition two different methods for mitigating interference generated by local and the aggregate of faraway nodes are used. Local transmissions take place in time in a pseudo-random fashion. That is, a variation of time-hopping is used to separate local transmissions from each other. At the same time each transmission is carried out by spread-spectrum (Direct Sequence) to mitigate background interference generated by faraway nodes. Because of time-hopping no fixed transmission times are scheduled to carry traffic between fixed pairs of nodes and therefore, receivers must always be turned on in order to receive all intended packets. For this reason the described method is not an energy efficient scheme.

The system under consideration for RF-Tags [77] is a single cell topology with a single powerful basestation which controls the RF-Tags in a single hop (star network) configuration. The traffic is highly assymetric (with the information flowing from the base station to the RF-Tags). The single base station usually controls many RF-Tags and therefore issues of efficient channel access and fairness are important. Since RF-Tags use batteries which may not be changed the power conservation is also an issue here. The three protocols discussed are

1. Grouped tag-TDMA (similar to POCSAG [78] paging scheme)

2. Directory protocol: at the beginning of each transmission interval a list of tags which will receive messages are advertised. In this manner after
reading the directory, the tags which are not going to receive data in this interval can go to sleep until next interval.

3. Pseudorandom protocol: a time-hopping approach (each tag has its own unique wake up times which are generated abased on a pseudo random sequence which is controlled by the base station)

4.4 Summary

Self-organizing radio networks have been first studied in the context of military tactical communications networks. That work has lead to a great body of work dealing with issues of channel management for efficient (i.e., high throughput, low delay) communications for ad-hoc, multihop networks. The two major approaches taken have been to use contention-based random-access methods such as ALOHA [54] and its variants. The other methods, have used organized channel access schemes which lead to variations of TDMA/FDMA/CDMA access. For the scheduled channel access methods the problem of channel management becomes a big issue. The commercial market has had its own approach with the use of ALOHA like access schemes for Manets (Mobile Ad-hoc NETworks). However these solutions are not appropriate for sensor networks. The MAC protocol for the sensor netowkrs must be self-organizing, robust, and low energy. This leads to requirements for decentralized, scalable, and scheduled communications. In Chapter 5 we describe and investigate the Self-organizing MAC for Sensornets (SMACS) protocol which fits the above requirements.
Chapter 5

SMACS Protocol

The objective of the self-organization protocol at the link layer is to form a connected multi-hop network for a collection of randomly placed wireless sensor nodes. The algorithm must start the network cold. No information is available locally at the time each node starts. The node must find its radio neighbors, and participate in a group effort to form an ordered method of channel access. The single most important constraint is energy, and therefore, the self-organization methods described in previous chapters are not suitable for our purposes. Also in most systems described in chapter 4 it is assumed that a type of network wide synchronization is already in place. In this work we are concerned with a problem that occurs in an even earlier stage of network formation, and that is the problem of formation of an early skeletal time frame. In this chapter details of a self-organization protocol which achieves these goals will be given.
5.1 Motivation

5.1.1 Distributed Control

It is clear that a centralized control scheme is not suitable. The centralized methods do not generally scale well. Although the centralized resource allocation may lead to more efficient utilization of some resources such as bandwidth, the high energy cost of communications with a central controller cannot be tolerated in the sensor network environment. Reliance on a central master also leads to brittle architectures with the master being the most obvious point of failure in the system.

However it is not clear at this point whether a totally flat architecture or a somewhat hierarchical model at the link layer is more suitable. A deciding factor could be the level of homogeneity of the network at the hardware level. For example if different node types are deployed where some have more capable batteries and processing capabilities, then perhaps a more hierarchical topology should be used, while in a homogenous network where all the nodes are identical a flat architecture is better. Another deciding factor may be the functional objective of the network.

5.1.2 Medium Access Scheme

Channel access schemes which require continuous monitoring of the communication medium are unsuitable because they require the radios to be powered on at all times. For small ranges encountered in sensor networks it is almost as costly for a radio transceiver to be receiving as it is to be transmitting. Therefore the channel access scheme must make it possible to turn off the radios frequently.
Consequently CSMA methods are not suitable. This leads to a need for a time schedule i.e. a TDMA like channel access scheme. However conventional TDMA has a centralized element since a single TDMA schedule must be calculated. Also all the terminals participating in the schedule must be synchronized at the slot level. In conventional TDMA systems, such as satellite communications, this tight slot synchronization is needed for purposes of bandwidth efficiency.

In sensor networks it is possible to relax this network-wide slot synchronization requirement and as a result do away with the need for a single master. We contend that it will still be possible to maintain a scheduled mode of channel access. In this vein we introduce the concept of Nonsynchronous Scheduled Communications (NSC). Nonsynchronous refers to the notion that slot boundaries in the entire network need not be aligned and scheduled refers to the idea that every node is aware of the times it needs to turn its radio on and off in order to communicate with neighbors. The concept of NSC will be further explored in the following sections.

## 5.2 SMACS Protocol Details

Let $R$ be the set of all orthogonal channels available to our network. A channel could be a combination of time, frequency, or code division. Consider a network of $N$ nodes, with connectivity matrix $C = [c_{ij}]$. A link $l_{ij}$ exists from $i$ to $j$, if $j$ is able to receive signal from $i$ and $c_{ij} = 2$. If the received signal is not strong enough to be detected properly, but strong enough to interfere with other good signals, $c_{ij} = 1$. Otherwise $c_{ij} = 0$. Let this network have a total of $L$ links, numbered from 1 to $L$. Two links $l_1$, from node $i$ to node $j$, and $l_2$, from node
$k$ to node $m$, are defined to be interfering if at least one of the members of the set $\{c_{kj}, c_{im}\}$ is greater than zero. Now an interference free organization of the network will be a mapping, such that in the entire network no two interfering links have the same channel $r \in R$ assigned to them. The size of this organization is the total number of distinct channels assigned. It is a well known fact that finding a mapping where the total number of assigned channels is minimum is an NP complete problem for general topologies.

In the sensor-networks we relax the requirement for optimal organization. After all we are not concerned with pumping a lot of information through the network as fast as possible. We only require an interference-free mapping, regardless of its size. The important constraint is that this mapping must be found using minimal energy.

