Microcalorimetry electrothermal impedance spectroscopy (ETIS) informs entropy evolution at individual electrodes of PNb$_9$O$_{25}$ or TiNb$_2$O$_7$ battery cells

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ABSTRACT

This study proposes a novel and fast microcalorimetry electrothermal impedance spectroscopy (ETIS) method based on heat generation rate measurements at each electrode of a lithium-ion battery cell. This new method is capable of retrieving the open-circuit voltage, the entropic potential, and the partial entropy changes at each electrode from measurements at a single temperature. It also shortens the measurement duration to a few hours compared to several days using the galvanostatic intermittent titration technique (GITT). The method consists of imposing a sinusoidal current on the cell assembled in an operando isothermal calorimeter. The induced sinusoidal potential response is used to calculate the open-circuit voltage of the cell as a function of the state of charge. The measured heat generation rates are analyzed by fast Fourier transform to determine not only the entropic potential of the cell but also the partial entropy changes at each electrode. This novel microcalorimetry ETIS method was first validated with numerical simulations. Then, it was experimentally demonstrated on battery cells consisting of PNb$_9$O$_{25}$ or TiNb$_2$O$_7$ working electrodes and metallic lithium counter electrodes in 1 M LiPF$_6$ in EC:DMC 1:1 v/v electrolyte. The results of the open-circuit voltage and the normalized entropic potential matched those previously determined by potentiometric entropy measurements based on GITT measurements at different temperatures. Furthermore, while the normalized partial entropy changes exhibited notable features at the PNb$_9$O$_{25}$ or TiNb$_2$O$_7$ working electrodes, they varied little at the metallic lithium counter electrodes.

1. Introduction

The global transition towards renewable energy and the widespread electrification of everything has led to significant interest in electrical energy storage systems including lithium-ion batteries (LIBs) [1–6]. Over the past decades, efforts have focused on discovering new cathode and anode materials with large capacity and long cycle life, among other attributes. Simultaneously, electrochemical methods of analysis have been developed to gain insight into their charging and discharging mechanisms.

The entropic potential $\partial U_{O\!C\!V}/\partial T$ of a battery cell is defined as the derivative of the cell open-circuit voltage $U_{O\!C\!V}$ with respect to temperature $T$ as a function of the state of charge. Both $U_{O\!C\!V}$ and $\partial U_{O\!C\!V}/\partial T$ relate to thermodynamic properties whose measurement can provide insight into the charging mechanisms of LIBs and the reversible heat generation rate during cycling [7]. Multiple approaches have been proposed to measure the entropic potential of LIBs [8–16]. It can be determined by performing galvanostatic intermittent titration technique (GITT) at different temperatures. However, such measurements are time-consuming and usually require hundreds of hours for a single lithiation/delithiation cycle. Alternatively, the electrothermal impedance spectroscopy (ETIS) technique - first proposed by Schmidt

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et al. [17] and subsequently advanced by Hu et al. [18,19] - is capable of measuring the entropic potential of LIBs within only a few hours for one lithiation/delithiation cycle. However, these techniques use measurement apparatus that require substantial temperature changes and/or heat generation to produce accurate results. Therefore, so far they have been demonstrated only with commercial cylindrical and pouch cells with mass loadings on the order of grams. However, in laboratory settings it is more practical to synthesize electrodes with mass loadings on the order of milligrams of LIB materials [20–22]. Moreover, previous studies primarily focused on the entropic potential of the entire battery cell. However, the partial entropy changes at each electrode is also of interest, as they can uncover the thermodynamics behavior of the anode and cathode materials separately.

This study presents a novel microcalorimetry ETIS measurement method to rapidly determine the open-circuit voltage \( U_{\text{OCT}} \), the entropic potential \( \partial U_{\text{OCT}} / \partial T \), and the partial entropy changes at each electrode of a battery cell. This new method uses an operando isothermal calorimeter capable of measuring the instantaneous heat generation rates at individual electrodes with small mass loadings. After validating the method using numerical simulations, it was demonstrated experimentally with PNBzO\(_2\) or TiNbO\(_2\) battery cells with metallic Li counter electrode in organic electrolyte assembled in the calorimeter.

2. Background

2.1. Potentiometric entropy measurements

Potentiometric entropy measurements consist of determining the open-circuit voltage \( U_{\text{OCT}}(x,T) \) and the entropic potential \( \partial U_{\text{OCT}} / \partial T \) of a battery cell at a given temperature \( T \) and pressure as functions of lithium composition \( x \), specific capacity \( C_{\text{sp}} \), or state of charge. Our previous study [7] has not only described the fundamental relationships between \( U_{\text{OCT}}(x,T) \), \( \partial U_{\text{OCT}} / \partial T \), and the material thermodynamic properties, but also developed an interpretation guide of their measurements for LIBs. In brief, the open-circuit voltage \( U_{\text{OCT}}(x,T) \) of a battery cell with an intercalation compound (denoted by MA) working electrode and a metallic lithium (denoted by Li) counter electrode can be expressed as [7,23],

\[
U_{\text{OCT}}(x,T) = -\frac{1}{e} \frac{\partial s_{\text{MA}}(x,T)}{\partial x} - \frac{\partial s_{\text{Li}}(x,T)}{\partial x}
\]

where \( e \) is the elementary charge, \( s_{\text{MA}}(x,T) \) is the Gibbs free energy of Li\(_2\)MA per unit of MA, and \( s_{\text{Li}}(x,T) \) is the Gibbs free energy per unit of metallic lithium. Similarly, the entropic potential \( \partial U_{\text{OCT}} / \partial T \) can be expressed as [7,24],

\[
\frac{\partial U_{\text{OCT}}}{\partial T}(x,T) = \frac{1}{e} \frac{\partial s_{\text{MA}}(x,T)}{\partial x} - \frac{\partial s_{\text{Li}}(x,T)}{\partial x}
\]

where \( s_{\text{MA}}(x,T) \) is the entropy of Li\(_2\)MA per unit of MA and \( s_{\text{Li}}(x,T) \) is the entropy per unit of metallic lithium. As such, \( \partial s_{\text{MA}} / \partial x(x,T) \) and \( -\partial s_{\text{Li}} / \partial x(x,T) \) can be regarded as the respective partial entropy changes at each electrode. Furthermore, the counter electrode consists of macroscopic metallic lithium with negligible surface energy effects [25]. Thus, \( \partial s_{\text{Li}} / \partial x(x,T) \) corresponds to the standard Gibbs free energy per unit of metallic lithium \( s_{\text{Li}}(T) \), and \( -\partial s_{\text{Li}} / \partial x(x,T) \) is equal to the standard entropy per unit of metallic lithium \( -s_{\text{Li}}(T) \). Both \( s_{\text{Li}}(T) \) and \( -s_{\text{Li}}(T) \) are independent of \( x \). Finally, the evolution of \( U_{\text{OCT}}(x,T) \) and \( \partial U_{\text{OCT}} / \partial T(x,T) \) during lithiation can provide insight into the charging mechanisms of the battery cell such as lithium ion insertion in a homogeneous solid solution, two-phase coexistence, phase transition, and intralayer lithium ion ordering [7].

