

## Corrigendum

## Corrigendum to “Hierarchical trajectory refinement for a class of nonlinear systems” [Automatica 41(4) (2005) 701–708]

Paulo Tabuada<sup>a,\*</sup>, George J. Pappas<sup>b</sup><sup>a</sup>Department of Electrical Engineering, University of Notre Dame, Notre Dame, IN 46556, USA<sup>b</sup>Department of Electrical and Systems Engineering, University of Pennsylvania, Philadelphia, PA 19104, USA

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It was recently brought to our attention by Dr. Mario Sigalotti that Theorem 3.2 in Tabuada and Pappas (2005) does not hold under the stated assumptions. In particular, the following example presented by Dr. Mario Sigalotti contradicts Corollary 3.3.

Let  $r = k = 1$ ,  $X_M^0(y, z) = \arctan(z)\partial/\partial y$ ,  $X_M^1(y, z) = \partial/\partial z$ ,  $\phi(y, z) = y$ . It is easy to check that A.I, A.II, A.III, and (3.4) hold true. Using (2.3) we get  $F_N(y, (\alpha, \beta, \gamma)) = \beta$ . Therefore, every smooth trajectory  $y(\cdot)$  in  $\mathbb{R}$  should be a solution of  $\Sigma_N$ . If  $|\dot{y}(t)| > \pi/2$  for some  $t \in \mathbb{R}$ , however, then  $y(\cdot)$  cannot be refined to a trajectory of  $\Sigma_M$ .

The problem lies in Lemma 3.1 which does not hold under the stated assumptions. However, it does hold under the stronger assumption

$$[\ker(T\phi), [\ker(T\phi), \mathcal{A}_M]] \subseteq \ker(T\phi) \quad (1)$$

that should replace A.II. Similarly, Corollary 3.3 requires the stronger assumption

$$[\ker(T\phi), \Delta_M^1] \subseteq \ker(T\phi) \quad (2)$$

that should replace (3.4). Note that the previous example does not satisfy (1) since

$$[\ker(T\phi), [\ker(T\phi), X_M^0]] = \text{span} \left\{ -\frac{2z}{(1+z^2)^2} \frac{\partial}{\partial y} \right\} \notin \ker(T\phi) = \text{span} \left\{ \frac{\partial}{\partial z} \right\}. \quad (3)$$

**Reference**

Tabuada, P., & Pappas, G. (2005). Hierarchical trajectory generation for a class of nonlinear systems. *Automatica*, 41(4), 701–708.

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\* Corresponding author.

E-mail addresses: [ptabuada@nd.edu](mailto:ptabuada@nd.edu), [tabuadap@seas.upenn.edu](mailto:tabuadap@seas.upenn.edu) (P. Tabuada), [pappasg@ee.upenn.edu](mailto:pappasg@ee.upenn.edu) (G.J. Pappas).