For self-organizing ad-hoc networks the connectivity matrix must first be determined. Afterwards a centralized or distributed mapping algorithm is run to map each link to a specific channel. For the distributed case, a third phase exists to resolve any potential conflicting channel assignments that may arise due to having only partial connectivity information at each node.

For energy constrained systems, this general approach requires too much message passing and is therefore too costly. A node does not know the number of its neighbors ahead of time. Therefore it does not know when to stop the neighbor discovery phase. Also, this stopping time is different for each node, because the nodes have different numbers of neighbors and also they start the discovery phase at different times. If we impose an arbitrary stopping time, then there will be some nodes which have not had a chance to find any information yet. An intuitive solution is to mix the discovery phase and link assignment phases together. In
the simplest case this means that a node will assign a channel to a link, as soon as it is discovered. The node will then continue to find other neighbors and so on.

This procedure relieves the system from establishing network-wide synchronization as well. This means that different nodes may have different time-references, and that slot boundaries need not be aligned throughout the network, and hence the idea of NSC is born. A simple example demonstrates this point. Take a linear multihop network, as shown in Figure 5.4.

In this network each node is able to hear its immediate neighbors only. Each node $i$ communicates with its right and left neighbors only. It must therefore be aware of the timing of these two nodes: i.e. there must be agreement between each pair as to the times each transmits and the other receives. Node $i$ and $i + 2$ may not transmit simultaneously while $i + 1$ is listening. Beyond this, node $i$ and $k, k \leq i - 2$ or $k \geq i + 2$, need not coordinate in any form.

For general topologies each node synchronizes its transmission times with the immediate neighbor it has just discovered without adjusting the timing of its other allocated links, if they exist. As more nodes are discovered and attached to each other a frame structure emerges. In this structure, time is segmented into Super Frames. The length of a Super Frame is fixed. The Super Frame is broken into smaller frames. Each frame is used for a different purpose. Note that the size of each frame is not fixed, and may vary in time, for a single node. It may also vary from node to node. Figure 5.1 illustrates the concept of the Super Frame.
5.2.1 TDMA FRAME

The TDMA portion of the Super Frame is used for scheduled communication between nodes. The startup algorithms which will be described in subsequent sections are responsible for assignment of channels in the TDMA frame. In this mode a node transmits and receives mostly control and housekeeping packets to and from neighbors which have already been discovered. The TDMA slots, which are permanently assigned (until they fail), may be used as signalling channels to establish new links on the fly between neighbours when there is need for local, cooperative activities.

5.2.2 Un-assigned Bandwidth

The un-assigned bandwidth is used for formation of local networks on the fly to deal with specific tasks of sensing or collaborative activities. For example, when the existence of a target at some locality inside the hull of the network is detected,
a subset of nodes may need to form a local network to exchange sensor data and perform beam-forming [79]. Not all nodes need to be involved in this operation. Also the set of nodes which must group together to do the task may not be the same for different instances of target detection.

### 5.2.3 BOOTUP FRAME

The entire set of activities responsible for neighbor discovery and channel assignment occur in this period. When a node is in BOOTUP mode, it is in one of four possible states. A node passes from state to state upon reception of a valid expected message from another node over the air, or upon time-outs when certain messages are not received. The four states are SCAN, SCAN-RESPONSE, INVITATION, and INVITATION-RESPONSE. During this period, nodes exchange only four types of messages. These messages are:

- **TYPE1**: short invitation containing node’s id. The node which sends it, is the *inviter* during the search and hand-shaking transactions.

- **TYPE2**: response to **TYPE1**. The node which sends it, will be an *invitee*. There may be more than one *invitee* for each *inviter* node. This message gives the *inviter* and *invitee*’s addresses, and *invitee*’s attached state.

- **TYPE3**: response to **TYPE2**. Indicates which *invitee* was chosen. The selection process is based on received signal levels and order in which **TYPE2** messages are received. It contains the following additional information depending on the node’s attached state:

  i) *Inviter* not attached: none.
ii) Invited, inviter attached: inviter’s schedule and frame epoch.

iii) Invitee not attached, inviter attached: proposed channel for the link, calculated by inviter.

- **TYPE4**: response to **TYPE3**.
  
i) Invitee not attached, inviter not attached: channel determined by the invitee.

ii) Invitee not attached, inviter attached: none.

iii) Invitee attached, inviter not attached: channel determined by the invitee.

iv) Invitee attached, inviter attached: channel determined from own and inviter’s schedule information.

The messages are exchanged based on the state of the nodes as follows:

- **SCAN**: in this state the node scans the radio channel continuously on a given fixed frequency. The node’s receiver is on and it is waiting to hear a **TYPE1** or invitation message from another node.
  
  - If a **TYPE1** message is received in a window of duration of $\delta_{SCAN}$, the time the message is received is saved at the receiving node, as $T_{TYPE1}$. A **TYPE2** message is prepared and a number is chosen at random between 1 and $K$. The **TYPE2** message is broadcast on the $K^{th}$ sub-slot after $T_{TYPE1}$. The node will then go to SCAN-RESPONSE state.

  - If a **TYPE1** message is not received in $\delta_{SCAN}$, the node itself will prepare a **TYPE1** message and broadcast it, and go to an INVITATION state and wait for arrival of **TYPE2** message(s).
• SCAN-RESPONSE: once in this state the node is in receive mode. It is scanning the channel for a TYPE3 message from the same node which prompted the node to go to this state. When such a message arrives within $\delta_{\text{SCAN-RESPONSE}}$ of entering the state, and based on its contents, the receiving node determines that the two nodes are able to form a new TDMA link, the node prepares a TYPE4 message and sends it. At this point the node adds the new proposed link as a pending one into its schedule. The node will then turn itself off until the beginning of the next TDMA period. During the next TDMA period the new pending link is tested by means of exchange of very short NOM packets. If no valid message arrives the node will go back to SCAN mode and start a new search.