Potentiometric entropy measurements consist of imposing a series of constant current pulses on the battery cell at constant temperature similar to GITT [27–29]. However, each current pulse is followed by a relaxation period during which a step-like temperature profile with four temperature plateaus is applied to the battery cell. Simultaneously, the corresponding potential evolution of the battery cell is recorded by a high accuracy potentiostat. As such, the open-circuit voltage \( U_{\text{OCT}}(x,T) \) can be retrieved from the measured potential at the end of the relaxation period. Furthermore, the entropic potential \( \partial U_{\text{OCT}} / \partial T(x,T) \) can be calculated by taking the finite difference of the potential in response to each temperature step and averaging over the four instances. This method has been demonstrated to accurately measure the open-circuit voltage \( U_{\text{OCT}}(x,T) \) and the entropic potential \( \partial U_{\text{OCT}} / \partial T(x,T) \) of coin cells with metallic lithium counter electrodes and working electrodes made of intercalation compounds such as graphite [7], LiCoO\(_2\) [7], LiFePO\(_4\) [7], TiNbO\(_2\) [27], PNBzO\(_2\) [28], Ti,Nb,O\(_2\) [29], LiSiMoO\(_4\) [22], and MoO\(_2\) [21]. However, it requires long relaxation periods to ensure that the battery cell has reached thermodynamic equilibrium before collecting data for each lithium composition \( x \) at each temperature \( T \). In fact, the total measurement time for one lithiation/delithiation cycle of a coin cell usually ranges between 200 and 400 h [27–29]. Such durations are prohibitively long and faster alternative methods capable of providing meaningful information would be highly desirable.

2.2. Operando isothermal calorimetry

Heat generation arises from multiple physicochemical phenomena occurring inside electrochemical energy storage systems during operation [30]. Therefore, accurate estimations of heat generation are essential in designing effective thermal management strategies to prevent potential fire hazards such as thermal runaway [31]. Accordingly, various calorimetric techniques have been developed to measure the heat generation in batteries including accelerating rate calorimetry [31,32], differential scanning calorimetry [33,34], and isothermal calorimetry [30]. In particular, several isothermal calorimetric studies have reported heat generation rates in coin cells [30,34], cylindrical cells [35], Swagelok cells [33], and prismatic cells [31] under galvanostatic cycling. However, they measured the heat generation rate for the entire cell. To overcome this limitation, Munteshwar et al. [36] developed and validated experimentally an operando isothermal calorimeter capable of measuring the instantaneous heat generation rates at each electrode. Subsequently, the device has been used to measure heat generation rates at each electrode of electric double layer capacitors [36–41], hybrid pseudocapacitors [42,43], and LIBs [27–29]. The measurements revealed the thermal signatures associated with physical, chemical, and transport processes including resistive losses [27–29,38,43], entropic changes [28,29], ion adsorption/desorption [38–43], ion solvation/desolvation [28,43], enthalpy of mixing [27,28], electrolyte decomposition [40,41,43], overscreening effect [37,41], and insulator to metal transition [27,28].

2.3. Fast Fourier transform (FFT)

Fast Fourier transform (FFT) is an algorithm computing the discrete Fourier transform of a sequence and converting it from time domain to frequency domain [44]. It is an effective tool to reveal any periodically oscillating feature within a signal which may not be obvious from its temporal evolution. For example, let us consider a signal which can be represented by the function \( f(t) \) over time \( t \) such that,

\[
f(t) = A_0 + A_1 \cos (2\pi f_1 t + \phi_1) + A_2 \cos (2\pi f_2 t + \phi_2) + \ldots
\]

By applying FFT to \( f(t) \), the amplitudes \( (A_1, A_2, \ldots) \), frequencies \( (f_1, f_2, \ldots) \), and phase angles \( (\phi_1, \phi_2, \ldots) \) of every sinusoidal term can be identified. Note that the phase angle given by FFT has a range between \(-\pi \) and \( \pi \).
2.4. Electrothermal impedance spectroscopy (ETIS)

Previously, multiple characterization techniques have been developed to enable the simultaneous analysis of both electrochemical and thermal behavior of electrical energy storage systems. For example, Hess et al. [45] designed an in situ simultaneous thermal analysis (STA) cell for electric double layer capacitors. This technique monitors the change in heat flow, mass loss, resistance, and capacitance within electric double layer capacitors during operation. It was employed to investigate the impact of operating voltage and temperature on the cycling degradation of electric double-layer capacitors and on the associated thermal processes occurring within the devices [45–47]. Similarly for LIBs, Schmidt et al. [17] first proposed ETIS as an alternative to the time-consuming potentiometric entropy measurements based on GITT. The ETIS method consists of imposing on a battery cell a current \( i(t) \) with a very small constant offset \( I_0 \) and a sinusoidal oscillation with amplitude \( A_1 \) at frequency \( f_1 \), i.e.,

\[
i(t) = I_0 + I_1 \sin(2\pi f_1 t).
\]

Note that \( I_0 \) is small enough to be negligible compared to \( I_1 \), i.e., \( |I_0| \ll |I_1| \). Under such conditions, the irreversible Joule heating \( Q_J(t) \) can be expressed as [17],

\[
Q_J(t) = I(t)^2 R \approx \frac{I_1^2}{2} \cos(4\pi f_1 t) + \frac{I_1^2}{2} R
\]

where \( R \) is the internal resistance of the battery cell. Similarly, the reversible entropic heat generation rate \( Q_{rev}(t) \) can be written as [17],

\[
Q_{rev}(t) = I(t)\frac{\partial U_{OCV}}{\partial T}(x, T) \approx I_1 T_m \frac{\partial U_{OCV}}{\partial T}(x, T) \sin(2\pi f_1 t)
\]

where \( T_m \) is the measured cell temperature averaged over the sinusoidal period.

The measured instantaneous temperature response \( T_{cell}(t) \) of the battery cell can be expressed as [17],

\[
T_{cell}(t) = T_{amb} + \Delta T_J(t) + \Delta T_{rev}(t)
\]

where \( T_{amb} \) is the ambient temperature (assumed to be constant) while \( \Delta T_J(t) \) and \( \Delta T_{rev}(t) \) are the cell temperature changes due to irreversible Joule heating and reversible entropic heat generation, respectively. The thermal impedance \( Z_{th}(f) \) (in K/W) of a battery cell at frequency \( f \) can be defined as,

\[
Z_{th}(f) = \frac{T_{cell}(f) - T_{amb}(f)}{\frac{\partial U_{OCV}}{\partial T}(x, T) \sin(2\pi f_1 t + \phi_{Z_{th}}(2f_1))}
\]

where \( \Delta T_J(t) = \frac{I_1^2}{2} R \left| Z_{th}(2f_1) \right| \sin(4\pi f_1 t + \phi_{Z_{th}}(2f_1)) \right) \]

and \( \Delta T_{rev}(t) = I_1 T_m \frac{\partial U_{OCV}}{\partial T}(x, T) |Z_{th}(f_1)| \sin(2\pi f_1 t + \phi_{Z_{th}}(f_1)) \right) \]

As a result, the internal resistance \( R \) can be retrieved from the FFT output \( A_T(2f_1) \), as,

\[
R = \frac{2}{I_1^2 |Z_{th}(2f_1)|} A_T(2f_1).
\]

Similarly, the entropic potential \( \frac{\partial U_{OCV}}{\partial T}(x, T) \) can be obtained from the FFT output \( A_F(f_1) \), as,

\[
\frac{\partial U_{OCV}}{\partial T}(x, T) = \frac{1}{I_1 T_m |Z_{th}(f_1)|} A_F(f_1).
\]

To obtain the thermal impedance magnitudes \( |Z_{th}(2f_1)| \) and \( |Z_{th}(f_1)| \), the following procedure was suggested [17]. First, the entropic potential of the battery cell at a given state of charge (SOC) is predetermined by potentiometric entropy measurements based on GITT at four different temperatures. Then, the battery cell is set to this SOC and excited with a sinusoidal current at frequency \( 2f_1 \). As the entropic potential at this SOC is known, the reversible entropic heat generation rate \( Q_{rev}(t) \) can be calculated using Eq. (6). Simultaneously, the instantaneous temperature response \( T_{cell}(t) \) of the battery cell is measured. Subsequently, both the measured \( T_{cell}(t) \) and the calculated \( Q_{rev}(t) \) are analyzed by FFT. This identifies the amplitudes of the sinusoidal oscillations at frequency \( 2f_1 \) within \( T_{cell}(t) \) and \( Q_{rev}(t) \). Finally, the thermal impedance magnitude \( |Z_{th}(2f_1)| \) arises as the ratio of these two amplitudes, i.e., \( |Z_{th}(2f_1)| = \frac{|T_{cell}(2f_1)|}{|Q_{rev}(2f_1)|} \). The same procedure is repeated at frequency \( f_1 \) to obtain the thermal impedance magnitude \( |Z_{th}(f_1)| \), i.e., \( |Z_{th}(f_1)| = \frac{|T_{cell}(f_1)|}{|Q_{rev}(f_1)|} \).

Overall, this method was successfully demonstrated on commercial cylindrical and pouch cells with capacities around 1 Ah [17]. The retrieved entropic potential \( \frac{\partial U_{OCV}}{\partial T}(x, T) \) agreed with that determined by potentiometric entropy measurements based on GITT, and the measurement duration was shortened from several days to a few hours [17]. Nevertheless, in practice this method becomes unnecessarily complicated because of the requirement to measure the temperature. First, accurate values of the thermal impedance magnitudes \( |Z_{th}(2f_1)| \) and \( |Z_{th}(f_1)| \) must be obtained. The thermal impedance serves as the only available relationship from the measured temperature response \( T_{cell}(t) \) back to the heat generation rates \( Q_J(t) \) and \( Q_{rev}(t) \) in the battery cell which are not directly measured. However, several studies have illustrated that the thermal impedance can vary substantially with minor changes in ambient temperature [48] and ambient relative humidity [49]. Thus, consistent conditions must be maintained for the duration of the experiment. For example, throughout their experiment, Schmidt et al. [17] placed the battery cell and mounted the temperature sensor in the same positions. Furthermore, the entire setup was housed in an incubator to ensure constant ambient temperature and ambient relative humidity. Moreover, the imposed sinusoidal current needs to have large amplitude (on the order of amperes) and low frequency (on the order of millihertz) to create temperature oscillations on the order of a few degrees Celsius which are detectable by conventional temperature sensors [17]. These criteria are challenging for battery cells with large thermal conductivity and/or large specific heat capacity, as a larger heat generation rate is required to induce sufficiently large temperature oscillations [48].

To address these drawbacks, Hu et al. [18,19] attempted to eliminate the step of retrieving the heat generation rate from the measured temperature response. Instead, they directly measured the total heat generation rate \( Q_T(t) \) using an isothermal calorimeter at temperature \( T_m \) [18,19]. The imposed current \( i(t) \) was given by Eq. (4) and \( Q_T(t) \) was expressed as the sum of \( Q_J(t) \) and \( Q_{rev}(t) \) given by Eqs. (5) and (6), respectively. Therefore, after applying FFT to the measured \( Q_T(t) \), they expressed the amplitude \( A_Q(2f_1) \) associated with the heat generation rate oscillation at frequency \( 2f_1 \) as,

\[
A_Q(2f_1) = \frac{I_1^2}{2} R |Z_{th}(2f_1)|
\]

and \( A_Q(f_1) \) at frequency \( f_1 \) as,

\[
A_Q(f_1) = I_1 T_m \frac{\partial U_{OCV}}{\partial T}(x, T).
\]
Then, the internal resistance \( R \) and the entropic potential \( \partial U_{\text{OCV}} / \partial T(x,T) \) can be retrieved from the FFT output \( A_g(2f_1) \) and \( A_g(f_1) \) as,

\[
R = \frac{2}{f_1^2} A_g(2f_1)
\]

(17)

\[
\frac{\partial U_{\text{OCV}}}{\partial T}(x,T) = \frac{1}{f_1 f_m} A_g(f_1).
\]

(18)

This modified ETIS method was successfully demonstrated on a commercial LMO-NMC/graphite pouch cell with a capacity of 25.9 Ah [18, 19]. The isothermal calorimeter measured the heat generation rate and retrieved the entropic potential of the entire pouch cell. It simplified the experimental procedure and improved the accuracy of the retrieved entropic potential and internal resistance [18,19]. However, the isothermal calorimeter had a maximum measurement error of 0.67 W and a response time of at least a few seconds [18,19]. Thus, its most appropriate application is for commercial pouch cells with mass loadings on the order of milligrams and fabricated in a laboratory setting. An isothermal calorimeter with considerably better sensitivity and shorter response time is necessary to capture the instantaneous heat generation rates on the order of microwatts [27–29]. For coin cells, an isothermal calorimeter with considerably better sensitivity and shorter response time is necessary to capture the instantaneous heat generation rate typically featuring rapid fluctuations of relatively small magnitudes [36]. In addition, measuring the heat generation rates at each electrode could be used to investigate their individual partial entropy changes. This could provide insight into the thermodynamics behavior of both anode and cathode and facilitate the selection of electrode pairs for full cells.

This study aims to develop a novel microcalorimetry ETIS measurement method to quickly determine the open-circuit voltage \( U_{\text{OCV}} \) and the entropic potential \( \partial U_{\text{OCV}} / \partial T \) of battery cells with electrode mass loadings on the order of milligrams and fabricated in a laboratory setting. This new method uses an operando isothermal calorimeter designed to measure the instantaneous heat generation rates on the order of microwatts at individual electrodes, making it the first method capable of investigating the partial entropy changes at each electrode during cycling.

3. Analysis

3.1. Imposed current

Fig. 1 shows the schematic of the new procedure developed to determine the open-circuit voltage \( U_{\text{OCV}}(x,T) \) and the entropic potential \( \partial U_{\text{OCV}} / \partial T \) of an LIB cell from microcalorimetry ETIS measurements. The apparatus consists of the operando isothermal calorimeter described in Ref. [36] and reproduced in Fig. 2 for the sake of completeness. Battery cells consisting of two bare electrodes cast on current collectors and two thick separators impregnated with electrolyte are assembled in the calorimeter and cycled using a high accuracy potentiostat. Instantaneous heat generation rates at individual electrodes are measured by thermoelectric heat flux sensors in thermal contact with the back of each electrode.

To complement previous studies [17–19], here we describe how to retrieve the open-circuit voltage from the measured cell potential and the entropic potential as well as the partial entropy changes at each electrode from the measured instantaneous heat generation rates. The technique starts by imposing a current \( I(t) \) consisting of a constant offset \( I_0 \) and a sinusoidal function oscillating with amplitude \( I_1 \) at frequency \( f_1 \), i.e.,

\[
I(t) = I_0 - I_1 \sin(2\pi f_1 t) = I_0 + I_1 \cos(2\pi f_1 t + \frac{\pi}{2}).
\]

(19)

As discussed in detail by Schmidt et al. [17], the choice of \( I_0, I_1, \) and \( f_1 \) is a compromise among several different considerations. Here, \( I_0 \) is negative which slowly but discontinuously discharges the battery cell.