• INVITATION: In this state the node is waiting for arrival of TYPE2 messages in response to the TYPE1 message it just sent out. The node will stay in this state for $K$ sub-slots. If no valid TYPE2 messages are received then the node will go back to SCAN mode and start its search anew. Otherwise it will choose one of the arrived messages according to some criterion. At this time this criterion is the first arriving message. However, combinations of criteria such as received signal strength, time of arrival, and number of nodes attached to the sender may be used. At the end of the $K$ sub-slots the node prepares and sends out a TYPE3 message addressed to the proper node and goes to INVITATION-RESPONSE to wait for the arrival of TYPE4 message.

• INVITATION-RESPONSE: The node awaits arrival of TYPE4 message. Upon reception of the message within $\delta_{\text{INVITATION-RESPONSE}}$ of entering
the state the node will mark the new proposed link as a pending one, turn itself off, and wait until the next TDMA period to test the new link.

The state transitions are depicted in Figure 5.2. A node engages in a node attachment operation with only one other node at a time. During the handshake that takes place at discovery time the two nodes exchange their schedule information. Based on this information they attempt to find a time period in their respective schedules which is un-assigned and free for both. If there is such an interval then the time interval is assigned to the new link and a frequency band (or a hopping pattern) is also assigned at random (to protect against collisions with unknown conflicting links in the vicinity).

Node Attachment Scenarios

**Definition:** a sub-net is a collection of nodes which form a connected graph and all have coinciding Super Frame epochs.

The BOOTUP algorithm must be able to handle three scenarios of node attachment:

- **node ↔ node** attachment: when both nodes are unattached.

- **node ↔ sub—net** attachment: when a node attaches to another which is already attached.

- **sub—net ↔ sub—net** attachment: when two nodes which are already attached to other nodes discover each other.

The case when the two nodes belong to different sub-nets is the most challenging and is depicted in Figure 5.3. This case is most challenging because each of
the two nodes already has its own time reference (a Super Frame structure), and this frame may already be filled to some degree with assigned slots. However, because of the NSC concept, there is no need to resync the two existing schedules. All that is required is information about the offsets of the time references of the two schedule (i.e. how far apart are the Super Frame epochs), and the location of assigned slots in the two schedules. Because we are not going to re-shuffle the assigned slots, it may not be possible for the two nodes to connect. For example if there is no overlap between the respective TDMA Frames or none of the un-assigned slots in the TDMA Frames coincide. In this case the two nodes will
disengage from each other and continue to search for other nodes.

In Figure 5.3 node\textsubscript{i} wakes up, and listens on BOOTFREQ. It does not receive any invitations and therefore it broadcasts a \textit{TYPE}1 at time $T_{T1}$. It will wait and listen to the channel for a fixed period of duration $K$ sub-slots after transmission of \textit{TYPE}1. All the nodes which hear node\textsubscript{i} and wish to respond to it will transmit a \textit{TYPE}2 message at random during one of these $K$ subslots. Node\textsubscript{j} is one of these nodes. The inviter node, node\textsubscript{i} in this case, chooses node\textsubscript{j}. In \textit{TYPE}3 message node\textsubscript{i} announces its choice. In \textit{TYPE}3 message is also included the beginning time of node\textsubscript{i}’s next Super Frame, $FRAMEBEGIN_i$, and its schedule. When node\textsubscript{j} receives this information, it will first determine if it is possible for the two nodes to establish a link by means of determining whether the two nodes have enough overlap between their respective TDMA Frames. If so then node\textsubscript{j} will pick two slot locations as the time intervals for the new pending link. The location of the pending slots along with node\textsubscript{j}’s $FRAMEBEGIN_j$ is transmitted.
in \textit{TYPE4}. \textit{Node}_j will go to sleep after this. It will wake up at the beginning of its next \textit{TDMA frame}.

If the new proposed slot locations are agreeable to \textit{node}_i, it will mark the new link as a \textit{pending}, go to sleep, and wake up at the beginning of its next \textit{TDMA frame}. If not it will start the whole search all over again. This continues until either a new node is found and attached or the \textit{BOOTUP} period ends.

Note that if the number of available slots in the TDMA period is large there is higher likelihood of success in attaching nodes at the first attempt. The smaller the number of attachment attempts the lower the amount of energy used. Therefore a trade-off between energy usage and available bandwidth exists.

\textbf{BOOTUP and Frequency Hopping}

The \textit{BOOTUP} operation may be extended to operate on a very-slow frequency hopping channel where an entire packet is transmitted over one or very few hopping frequencies. The main task of capturing \textit{TYPE1} messages can be done as follows.

An outgoing \textit{TYPE1} message will be repeatedly transmitted over a sequence of frequencies. This sequence will be a hopping sequence with short period say 16 hops. The nodes scanning the channel will listen on all 16 hops according to their own hopping pattern phase until a hit occurs. At this point the receiving node will be in coarse synchronization with the transmitter. Once the \textit{TYPE1} message is captured the rest of the hand-shake transaction and channel assignments will be the same as before. The drawback of this method is that extra time and extra energy are needed to connect the network. The extra amount of energy is required to transmit multiple copies of the \textit{TYPE1} message at the \textit{inviter} node.
5.3 Master Slave Bootup

The SMACS startup algorithm builds a totally flat topology at the link layer. However, we would like to compare this with the performance of a link layer startup algorithm which builds a more hierarchical topology. The network formation methodology which is used in the Bluetooth standard [72] provided a good starting point for the hierarchical approach.

A standard Bluetooth network is comprised of a single MASTER node. The first node awake is usually the MASTER. This node will then search for and attach up to seven other nodes to itself as Slaves in a star topology. The Slaves follow the timing reference of the Master. This single star network is a piconet. To extend multihop capability to this network different piconets are connected together to form scatternets. The mechanism is as follows: a Slave of a particular Master may itself become a new Master, or the Slave of another master. In this manner some Slave may act as gateways between adjacent piconets and connect them. Each piconet is distinguished by the timing reference of its Master. When a Slave is attached to two different Masters it must then follow two different timing references.

The Master Slave Bootup (MSB) algorithm which we have developed parallels the Bluetooth concepts, except that practical issues such as content of messages, timing of messages, assumed signalling rates, and consequently message lengths, etc. are changed to be comparable to the BOOTUP algorithm.