Note also that \( I_0 \) should be negligible compared to \( I_1 \), i.e., \( |I_0| \ll |I_1| \). However, a large magnitude of \( I_0 \) results in faster discharging and thus quicker measurements. Similarly, \( I_1 \) should be large enough to ensure an adequate signal-to-noise ratio in the measured oscillating heat generation rates. However, a small \( I_1 \) is preferable as (i) it maximizes the proportion of reversible entropic heat generation \( Q_{\text{rev}}(t) \) compared to Joule heating \( Q_H(t) \) and (ii) it minimizes the sinusoidal variation in the lithium composition \( x \) over a period. In fact, every data point of the open-circuit voltage \( U_{\text{OCV}}(x,T) \) and the entropic potential \( \partial U_{\text{OCV}} / \partial T \) retrieved by microcalorimetry ETIS measurements is actually the time-average over a sinusoidal period of an oscillating variable function of \( x \). Therefore, this uncertainty can be alleviated by reducing the variation in \( x \), which in turn improves the resolution of the retrieved \( U_{\text{OCV}}(x,T) \) and \( \partial U_{\text{OCV}} / \partial T \). In addition, \( f_1 \) should be sufficiently large to acquire enough data points. Here also, a large frequency \( f_1 \) shortens the period of every sinusoid, reduces the variation in \( x \), and improves the resolution of the retrieved results. However, every period needs to last at least a few seconds to provide sufficient time for the periodically alternating redox reactions to occur within the battery cell. Finally, the phase angle of \( I(t) \) is chosen as \( \pi / 2 \) such that \( I(t) \approx 0 \) at \( t = 0 \) to avoid a sudden load on the potentiostat at the start of the measurements and (ii) \( I(t) \) is negative during the first half-period to avoid overcharging the battery cell when it already begins in fully charged (delithiated) state.

The elapsed time \( t \) (in s) can be converted into the lithium composition \( x \) in Li,MA such that,

\[
x(t) = -\frac{x_{\text{theo}} \Delta q(t)}{3600 m \text{C}_{\text{m,tho}}} = -\frac{x_{\text{theo}} \int_0^t I'(t') \, dt'}{3600 m \text{C}_{\text{m,tho}}}
\]

(20)

Here, \( \Delta q(t) \) (in mC) is the amount of charge transferred to the battery cell between times 0 and \( t \), \( I(t) \) (in mA) is the imposed current given by Eq. (19), \( m \) (in g) is the mass loading of active material MA, and \( C_{\text{m,tho}} \) (in mAh/g) is the theoretical specific capacity of the intercalation compound corresponding to the theoretical lithium composition \( x_{\text{theo}} \). For example, in the case of a Li,PNbO25 working electrode, \( C_{\text{m,tho}} = 190 \text{ mAh/g} \) assuming \( x_{\text{theo}} = 9 \) [28], while for a Li,TNbO3 working electrode, \( C_{\text{m,tho}} = 388 \text{ mAh/g} \) assuming \( x_{\text{theo}} = 5 \) [27].

3.2. Potential response and open-circuit voltage

Under the imposed current \( I(t) \) of Eq. (19) and assuming \( |I_0| \ll |I_1| \), the measured potential response \( V(t) \) can be expressed as,

\[
V(t) = U_{\text{OCV}}(x(T)) + I_1 |Z(f_1)| \cos 2\pi f_1 t + \frac{\pi}{2} + \phi_Z(f_1)
\]

(21)

Here, \( Z(f_1) \) (in \( \Omega \)) is the electrochemical impedance of the battery cell at frequency \( f_1 \). Note that \( Z(f_1) \) is a complex number such that \( Z(f_1) = Z_R(f_1) + iZ_I(f_1) \). Alternatively, \( Z(f_1) \) can be described by its magnitude \( |Z(f_1)| \) and phase difference \( \phi_Z(f_1) \), i.e., \( Z(f_1) = |Z(f_1)| \exp [i\phi_Z(f_1)] \) [50,51]. Accordingly, the open-circuit voltage \( U_{\text{OCV}}(x,t) \) at lithium composition \( x \) can be calculated by averaging the measured cell potential \( V(t) \) over a period such that,

\[
U_{\text{OCV}}(x,t) = \frac{1}{t_1 - t_0} \int_{t_0}^{t_1} V(t') \, dt'
\]

(22)

where \( t_1 = t_0 + t \) is the period of \( I(t) \) and time \( t \) falls within this period from \( (t-1) t_0 \) to \( t_1 t_0 \). In other words, \( U_{\text{OCV}}(x,T) \) is considered equal to \( U_{\text{OCV}}(x,T) \) for any lithium composition \( x \) between \( x_{t_0} \) and \( x_t \) such that,

\[
x_t = -\frac{x_{\text{theo}} \int_0^t I'(t') \, dt'}{3600 m \text{C}_{\text{m,tho}}}
\]

(23)
Fig. 1. Schematic of the procedure and experimental apparatus developed to determine the open-circuit voltage $U_{OCV}(x, T)$ and the entropic potential $\frac{\partial U_{OCV}}{\partial T}(x, T)$ of an LIB cell from the novel microcalorimetry ETIS measurements.

Fig. 2. Schematic of the operando isothermal calorimeter used in microcalorimetry ETIS measurements.
3.3. Heat generation rates

The total instantaneous heat generation rate $\dot{Q}_t(t)$ in a battery cell can be divided into several contributions including (i) Joule heating $\dot{Q}_J(t)$, (ii) reversible entropic heat generation $\dot{Q}_{rev}(t)$, (iii) enthalpy of mixing $\dot{Q}_{mix}(t)$, and (iv) heat generation due to side reactions $\dot{Q}_{r}(t)$, i.e. \[ \dot{Q}_t(t) = \dot{Q}_J(t) + \dot{Q}_{rev}(t) + \dot{Q}_{mix}(t) + \dot{Q}_{r}(t). \] (24)

The heat generation rate $\dot{Q}_J(t)$ associated with irreversible resistive losses can be expressed as \[ \dot{Q}_J(t) = I(t)[V(t) - U_{OCV}(x,T)]. \] (25)

Substituting $I(t)$ given by Eq. (19) (assuming $|I_0| \ll |I_1|$) and $V(t)$ given by Eq. (21) into Eq. (25) yields, \[ \dot{Q}_J(t) = I_1^2 \sum |Z(f_i)| \cos \left[ 4\pi f_i t + \pi + \phi_Z(f_i) \right] + I_2^2 |Z(f_i)| \cos \left[ \phi_Z(f_i) \right]. \] (26)

Similarly, the reversible heat generation rate $\dot{Q}_{rev}(t)$ due to entropic changes can be expressed as \[ \dot{Q}_{rev}(t) = I(t)T \frac{\partial U_{OCV}}{\partial T}(x,T). \] (27)

Here, $T$ is the temperature of the battery cell imposed to be constant during operando isothermal calorimetry. Although $\partial U_{OCV}/\partial T(x,T)$ is a real number, for the convenience of FFT analysis we describe it by its magnitude $|\partial U_{OCV}/\partial T(x,T)|$ and phase difference $\phi_{rev}$. Then, substituting $I(t)$ given by Eq. (19) into Eq. (27) and assuming $|I_0| \ll |I_1|$ yields, \[ \dot{Q}_{rev}(t) = I_1 T \left| \frac{\partial U_{OCV}}{\partial T}(x,T) \right| \cos \left( 2\pi f_i t + \frac{\pi}{2} + \phi_{rev} \right). \] (28)

Mathematically during discharging (lithiation) with negative $I(t)$, if $\phi_{rev} \approx 0$ then $|\partial U_{OCV}/\partial T(x,T)|$ is positive and $\dot{Q}_{rev}(t)$ is endothermic, or if $\phi_{rev} \approx \pi$ then $|\partial U_{OCV}/\partial T(x,T)|$ is negative and $\dot{Q}_{rev}(t)$ is exothermic.

Furthermore, $\dot{Q}_{mix}(t)$ can be defined as the sum of the reversible heat generation rates at the intercalation compound working electrode $\dot{Q}_{rev,M}(t)$ and at the metallic lithium counter electrode $\dot{Q}_{rev,L}(t)$ such that $\dot{Q}_{mix}(t) = \dot{Q}_{rev,M}(t) + \dot{Q}_{rev,L}(t)$ \[ \dot{Q}_{mix}(t) = \dot{Q}_{rev,M}(t) + \dot{Q}_{rev,L}(t) \] \[ \dot{Q}_{rev,M}(t) = \frac{I_1 T}{e} \left| \frac{\partial H_{MA}}{\partial x}(x,T) \right| \cos \left( 2\pi f_i t + \frac{\pi}{2} + \phi_{rev,MA} \right). \] (29)

Here also, the partial entropy change at the intercalation compound working electrode $|\partial H_{MA}/\partial x|/\partial x(x,T)$ is a real number that can be described by its magnitude $|\partial H_{MA}/\partial x|/\partial x(x,T)$ and its phase difference $\phi_{rev,MA}$. Similarly, $\dot{Q}_{rev,L}(t)$ can be written as, \[ \dot{Q}_{rev,L}(t) = -\frac{I_1 T}{e} \left| \frac{\partial H_{Li}}{\partial x}(x,T) \right| \cos \left( 2\pi f_i t + \frac{3\pi}{2} + \phi_{rev,LI} \right). \] (30)

Finally, $\dot{Q}_{r}(t)$ is the heat generation rate associated with the enthalpy of mixing caused by ion concentration gradients. Here, $\dot{Q}_{mix}(t)$ is related to the local values of the partial molar enthalpy and the concentration gradient of each ion species in the battery cell \[ \dot{Q}_{mix}(t) \] \[ \text{is negligible at low C-rates} \] \[ \text{as assumed in the present FFT analysis.} \]

Furthermore, the heat generation rate due to side reactions $\dot{Q}_{r}(t)$ is generally neglected unless the battery cell is operating under extreme conditions \[ \text{[30,52,54].} \]

3.4. Entropic potential and partial entropy changes

Substituting Eqs. (26) and (28) into Eq. (24) yields, \[ \dot{Q}_t(t) = A_{i}(0) + A_{i}(f_i)\cos \left[ 2\pi f_i t + \phi_i(f_i) \right] \] \[ + A_{i}(2f_i)\cos \left[ 4\pi f_i t + \phi_i(2f_i) \right] \] \[ \text{where the terms} \] \[ A_{i}(0), A_{i}(f_i), \text{and} \] \[ A_{i}(2f_i) \] \[ \text{are given by,} \] \[ A_{i}(0) = I_1^2 \frac{T}{2} |Z(f_i)| \cos \left( \phi_Z(f_i) \right). \] (32)

Applying FFT to the measured $\dot{Q}_t(t)$ during a given period from $(-1)\omega_i$ to $\omega_i$ yields the amplitude $A_{i}(f_i)$ of the sinusoidal oscillation at frequency $f_i$ given by Eq. (33) and the corresponding phase angle $\phi_i(f_i)$ expressed as, \[ \phi_i(f_i) = \frac{\pi}{2} + \phi_{rev} \] \[ \text{Thus, the entropic potential} \] \[ |U_{OCV}/\partial T(x,T)| \] \[ \text{at discrete lithium composition} \] \[ \text{can be written as,} \] \[ A_{i}(f_i) = \frac{I_1 T}{e} \left| \frac{\partial H_{MA}}{\partial x}(x,T) \right| \cos \left( \phi_{MA}(f_i) - \frac{\pi}{2} \right) \] \[ \text{while the phase angle} \] \[ \phi_{MA}(f_i) = \frac{\pi}{2} + \phi_{rev,MA}. \] (37)

Similarly, FFT can also be applied to the instantaneous heat generation rates $\dot{Q}_{MA}(t)$ measured at the intercalation compound working electrode and $\dot{Q}_L(t)$ measured at the metallic lithium counter electrode, both during the same period from $(-1)\omega_i$ to $\omega_i$. Applying FFT to $\dot{Q}_{MA}(t)$ given by Eq. (29) yields the amplitude $A_{MA}(f_i)$ of the sinusoidal oscillation at frequency $f_i$ expressed as, \[ A_{MA}(f_i) = \frac{I_1 T}{e} \left| \frac{\partial H_{MA}}{\partial x}(x,T) \right| \cos \left( \phi_{MA}(f_i) - \frac{\pi}{2} \right) \] \[ \text{Likewise, applying FFT to} \] \[ \dot{Q}_L(t) \] \[ \text{given by Eq. (30)} \] \[ \text{yields the amplitude} \] \[ A_{Li}(f_i) \] \[ \text{of the sinusoidal oscillation at frequency} \] \[ f_i \] \[ \text{expressed as,} \] \[ A_{Li}(f_i) = \frac{I_1 T}{e} \left| \frac{\partial H_{Li}}{\partial x}(x,T) \right| \cos \left( \phi_{Li}(f_i) - \frac{\pi}{2} \right) \] \[ \text{while the phase angle} \] \[ \phi_{Li}(f_i) = \frac{3\pi}{2} + \phi_{rev,LI}. \] (41)

Thus, the partial entropy change at the metallic lithium counter electrode $|\partial H_{Li}/\partial x|(x,T)$ at discrete lithium composition $x_i$ can be written as, \[ -\frac{\partial H_{Li}}{\partial x}(x_i,T) = -\frac{A_{Li}(f_i)e}{I_1 T} \cos \left( \phi_{Li}(f_i) - \frac{3\pi}{2} \right). \] (42)

4. Materials and methods

4.1. Synthesis of PbNi$_2$O$_{25}$ powder

To synthesize the PbNi$_2$O$_{25}$ powder, 0.9 mmol of PbO, 0.1 mol of Ni$_2$O$_3$ (Sigma Aldrich, 99.99%) and 0.2 mol of NH$_4$H$_2$PO$_4$ (Sigma Aldrich, 98%) powders were mixed. This mixture was ground with a pestle in an agate
mortar for 10 min to obtain a homogeneous powder. This powder was transferred into an alumina crucible and placed in a tube furnace with Ar flow at room temperature for 2 h to get rid of air. The furnace was first heated to 350 °C at 1 °C/min of ramp rate where it was maintained for 8 h with Ar flow. Then, the Ar flow was stopped and the furnace was heated to 1000 °C at 5 °C/min of ramp rate where it was maintained for 24 h. Finally, this sample was naturally cooled down to room temperature to obtain PnBnO₂₅ powder.

4.2. Synthesis of TiNb₂O₇ powder

To synthesize the TiNb₂O₇ powder, TiO₂ (Sigma Aldrich, 99%) and Nb₂O₅ (Materion, 99.95%) powders were mixed in stoichiometric ratio. This mixture was ground with a pestle in an agate mortar for 30 min to obtain a homogeneous powder. Then, 300 mg of this powder was pressed into a pellet. The latter was placed on a bed of sacrificial powder of the same material in an alumina crucible, which was nestled into a larger alumina crucible filled with 7 g of activated charcoal. This stack was heated in a microwave oven at 1125 W for 8 to 9 min. Finally, the insulation was removed and the TiNb₂O₇ pellet was left to cool to room temperature.