There are three message types in MSB: INVITE, INVITE-RESPONSE, VERDICT. Also there are two logical types of nodes: MASTER and SLAVE. Only a MASTER node sends an INVITE, but all nodes may choose to respond to an
INVITE. A MASTER sends out an INVITE message to find and attach new neighbors. Another node which hears this INVITE, and decides to respond to it, will transmit an INVITE-RESPONSE message at some random time somewhere within the window $\Delta_{\text{response}}$ after reception of the INVITE. The response is sent over a frequency band centered at HANDSHAKEFREQ. The values of $\Delta_{\text{response}}$ and HANDSHAKEFREQ are chosen by the MASTER, usually at random, and are included in the INVITE message. The INVITE-RESPONSE includes the respondent’s id, its connectivity information, and link assignment schedule if it is already attached. Once the MASTER has received all the responses, it will calculate a conflict free schedule for all the participating nodes, and form a local star network, with itself at the center. The new schedule is broadcast over HANDSHAKEFREQ in the body of a VERDICT message at the end of $\Delta_{\text{response}}$ window.

At startup there are a number of MASTER nodes which will form a number of local star networks. In order to connect the entire collection of nodes these local start networks must all become connected. At some point in time some of the SLAVE members of the star networks may declare themselves as MASTERs and start searching for other neighbors. In this fashion it is possible to connect the entire network as an interconnection of many local star formations. Note that unlike the Bluetooth standard, where all the SLAVEs are time synchronized with their local MASTER, we use the NSC concept. This is to ease the process of connection of two different local star networks.

Details such as which nodes are chosen as MASTERs, and under what criterion SLAVEs become MASTERs will affect the behavior of the algorithm. Here
we choose MASTERS at random, i.e. a node is a MASTER with probability \( p_m \), \( 0 < p_m < 1 \). A node becomes a MASTER if it is already attached, but to less than \( N_n \) other nodes. As the number \( N_n \) becomes smaller, the MSB moves closer to building a flat topology. If a very long time has passed and a SLAVE has not heard from any other nodes, it will become a MASTER. In this algorithm, it is possible to assign slots throughout the entire frame therefore distinct BOOTUP and TDMA periods do not exist.

### 5.3.1 Power Control

We claim that it is more energy efficient to transport bits in the network along many short range hops than via a single longer range hop. The key reason for this is the fourth power drop-off of path-loss for near surface propagation as a function of distance [80]. This phenomenon makes long distance communications much more costly in terms of energy usage compared to an environments such as those considered in [81] with 2nd order power drop-off.

To further illustrate this point, we investigate a simple example of a linear topology network, and follow the same line of analysis used in [81]. The network diagram is given in Figure 5.4. There are \( n + 1 \) nodes, with separation \( r \) between adjacent nodes, all placed along a straight line. A single information symbol is to be sent from node 0 to node \( n \). Two scenarios are considered. In the first scenario, node 0 transmits the single bit directly to node \( n \) in one large hop. This requires the node to use a relatively large transmit power to reach the destination node particularly if the values of \( r \) or \( n \) or both are large. In this case a single transmission and a single reception takes place. The radios on the nodes consume \( E_J/\text{bit} \) when turned on, in either transmit or receive mode, and the radio front
end consumes $\alpha J/(\text{bit} \times m^4)$ to amplify the signal, to arrive at a receiver 1m away, having a desired signal to noise ratio of $s_1$. The total energy consumed is

$$E_{\text{direct}} = E + \alpha n^4 r^4$$

(5.1)

In the second scenario, the single bit is transported to the destination, via $n$ small hops. In this case there will be $n - 1$ receptions, and $n$ transmissions, each over a distance of $r$. The total consumed energy will be

$$E_{\text{mult}} = nE + n\alpha r^4 + (n - 1)E$$

(5.2)

$$= (2n - 1)E + \alpha nr^4$$

(5.3)

Wanted are values of $r$ and $n$ for which direct method consumes less total energy per bit than the multiple method. That is

$$E_{\text{direct}} \leq E_{\text{mult}}$$

(5.4)

$$E + \alpha n^4 r^4 \leq (2n - 1)E + \alpha nr^4$$

(5.5)

$$r^4(n^3 + n^2 + n) \leq E/\alpha$$

(5.6)

To understand the implications of this result, we use the following example. For state of the art low power radios, operating at 2.5V and 30mA, with power
efficiency of approximately 5 percent, the values of $E = 7.9 \times 10^{-7} J/bit$ and $\alpha = 7.3 \times 10^{-9} J/(bit \times m^4)$ are typical. These values are valid for 2FSK non-coherent reception, with noise power of $N_p = -67 dBm$, at a symbol rate of $1/T_b = 10 \text{ Kb/s}$ and $BER = 10^{-3}$.

Defining $F(n, r) = E/\alpha - r^4(n^3 + n^2 + n)$, the graph of Figure 5.5 gives the region in the $r \times N$ plane where direct communications is better than multiple hops. It can be seen that, the feasible number of steps of length $r$ per hop quickly drops down to unity, as the range between adjacent nodes increases or number of nodes increases. For comparison, we include the same region for the case where path loss drops off with second power of distance, in Figure 5.6. It is clear that, for second power loss, in many cases, direct communications is more feasible. But as power loss becomes more severe, multiple hops become more feasible. Therefore, at least for linear topologies, it can be concluded that connecting the network by means of forming links which require the lowest transmit powers will result in lower energy consumption for long-haul transport of bits, and thus extend the lifetime of the network. We adopt the same strategy for spatial configurations other than straight lines.

5.4 Time Management of Protocols

As the network becomes more connected, that is, each node find and attaches more neighbors, the need for finding new neighbors is reduced. It also becomes harder to find new neighbors. So it is reasonable to reduce the duty cycle of the time each node spends in BOOTUP. A number of different methods may be used
Figure 5.5: Feasible region for direct communications, for fourth power path loss.

to achieve this limiting effect.

- Each node will be actively participating in BOOTUP with probability $p_a(k) = 1/(N_n + 1)$, where $N_n$ is the number of neighbors the node has at the beginning of a SUPER FRAME $k$.

- Reduce the length of BOOTUP period in each SUPER FRAME, inversely proportional to the number of a node’s neighbors, or the length of time it has been active. After a maximum number of neighbors are attached to a node, it will stop participating in BOOTUP. It will start searching for new nodes, if and when some of its neighbors are lost.
Figure 5.6: Feasible region for direct communications, for second power path loss.

5.5 Simulation Model

Our protocols are implemented in a simulation environment written in PARSEC [82]. In this model, each sensor node is modelled as a PARSEC entity. The functionality of each networking layer, i.e. PHY, MAC, Networking, and etc. are implemented as methods, or functions, within the body of the entity.

The sensor network is modelled as a collection of nodes, which transmit and receive packets over a radio channel. The channel is also modelled as a specific entity, which receives messages from nodes, implements radio propagation effects such as path loss and shadowing, on each packet, and delivers it to all nodes within radio earshot of the transmitting node. The channel entity simulates a broadcast channel. The entire simulation is controlled by a driver entity which is responsible for reading all the input files, setting up each entity, informing the channel of the number and location of nodes, and collecting simulation statistics, when the run is finished.
Inter layer communications within a single node, and PHY-PHY communication between different nodes, are accomplished by means of passing of messages. When a packet is generated at a node, it is passed down from layer to layer, until it reaches the radio layer of the sending node. The radio layer generates an over the air packet, and sends it to the channel entity. The channel entity will then simulate the conditions of a radio broadcast channel, and deliver the packet to all nodes which are close enough to receive it. The simulation model is depicted in Figure 5.7.

![Simulation Model of Self-organizing algorithms](image)

**Figure 5.7:** Simulation Model of Self-organizing algorithms.

### 5.5.1 The Propagation Model and Packet Capture

The radio channel model simulates Log-normal shadowing with $\sigma = 8dB$. In addition, additive white gaussian is added to transmitted signals. For each transmit power level, two ranges $R_1$ and $R_2$, with $R_1 < R_2$ are considered. The smaller radius corresponds to the range of good communication for the transmitter, and $R_2$ is the range over which the node is capable of producing interfering signal
levels. The value of $R_1$ depends on the transmit power level, propagation loss model, and additive background noise levels. Here we set $R_1$ to the distance which corresponds to received SNR of $s_1$. The value of $s_1$ is chosen to yield a raw symbol error rate of $10^{-3}$ for the given modulation method in additive noise.

The value of $R_2$ depends on the sensitivity level of the radio receivers. Here we set the value of $R_2$ to the distance which yields SNR ratios of $s_1 - 11dB$. A good packet is one which has received SNR above $s_1$. Note that due to shadowing, the goodness of a packet may not be determined solely based on distance between transmitter/receiver pair. Only good packets which have no overlap with other packets are captured. All other packets are dropped.

### 5.6 Simulation Results

A number of different simulation experiments were conducted to investigate the performance of our self-organization algorithms. We are interested in determining:

- **Scalability**: the ability to connect networks of many nodes, where the protocol overhead stays essentially constant, regardless of network size
- **Ability to conserve energy when connecting the network**
- **Ability to conserve energy both in short term and in the long run**

The following set of experiments test one or more of the above attributes for the network formation algorithms described previously.
5.6.1 SMACS vs. MSB

We are interested in determining whether performance tradeoffs exist when we form a totally flat network by means of the SMACS protocol, compared to a more hierarchical topology, as is done in the MSB scheme. Particularly we are interested in determining the time and energy it takes to build the network under each of the algorithms. To generate the following results, the BOOTUP and MSB procedures were run each for 1000 different random configurations of collections containing 18, 45, 150 and 400 nodes respectively. Each network topology has spatial node density of $\lambda = 0.04$ nodes/m$^2$. The nodes are distributed randomly and uniformly in a square shaped plane. The Super Frame is set to 40 slots. There are 100 different frequencies to choose from, apart from the BOOTFREQUENCY. For the BOOTUP algorithm, the TDMA frame contains 20 slots. That is, only half of the bandwidth is set aside for scheduled communications. In all simulations a fixed transmit power of 3.0 mW is used. Two scenarios are considered: BOOTUP with fixed transmit power, and MSB with fixed power. For all cases, the initial invite is sent over the common BOOTFREQUENCY band. However, the rest of the handshaking procedure for all cases is carried out over the specific hand-shaking frequency of the transaction. The simulation stopping time is the first instance when the network becomes connected.

Figure 5.8 gives the time, in SUPER FRAMES, until the network becomes connected for the first time. We see that the MSB is able to connect the network faster, for this experiment. This ability to connect the network faster is due to the fact that a single master node is able to connect many nodes within a single handshake transaction, while the BOOTUP (or SMACS) method, adds at most one neighbor at a time, for each handshake transaction. However, as
we see in Figure 5.9, the MSB, requires nodes to be, on average, turned on for longer durations, to achieve the faster connection times. This is again due to the fact that, the MASTER nodes in MSB, must stay awake for a much longer time, in order to hear all the responses to each of their INVITE messages.

![Graph showing elapsed time until network is connected.](image)

Figure 5.8: Elapsed time until network is connected.

The consequence of longer duty cycles for the radios is evident in Figure 5.10, where we see the average used energy until connection time for MSB is larger than BOOTUP fixed power. The conclusion to be made here, is that by adding neighbors one at a time, as is done on the SMACS procedure, we will be able to save energy, at the cost of prolonging the time it takes to connect the network.

### 5.6.2 Network Lifetime

The average consumed energy per node in 500 Super Frames was measured under the following scenarios:
Figure 5.9: Duration of time radios are powered up.

1. Scenario 1: Each node continues to search for more neighbors in each Super Frame with probability \( p_n = 1/(N_n + 1) \) where \( N_n \) is a node’s number of neighbors.

2. Scenario 2: In addition to the constraint in the above scenario, a node stops searching for nodes, after it has found \( N_{max} \) neighbors.