4.3. Electrode fabrication

To fabricate the PnBnO₂₅ or TiNb₂O₇ electrodes, the previously synthesized PnBnO₂₅ powder or TiNb₂O₇ pellet was mixed with SuperP (TIMCAL) and ground with a pestle in an agate mortar for 10 min. To prepare the PnBnO₂₅ or TiNb₂O₇ slurry, polyvinylidene fluoride (PVDF) was first dissolved in N-Methyl-2-pyrrolidone (NMP). The PnBnO₂₅/SuperP or TiNb₂O₇/SuperP mixture was then added to the PVDF/NMP solution. The resulting slurry had a PnBnO₂₅ or TiNb₂O₇:SuperP:PVDF mass ratio of 7.5:1:5.1. Finally, the slurry was cast on a large copper foil using a doctor blade adjusted to the desired gap. The electrodes were first dried on a 40 °C hot plate overnight and then dried in a 110 °C vacuum oven for 6 h. The thickness of the PnBnO₂₅ electrodes was around 40 μm and their PnBnO₂₅ mass loading was around 2 mg/cm². For the TiNb₂O₇ electrodes, the thickness was around 20 μm and the TiNb₂O₇ mass loading was around 1 mg/cm². Note that X-ray diffraction spectra, cyclic voltammetry, and galvanostatic cycling measurements of similar cells with PnBnO₂₅ or TiNb₂O₇ electrodes made using the same material synthesis and electrode fabrication methods can be found in our previous studies [27, 28].

4.4. Operando isothermal calorimeter

Microcalorimetry ETIS measurements were performed in an operando isothermal calorimeter described in Ref. [36]. Here, the two-electrode calorimetric battery cells consisted of (i) a PnBnO₂₅ or TiNb₂O₇ working electrode previously fabricated and cut into 1 cm × 1 cm square shape, (ii) a polished metallic lithium (Sigma Aldrich, 99.9%) counter electrode also cut into 1 cm × 1 cm square shape, (iii) two 260 μm thick glass microfiber filters (Whatman, Grade GF/C) acting as both separators and thermal insulators, impregnated with (iv) 1 M LiPF₆ in EC:DMC 1:1 v/v (Sigma Aldrich, battery grade) electrolyte. Note that the two-electrode calorimetric battery cells were assembled in a glove box containing Ar gas with less than 0.1 ppm of O₂ and H₂O. During microcalorimetry ETIS measurements, the current was imposed and the potential was measured using a high accuracy potentiostat (BioLogic, SP-150). Simultaneously, the instantaneous heat generation rates ̇Qᵢ(t) (in mW) at the PnBnO₂₅ or TiNb₂O₇ working electrode and at the metallic lithium counter electrode were calculated from the instantaneous heat fluxes qᵢ'(t) (in mW/cm²) measured by a 1 cm × 1 cm thermoelectric heat flux sensor (greenTEG, eSKIN-XP) in thermal contact with the back of each electrode "i" according to [36],

$$\dot{Q}_i(t) = q'_i(t)A_i = \frac{AV(t)}{S_i} A_i \quad \text{with } i = MA \text{ or } Li.$$  

Here, Aᵢ (in cm²) is the footprint area of the electrode and ΔV(t) (in μV) is the instantaneous voltage difference measured by the heat flux sensor with sensitivity Sᵢ (in μV/W/cm²). Then, the total instantaneous heat generation rate in the battery cell ̇Qₓ(t) can be expressed as the sum of those at each electrode, i.e.,

$$\dot{Q}_x(t) = \dot{Q}_{MA}(t) + \dot{Q}_{Li}(t).$$  

5. Results and discussion

5.1. Numerical simulations of microcalorimetry ETIS

To evaluate the data analysis procedure previously described, numerical simulations of the novel microcalorimetry ETIS method were performed. The open-circuit voltage U_OC(t,x,T) and the entropic potential |dU_OC(t,x,T)/dT| of a PnBnO₂₅ battery cell as functions of lithium composition x previously obtained experimentally from GITT measurements [28] were used as input parameters. In addition, the following parameters were imposed: (i) the ambient temperature was T = 293.15 K, (ii) the electrochemical impedance of the battery cell was defined as |Z(ƒ)| = 100 Ω and \(\phi_Z(ƒ_i) = -\pi/6\), and (iii) the data acquisition period was Δt = 0.1 s. The offset \(I_0 = -0.05, -0.1, -0.2 \text{ mA}\), amplitude \(I_1 = 0.5, 1, 2 \text{ mA}\), and frequency \(f_1 = 25, 50, 100 \text{ mHz}\) of the imposed current I(t) calculated according to Eq. (19) were realistic values typical of experimental measurements. Based on the imposed current I(t), the corresponding lithium composition x at time t was calculated according to Eq. (20). If x fell between any two nearest compositions x₁ and x₂ available from the GITT dataset, then the value of U_OC(x,T) was interpolated linearly between U_OC(x₁,T) and U_OC(x₂,T). Then, the potential response V(t) was calculated according to Eq. (21). Likewise, the value of |dU_OC(t)/dT(x,T)| was also interpolated between |dU_OC(t)/dT(x₁,T)| and |dU_OC(t)/dT(x₂,T)| given by GITT. Then, the irreversible Qᵢ(t) and reversible Qᵦᵢ(t) heat generation rates were calculated according to Eqs. (25) and (27), respectively. The sum gave the total instantaneous heat generation rate \(\dot{Q}_x(t)\) such that \(\dot{Q}_x(t) = \dot{Q}_r(t) + \dot{Q}_w(t).

Note that, in the present microcalorimetry ETIS method, the battery cell is assumed to be operating at low C-rates, such that the heat generation rates Qᵦᵢ(t) associated with the enthulphy of mixing and Qᵢ(t) due to side reactions both become negligible. Moreover, to reproduce actual experimental measurements, white noise was added to the calculated \(\dot{Q}_x(t)\) with signal-to-noise ratio equal to 10, 10, or 5. By applying FFT to the calculated heat generation rate \(\dot{Q}_x(t)\) with white noise, |dU_OC(t)/dT(x,T)| was determined according to Eq. (36).

Fig. 3 plots the entropic potential |dU_OC(t)/dT(x,T)| of a PnBnO₂₅ battery cell retrieved from numerical simulations of microcalorimetry ETIS after applying FFT to the calculated \(\dot{Q}_x(t)\) with white noise for different values of (a) current offset I₀, (b) current amplitude I₁, (c) current frequency f₁, and (d) signal-to-noise ratio SRn. The baseline case corresponds to T = 293.15 K, I₀ = -0.1 mA, I₁ = 1 mA, f₁ = 50 mHz, and SRn = ∞. Fig. 5 also compares the retrieved entropic potential |dU_OC(t)/dT(x,T)| with the input parameters previously obtained experimentally with GITT at 20 °C [28]. Here, it is interesting to note that the choice of I₀ had a strong impact on the retrieved |dU_OC(t)/dT(x,T)| while the influence of I₁ and f₁ was less visible. In fact, the deviation of the retrieved |dU_OC(t)/dT(x,T)| relative to that obtained from GITT was reduced by minimizing I₀. Nevertheless, in every case the |dU_OC(t)/dT(x,T)| retrieved from simulations accurately reflected the evolution of |dU_OC(t)/dT(x,T)| imposed and obtained experimentally from GITT. Finally, Fig. 3(d) illustrates that even with a signal-to-noise ratio of 10 the evolution of |dU_OC(t)/dT(x,T)| can be successfully retrieved.

Furthermore, the profile of |dU_OC(t)/dT(x,T)| with respect to x is generally more informative than its magnitude. In fact, the former was sufficient in creating the interpretation guide of different charging mechanisms from our previous study [7]. Therefore, the retrieved
The entropic potential \( \frac{\partial U_{OCV}}{\partial T} (x, T) \) of a PNb\(_9\)O\(_{25}\) battery cell retrieved from numerical simulations of microcalorimetry ETIS for different values of (a) current offset \( I_0 \), (b) current amplitude \( I_1 \), (c) current frequency \( f_1 \), and (d) signal-to-noise ratio (SNR), with comparison to the \( \frac{\partial U_{OCV}}{\partial T} (x, T) \) obtained experimentally from GITT [28] and used as input. Unless otherwise noted, \( T = 293.15 \) K, \( I_0 = -0.1 \) mA, \( I_1 = 1 \) mA, \( f_1 = 50 \) mHz, and SNR = \( \infty \).