Both Scenarios were run for a single network of 18 nodes, and the second one for a network of 150 nodes, with fixed values of link transmit power, for node density of \( \lambda = 0.04 \). In Figure 5.11 we see that, as expected, the consumed energy increases with increased link transmit power. However, after inspection of the sources of energy consumption, it was found that most of the energy consumption is due to transmissions of \( TYPE1 \) messages, which are never acknowledged. This idea is supported based on the data given in Figure 5.12. The top curve gives the total number of transmitted BOOTUP messages in 150 SUPER FRAMES.
The middle curve gives the total number of TYPE1 messages sent. The lower curve gives the number of TYPE1 messages which were sent and never received by another node. So we see that a very large portion of the messages which are sent over the air are in effect wasted, and do in fact waste energy. So, if we are able to limit the number of transmitted TYPE1 messages, and still manage to connect the network in a reasonable time, we may be able to save considerable amounts of energy.

As it turns out, the BOOTUP portion of SMACS protocol, is able to connect the majority of a node’s neighbors very quickly, and after that, there is no point in using the entire un-used bandwidth of the node to search for more nodes. For this reason, we will allow a node to participate in BOOTUP only until it has found $N_{max} = 5$ neighbors. The improvements in energy consumption for Scenario 2 are evident from Figure 5.11. An alternative approach which will limit the time spent in BOOTUP, is to make the duration spent searching for new neighbors...
Figure 5.11: Energy Consumption in 500 Super Frames

Figure 5.12: Message exchange behavior in Scenario 1.
inversely proportional to the number of neighbors as well. In this manner, even after $N_n$ neighbors are attached, a node may still spend some time in BOOTUP. This will enable the attachment of newly activated nodes possible well into the lifetime of the network. This approach is a refinement to the SMACS, and its performance will not be discussed further here.

The increase in the lower region of the curves in Figure 5.13, which is a closeup of Figure 5.11 indicates that link transmit power cannot be reduced arbitrarily. Apart from the fact that with a fixed and low power level, the network may not become connected, the data indicates that before this hard limit is reached, as transmit power is reduced, it becomes harder to have successful handshakes in the network, as shown in Figure 5.12. We see that for a given network, for both Scenarios, there is an optimum transmit power level, which will achieve the lowest possible consumed energy levels. However this value is a function of node density and channel parameters, and may not be known prior to network deployment.

5.6.3 Variable Transmit Power levels

It is clear that we need power control on individual links in the network. There are two possible approaches here. One is to connect the network at some fixed transmit level, and then after links are established, use closed loop schemes to lower the transmit levels on individual links, or use distributed power control schemes similar to those used in cellular systems. The second approach is to use a very simple open loop method of assignment of power levels to links, during the operation of SMACS protocol. A rudimentary scheme which was used in our networks is as follows: Each node, upon wakeup, starts to engage in BOOTUP at some lowest transmit level. If after certain number of Super Frames it has
Figure 5.13: Energy consumption as transmit power level changes.

not found any neighbors, it will use the next higher transmit level, and so on. If the nodes has found some neighbors, and it is after \( POWER - CYCLE Super Frames \), then the node will also start cycling through its power levels to find far away nodes. On the other hand if a node receives a \( TYPE1 \) message from an unattached node, the receiver will adjust its power level to that of the transmitter (the transmit power level is included in the body of the incoming \( TYPE1 \) message).

The average short term and long term behavior of the SMACS algorithm was measured for networks of 18, 45, 150, and 400 nodes under fixed and variable power levels. In these experiments, the radio consumes 98 mW whenever it is turned on. This number is comparable to a typical Bluetooth radio power consumption. In addition, it will use an additional incremental level \( \delta_p \). The value of \( \delta_p \) is a function of the output transmit power. The \( \delta_p \) represent the
Table 5.1: Values of $\delta_p$ for various transmit power levels.

<table>
<thead>
<tr>
<th>$P_{\text{transmit}}$ (mW)</th>
<th>$\delta_p$ (mW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>6.7</td>
</tr>
<tr>
<td>3</td>
<td>30.0</td>
</tr>
<tr>
<td>10</td>
<td>66.7</td>
</tr>
</tbody>
</table>

power consumption at the RF front end. The values used for $\delta_p$ are given in Table 5.1. The power consumption for transmission is then $(98 + \delta_p)$ mW. The network statistics were gathered at two points in time for each network: first at the time the network becomes connected, and then after 500 SUPER FRAMES are elapsed. We measure the average length of time a node is turned on, the average transmit power level for the variable power case, the length of time it takes to connect the network, and average energy used per node. These values are depicted in the following figures. Figure 5.14 gives the average time it takes until the network is connected. In Figure 5.15, the average duration of radio on time, in lengths of SUPER FRAMES, is given for fixed and variable power scenarios. Figure 5.16 gives the average consumed energy until network becomes connected. On this plot, the amount of energy which would be consumed, if we used the classical Linked Clustering Algorithm (LCA), to self-organize the network is also given. The energy consumtopn of LCA is calculated, assuming the packet lengths for LCA are the same as a TYPE3 message, and that a single round of LCA is sufficient to form the network. Radios are always in receive mode for LCA, unless they transmit a message. It can be seen the level of energy savings
Figure 5.14: Time until the network becomes connected.

SMACS will afford, compared to LCA. Furthermore, the SMACS algorithm has the added benefit that it does not require a global time reference to be established before the algorithm is run, unlike the LCA. Also, we do not need to have any information about the network size for SMACS.

We also see that there is clearly an optimum average transmit power level, which brings down the consumed energy required to connect the network. Further, the variable power level scheme is able to bring down the actual consumed energy. So, for the short term, it makes sense to use variable powers. The penalty for using variable levels, is increased time until the network becomes connected, as is shown in Figure 5.14, a penalty which is most likely tolerable in sensor networking environments.

The effect of having variable power levels on the long run energy consumption, is given in Figure 5.17. In this scheme, each node stops searching for new nodes,
Figure 5.15: Average length of time radio is turned on, until network is connected.

once it has found 5 neighbors. We see that, in the long run, the variable power scheme builds a network which consumes the least amount of energy. This is due to the fact that the variable power scheme builds a network with links which use the smallest transmit power levels. Over repeated link usage, the power savings will add up. Therefore, although it may take longer to build the network, if we use variable power levels, in the long run, it is worth the effort, to do so. Another important factor is that, for a randomly deployed network, the node density, and therefore the optimal link transmit power levels are not known, and in this case, the only intelligent solution is to use a variable power scheme.

5.6.4 Effect of Number of Channels on Performance

Networks of 150 nodes were investigated for the effect of the number of available channels on the performance of the system. All the performance indicators were measured for 5000 different runs of the SMACS. The average of results of the
simulation are given the Table 5.2. All measures of performance improve with increasing number of channels. The most pronounced improvement is with the time it takes to connect the network.

5.7 Conclusion and Future Work

Both the SMACS and MSB procedures are scalable schemes, which enable building of a network infrastructure for our sensor nodes. The MSB algorithm may be described qualitatively as follows. The protocol attempts to build a more hierarchical topology, by means of assigning, at random, to some nodes the responsibility of being a \textit{MASTER} node. These nodes then will search and find neighbors, and attach them to form a local star network. The star networks are then attached together, when a \textit{SLAVE} of a \textit{MASTER} declares itself to be a \textit{MASTER} and
Figure 5.17: Energy consumed in 500 SUPER FRAMES.

attaches two distinct star networks of which it is a member.

The SMACS protocol, on the other hand, builds a flat topology. In this scheme, a node finds neighbors one at a time, and once a neighbor is found, it is attached immediately. This method may take longer to build (connect all the nodes in the network), compared to MSB, but it uses less energy to do so.

The self-organizing schemes were implemented in a simulation environment written in PARSEC. It was determined that a variable transmit power scheme is necessary in order to reduce short term and long term energy consumption. The SMACS scheme is able to form a network in a scalable fashion, as compared to the LCA. In order to conserve energy, the self-organization mechanism must employ some form of limiting behavior, to reduce its duty cycle as the network ages, or as enough neighbors are found for each node.

We have demonstrated in simulation, that it is possible to form an ad-hoc
Table 5.2: Performance as number of channels changes

<table>
<thead>
<tr>
<th>Frequency Count (Number of Channels)</th>
<th>50</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stop Time (FRAMES)</td>
<td>13.12</td>
<td>16.92</td>
</tr>
<tr>
<td>Time Radio On (FRAMES)</td>
<td>2.07</td>
<td>2.54</td>
</tr>
<tr>
<td>Consumed Energy (J)</td>
<td>0.82</td>
<td>1.00</td>
</tr>
<tr>
<td>Link Transmit Power (mW)</td>
<td>1.27</td>
<td>1.33</td>
</tr>
<tr>
<td>Number of Neighbors</td>
<td>3.02</td>
<td>3.03</td>
</tr>
<tr>
<td>Percent of Nets Connecting</td>
<td>75.5</td>
<td>74.1</td>
</tr>
</tbody>
</table>

infrastructure for sensor networks, without the need for prior time synchronization, information about the network size, and network topology. The variable power SMACS presents the most number of advantages as a suitable choice for self-organization at the link layer.

Future work on this topic includes investigation of the effect of a particular link layer self-organization scheme on the overall performance of the sensor network, by simulating the joint performance of the system with an appropriate routing mechanism. This measurement may be done under different traffic scenarios. This requires development of suitable physical target and event models, which will then translate into network traffic models.

It is also of great value if we are to develop a method for determining a link topology and its associated link transmit power levels, which will minimize the average energy consumed per node. This “minimum energy” method may use
global information, and could be either a centralized or distributed algorithm, and its output will be used as a performance benchmark for, say, comparing various energy conscious infrastructure building algorithms.
Chapter 6

Conclusion

The fact that path loss varies with the fourth power of the inverse transmitter-receiver distances for low lying antennas has many significant impacts on the design choices one will make for wireless sensor networks.

Based on our measurements we found that the fourth power path loss, is prevalent mostly in outdoor situations, and that the onset of the this phenomenon is at very small distances. The path loss characteristics, indicate that many small hops, in general, are more energy efficient in moving bits around the network, compared to having fewer but longer distance hops. This in turn had implications as to the need for power control on the links themselves. In other words, it would be best to use the lowest possible transmit power level of the radio to search for neighbors and build an infrastructure. However, in order to make sure the network actually becomes connected, higher transmit levels must also be used. We found that using a very simple power control scheme, which involved cycling through all possible transmit power levels periodically, resulted in good energy savings, particularly in the long run.
We also found out that building a flat topology, may be more energy efficient compared to a hierarchical one. However, further studies, which will combine the joint energy consumption of routing algorithms with link layer design must be made, to determine the best solution. It is highly likely that, when routing issues are also considered, the impact of the traffic type, and nature of observed phenomena, will also have an impact on the overall energy consumption characteristics.

Finally, in studying the frequency hopping issues, we found out that it is possible, in principle to maintain code synchronism, for fairly long periods (tens of thousands of frames), if we are able to keep the multiple access interference levels low in the network. The effective node density in the network has a great bearing in this respect. It was again concluded that, by reducing the transmit power levels, and hence, reducing the effective node density in the network, better maintenance of code phase is possible.

In short, we have seen that it is possible to build an ad-hoc wireless sensor network, without having any prior information about number of nodes involved, their time references, and their locations. The self-organizing schemes which were developed were highly scalable and able to form the network in a distributed manner.
Appendices
Appendix A

Some Number Theoretic Definitions

The following is a short list of some required definitions and facts. They may be found in any text dealing with cryptography, such as [43]

List of definitions

1. If \( n \) is an integer, then \( \mathbb{Z}_n^* = \{ x \in \{0, 1, 2, \ldots, n-1 \} \mid \gcd(x, n) = 1 \} \)

2. \( a \in \mathbb{Z}_n^* \) is a quadratic residue modulo \( n \) when \( \exists x \ni x^2 \equiv a \mod n \). If \( a \in \mathbb{Z}_n^* \) and \( a \) is not a quadratic residue, then it is called a quadratic non-residue modulo \( n \).