The entropic potential \( \frac{\partial U_{OCV}}{\partial T} (x, T) \) can be normalized according to,

\[
\frac{\partial U_{OCV}}{\partial T}^* (x, T) = \frac{\partial U_{OCV} (x, T) - \partial U_{OCV}^\text{max} (x, T)}{\partial U_{OCV}^\text{max} (x, T) - \partial U_{OCV}^\text{min} (x, T)}
\]

where \( \partial U_{OCV} / \partial T \)\text{max}(x, T) and \( \partial U_{OCV} / \partial T \)\text{min}(x, T) are respectively the maximum and minimum values of the entropic potential over the entire window of lithium composition. Fig. 4 plots the normalized entropic potential \( \partial U_{OCV} / \partial T^* (x, T) \) for the same cases as those presented in Fig. 3. First, in every case the relative difference between the normalized entropic potential \( \partial U_{OCV} / \partial T^* (x, T) \) retrieved from simulations and that obtained experimentally from GITT (Fig. 4) was smaller than the difference between their original values (Fig. 3). This illustrates the fact that normalization can alleviate the impact of the arbitrary choice of \( I_0 \) while accurately retrieving the features of \( \partial U_{OCV} / \partial T (x, T) \) necessary for its interpretation. In addition, the results can be further improved by minimizing \( I_1 \) and maximizing \( f_1 \).

These observations can inform the experimental implementation of the present microcalorimetry ETIS method.

5.2. Microcalorimetry ETIS measurements on a battery cell

5.2.1. Imposed current and potential response

To validate experimentally the novel microcalorimetry ETIS method, measurements using operando isothermal calorimetry were performed on battery cells at temperature \( T = 293.15 \) K. Here, the full cell was assembled in the operando isothermal calorimeter previously described with a PNb\(_9\)O\(_{25}\) or TiNb\(_2\)O\(_7\) working electrode and a metallic lithium counter electrode immersed in 1 M LiPF\(_6\) in EC:DMC 1:1 v/v electrolyte. The experimentally imposed current \( I(t) \) during discharging (lithiation) featured offset \( I_0 = -0.1 \) mA, amplitude \( I_1 = 1 \) mA, frequency \( f_1 = 50 \) mHz, and period \( t_1 = 20 \) s. Note that these settings were chosen as a compromise between (i) superior accuracy of results calling for small \( I_0 \), small \( I_1 \), and large \( f_1 \), and (ii) the constraints of actual experimental conditions favoring large \( I_0 \) for shorter measurement duration, large \( I_1 \) for adequate heat generation rate signal, and small \( f_1 \) to give redox reactions sufficient time to proceed.

Fig. 5 plots the measured potential \( V(t) \) and the retrieved opencircuit voltage \( U_{OCV}(x, T) \) determined using Eq. (22) as the average of \( V(t) \) over every period. As predicted by Eq. (21), the sinusoidal
o.) for positive \( I \) was endothermic (patterns and period \( t \) frequency \( f \)) over four consecutive periods. Interestingly, \( \dot{Q} \) was measured at the TiNb \(_9\) corresponding metallic lithium counter electrode, and (c) \( \dot{Q} \) measured at the TiNb \(_{25}\) working electrode or (b) \( \dot{Q} \) measured at the TiNb \(_9\) battery cell, compared to 150 h and 70 h, respectively, for potentiometric entropy measurements based on GITT [28].

### 5.2.2. Heat generation rates

Fig. 6 plots the instantaneous heat generation rates (a) \( Q_{PN_0(t)} \) measured at the Pnb\(_{25}\) working electrode or (b) \( Q_{TN_0(t)} \) measured at the TiNb\(_9\) working electrode, as well as \( Q_L(t) \) measured at the corresponding metallic lithium counter electrode, and (c) \( Q_T(t) = Q_{PN_0(t)} + Q_L(t) \) or (d) \( Q_T(t) = Q_{TN_0(t)} + Q_L(t) \) measured in the entire battery cell over four consecutive periods. Interestingly, \( Q_{PN_0(t)} \), \( Q_{TN_0(t)} \), and \( Q_L(t) \) were all sinusoidal functions with the same frequency \( f_L \) as \( I(t) \) and \( V(t) \). As a result, \( Q_T(t) \) was periodic with complex patterns and period \( t_1 = 1/f_L = 20 \) s. Moreover, \( Q_{PN_0(t)} \) or \( Q_{TN_0(t)} \) was endothermic (< 0) for negative current \( I(t) \) and exothermic (> 0) for positive \( I(t) \), whereas \( Q_L(t) \) was exothermic for negative \( I(t) \) and endothermic for positive \( I(t) \). In fact, according to Eqs. (29) and (30), such behavior indicates that the partial entropy changes were positive at the Pnb\(_{25}\) or TiNb\(_9\) working electrodes and negative at the corresponding metallic lithium counter electrodes. These results were consistent with the observations made in our previous study [28]. Finally, even though state-of-the-art potentiostat and heat flux sensors were used, Fig. 6 illustrates that with \( i_1 = 1 \) mA and \( f_L = 50 \) mHz, the signal-to-noise ratio in the measured heat generation rates was already around 10. Based on the numerical simulation results shown in Fig. 3(d), a signal-to-noise ratio of at least 10 was necessary to successfully retrieve the evolution of \( \partial U_{OCV}/\partial T(x,T) \). Further decreasing \( i_1 \) and/or increasing \( f_L \) would decrease the magnitude of the heat generation rates and, consequently, the signal-to-noise ratio would fall below 10 which would compromise the precision of the retrieved \( \partial U_{OCV}/\partial T(x,T) \).

### 5.2.3. Open-circuit voltage and entropic potential

After applying FFT to the total heat generation rate \( Q_T(t) \) in each battery cell, the entropic potential \( \partial U_{OCV}/\partial T(x,T) \) was determined according to Eq. (36). The entropic potential was then normalized to compute \( \partial U_{OCV}/\partial T(x,T) \) according to Eq. (45). Fig. 7 compares the open-circuit voltage \( U_{OCV}(x,T) \) and the normalized entropic potential \( \partial U_{OCV}/\partial T(x,T) \) of the investigated (a, b) Pnb\(_{25}\) or (c, d) TiNb\(_9\) battery cell determined by GITT [28] and by microcalorimetry ETIS.
measurements. Here, \( U_{\text{OCV}}(x, T) \) and \( \partial U_{\text{OCV}} / \partial T \) determined by both methods were in very good agreement for both battery cells. In fact, while GITT only offered a limited number of data points, hundreds of data points were acquired from microcalorimetry ETIS which created continuous curves for \( U_{\text{OCV}}(x, T) \) and \( \partial U_{\text{OCV}} / \partial T \) (x, T). This is particularly noticeable for the PNNb\(_9\)O\(_{25}\) cell for \( 0 < x < 0.5 \) and for the TiNb\(_2\)O\(_7\) cell for \( 3.2 < x < 4.3 \), when sharp changes in \( \partial U_{\text{OCV}} / \partial T \) (x, T) occurred but were not captured by the GITT method. In addition, combining the profiles of both \( U_{\text{OCV}}(x, T) \) and \( \partial U_{\text{OCV}} / \partial T \) (x, T) enables the identification of different regions with distinctive features [28].