3. For \( p \) prime and \( 0 < a < p \) the Legendre symbol is defined as:

\[
L(a, p) = \begin{cases} 
-1, & a \text{ not a quadratic residue} \\
1, & a \text{ a quadratic residue} 
\end{cases}
\]  \hfill (A.1)

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4. For $N \equiv pq$, where $p$ and $q$ are primes, the Jacobi symbol is defined as

$$J(a, N) = \begin{cases} 
  0, & \text{if } a \text{ divides either } p \text{ or } q \\
  L(a, p)L(a, q), & \text{otherwise}
\end{cases}$$

(A.2)

5. Let $N \equiv pq$, and $p$ and $q$ primes, and both congruent to 3 modulo 4. Then $N$ is a Blum integer.

6. A one-way function is defined as a function $f$ such that for every $x$ in the domain of $f$, $f(x)$ is easy to compute; but for virtually all $y$ in the range of $f$, it is computationally infeasible to find an $x$ such that $y = f(x)$.

7. A trapdoor one-way function is defined as a one-way function, $f_z$, such that given $z$ it is easy to find algorithms $E_z$ and $D_z$ that compute $f_x(x)$ and $f_z^{-1}(y)$. In this case the algorithm $D_z$ is the trapdoor function, which is kept secret, and is known only by the agent authorized to invert $f_x(x)$. Note that it is still infeasible to calculate $f_z^{-1}(y)$, even with knowledge of $E_z$.

List of some relevant facts

1. For $N \equiv pq$, $p$ and $q$ prime, and $z \in \mathbb{Z}_n^*$, define $z_p = z \mod p$ and $z_q = z \mod q$, then $z$ is a quadratic residue mod $N$ iff $L(z_p, p) = 1$ and $L(z_q, q) = 1$.

2. For $N \equiv pq$, $p$ and $q$ prime, $|\mathbb{Z}_n^*| = (p - 1)(q - 1)$. Of all the members of $\mathbb{Z}_n^*$, only one-half have Jacobi symbol equal to one. Of these, only one-half are quadratic residues mod $N$.

3. If the factorization of $N$ is unknown, and for $z \in \mathbb{Z}_n^*$ we know $J(z, N) = 1$. Then it is not possible to determine whether $z$ is a quadratic residue or not.
in polynomial time. This is called the Quadratic Residuancy Determination problem.

4. If \( N \) is a Blum integer and \( z_0 \) is a quadratic residue mod \( N \), then \( \forall i > 0, z_i = z_{i-1}^2 \mod N \).
Appendix B

Marker Tone Locations Are Almost Independent

The distribution of marker tones in a SUPER FRAME, once it is determined, remains fixed for a node. We represent the SUPER FRAME by a line interval $I_1$ of length $T_{FRAME}$. Marker tones are represented as intervals of length $\tau_m$. The $i^{th}$ marker tone starts at $b_i$, $i = 1, 2, \cdots, L$. Distinct marker tones may not overlap in time.

Each marker tone’s start time, $b_i$, is a random variable. We would like to determine the join distribution of marker tone locations for a single node. The distribution is represented by $\varphi(b_1, b_2, \cdots, b_L)$.

We define $B_i$ to be the collection of points in the SUPER FRAME which are blocked as choices for $b_i$, and $I_i$ as $T_{frame} - B_i$. The set $I_i$ will be the union of a finite number of disjoint line intervals all inside $I_1$. We define $\Lambda_i = \text{length}(I_i)$. The sequence of $\Lambda_i$ is a decreasing sequence.

Tone locations are determined according to the following procedure:
• The location of the first tone, \( b_1 \) is chosen randomly in the interval \( I_1 \).

• Given \( \{b_1, b_2, \cdots, b_{i-1}\} \), \( b_i \) is chosen uniformly from the points in \( I_i \).

• Stop after \( b_L \) is determined.

For \( i > 1 \) we have the following:

\[
\Lambda_1 - (i - 1)(2\tau_m - \epsilon) \leq \Lambda_i \leq \Lambda_1 - i\tau_m + \epsilon \tag{B.1}
\]

The upper limit corresponds to the case when all the previous tones are placed next to each other contiguously, and the lower limit corresponds to the case when all previous tones were placed with exactly \((\tau_m - \epsilon)\) separation between them, where \( \epsilon \) is an positive and arbitrarily small real number. Then we may write the distribution of \( b_i \) conditioned on the past marker locations as:

\[
\varphi(b_i/b_{i-1}, \cdots, b_1) = \frac{1}{\Lambda_i} \quad \tag{B.2}
\]

Then we have

\[
\varphi(b_i, \cdots, b_2, b_1) = \varphi(b_i/b_{i-1}, \cdots, b_1)\varphi(b_{i-1}/b_{i-2}, \cdots, b_1) \cdots \varphi(b_2/b_1)\varphi(b_1) \\
= \frac{1}{\Lambda_i} \cdot \frac{1}{\Lambda_{i-1}} \cdots \frac{1}{\Lambda_2} \cdot \frac{1}{\Lambda_1} \quad \tag{B.3}
\]

Using the upper and lower bounds of B.1, we may bound the joint distribution as

\[
\frac{1}{T_{frame}} \prod_{i=2}^{L} \frac{1}{T_{frame} - i\tau_m + \epsilon} \leq \varphi(b_i, \cdots, b_2, b_1) \leq \frac{1}{T_{frame}} \prod_{i=2}^{L} \frac{1}{T_{frame} - (i - 1)(2\tau_m - \epsilon)} \tag{B.4}
\]

If we have

\[
2(L - 1)\tau_m << T_{frame} \quad \tag{B.5}
\]
and let \( \epsilon = 0 \) then the upper and lower bounds of B.4 may both be approximated by \( \frac{1}{T_{frame}} \) and we will have:

\[
\varphi(b_k, \cdots, b_2, b_1) \approx \frac{1}{T_{frame}} \tag{B.6}
\]

This indicates that we may model the process of assignment of marker tones in the SUPER FRAME as a sequence of \( L \) independent marker tone assignments, where the location of each tone is independently and uniformly chosen over the entire SUPER FRAME. Note that the condition of B.5 implies that total interval covered by all the marker tones must occupy a very small fraction of the SUPER FRAME length in order for the independence arguments of this Appendix to hold. This requires the marker tone duration to be short and the length of the marker word, \( L \), small.
Bibliography