For the PNNb\(_9\)O\(_{25}\) battery cell, seven regions could be identified [7]. (i) Region I for \( 0 < x < 0.5 \): \( U_{\text{OCV}} \) decreased sharply as a result of lithium intercalation in a homogeneous solid solution [28]. By contrast, \( \partial U_{\text{OCV}} / \partial T \) featured a sharp peak and a maximum. This can be attributed to the fact that PNNb\(_9\)O\(_{25}\) is an insulator in pristine phase but quickly becomes a semiconductor upon lithiation [20,55]. As the electrical conductivity increases, so does the electronic entropy, which in turn led to an increase in \( \partial U_{\text{OCV}} / \partial T \) [28]. Note that this was not captured by previous GITT measurements. (ii) Region II for \( 0.5 < x < 2 \): both \( U_{\text{OCV}} \) and \( \partial U_{\text{OCV}} / \partial T \) decreased indicating lithium intercalation in a homogeneous solid solution and the associated configurational entropy change [7]. (iii) Region III for \( 2 < x < 3.5 \): \( U_{\text{OCV}} \) plateaued as a sign of phase transition accompanied by two-phase coexistence [7]. Curiously, \( \partial U_{\text{OCV}} / \partial T \) retrieved from microcalorimetry ETIS increased as opposed to staying relatively constant in GITT measurements. Note that PNNb\(_9\)O\(_{25}\) has also been reported to undergo a semiconductor-to-metal transition around this range of lithium composition [20,55]. It is possible that microcalorimetry ETIS could not capture the plateau in \( \partial U_{\text{OCV}} / \partial T \) associated with two-phase coexistence as effectively as GITT. In fact, phase transition is a kinetically slow process, which is captured by the long relaxation periods of GITT but not by microcalorimetry ETIS due to the constant switching between lithiation/delithiation half-periods arising from the sinusoidal current \( I(t) \). (iv) Region IV for \( 3.5 < x < 5 \): \( U_{\text{OCV}} \) decreased again suggesting lithium intercalation in a homogeneous solid solution [7]. Moreover, \( \partial U_{\text{OCV}} / \partial T \) first increased then decreased resulting in a local maximum, during which the semiconductor-to-metal transition was completed [28]. (v) Region V for \( 5 < x < 8 \): this region also featured lithium intercalation in a homogeneous solid solution as both \( U_{\text{OCV}} \) and \( \partial U_{\text{OCV}} / \partial T \) decreased monotonously [7]. (vi) Region VI for \( 8 < x < 11 \): the decrease in \( U_{\text{OCV}} \) was accompanied by a tilde-shaped fluctuation in \( \partial U_{\text{OCV}} / \partial T \), which can be attributed to intralayer ion ordering [7]. It is interesting to note that the intralayer ion ordering spanned a wider range of lithium composition when

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**Fig. 5.** Measured potential \( V(t) \) during discharging and retrieved open-circuit voltage \( U_{\text{OCV}}(x, T) \) determined using Eq. (22) as the average of \( V(t) \) over every period during microcalorimetry ETIS measurements on (a, b) PNNb\(_9\)O\(_{25}\) or (c, d) TiNb\(_2\)O\(_7\) battery cell. The imposed current \( I(t) \) was given by Eq. (19) with \( I_h = -0.1 \) mA, \( I_i = 1 \) mA, and \( f = 50 \) mHz. Note that Figs. 5(b) and 5(d) are enlargements of arbitrary time windows shown in green in Figs. 5(a) and 5(c), respectively.
measured by microcalorimetry ETIS than by GITT. Likewise, this difference possibly emerged as a result of the constant switching between lithiation/delithiation half-periods during microcalorimetry ETIS measurements, which might have prolonged the ion ordering process. (vii) Region VII for $11 < x < 11.5$: both $U_{OCV}$ and $[\partial U_{OCV}/\partial T]^{*}$ featured a plateau indicative of phase transition accompanied by two-phase coexistence.

In the case of the TiNb$_2$O$_7$ battery cell, five regions could be identified [27]. (i) Region I for $0 < x < 0.2$: $U_{OCV}$ featured a sharp drop indicating lithium intercalation in a homogeneous solid solution [7]. By contrast, $[\partial U_{OCV}/\partial T]^{*}$ rose to reach a maximum. This can also be attributed to the rapid electrical conductivity increase of TiNb$_2$O$_7$ upon lithiation [27,56]. (ii) Region II for $0.2 < x < 0.6$: both $U_{OCV}$ and $[\partial U_{OCV}/\partial T]^{*}$ decreased due to lithium intercalation in a homogeneous solid solution [7]. The configurational entropy change contributed to the sharp decrease in $[\partial U_{OCV}/\partial T]^{*}$ [7]. (iii) Region III for $0.6 < x < 1.7$: $U_{OCV}$ decreased slowly while $[\partial U_{OCV}/\partial T]^{*}$ featured a tile-shaped fluctuation characteristic of intralayer ion ordering [7]. (iv) Region IV for $1.7 < x < 3.2$: $U_{OCV}$ continued decreasing while $[\partial U_{OCV}/\partial T]^{*}$ first increased then decreased resulting in a local maximum. This behavior can be attributed to the continuous electrical conductivity increase of TiNb$_2$O$_7$ during lithiation [27,56]. Here also, the electronic entropy increased like the semiconductor-to-metal transition observed within region IV of the PNb$_9$O$_{25}$ cell, thus leading to an analogous shape of the entropic potential. (v) Region V for $3.2 < x < 4.3$: both $U_{OCV}$ and $[\partial U_{OCV}/\partial T]^{*}$ decreased monotonously corresponding to lithium intercalation in a homogeneous solid solution [7]. Note that this last region was observed only in the microcalorimetry ETIS method. In fact, our previous GITT measurements [27,28] imposed a cell potential cutoff of 1 V to prevent the formation of solid electrolyte interphase (SEI) and dendrites in the battery cell under continuous discharging below 1 V [57,58]. During microcalorimetry ETIS measurements though, the sinusoidal current $I(t)$ meant that whenever the cell potential went below 1 V, it only lasted a few seconds before the direction of current flow and ion diffusion was reversed again. This enabled the cell potential cutoff to be lower than 1 V without significantly damaging the battery cell. In particular, the potential of the TiNb$_2$O$_7$ cell was allowed to reach as low as 0.8 V during microcalorimetry ETIS measurements.

5.2.4. Partial entropy changes

FFT analysis was also applied to the heat generation rates $\dot{Q}_{PN10}(t)$ or $\dot{Q}_{TN10}(t)$ and $\dot{Q}_{Li}(t)$ measured at each electrode to determine the partial entropy changes at the PNb$_9$O$_{25}$ or TiNb$_2$O$_7$ working electrodes and at the corresponding metallic lithium counter electrodes according
Fig. 7. (a, c) Open-circuit voltage $U_{OCV}(x, T)$ and (b, d) normalized entropic potential $[\partial U_{OCV}/\partial T](x, T)$ of a PNb$_9$O$_{25}$ or TiNb$_2$O$_7$ battery cell determined by GITT [28] or microcalorimetry ETIS measurements. The different colored regions correspond to specific phenomena occurring in the battery cell.

6. Conclusion

This paper presented a novel and fast microcalorimetry ETIS measurement method using an operando isothermal calorimeter to determine the open-circuit voltage $U_{OCV}$, the entropic potential $\partial U_{OCV}/\partial T$, and the partial entropy changes at each electrode as functions of the state of charge of a battery cell, all within only a few hours. The apparatus was designed for bare electrodes (i.e., without casing) with material mass loadings on the order of milligrams and measured heat generation rates on the order of microwatts. The method consists of imposing a sinusoidal current and measuring the potential response as well as the heat generation rates at each electrode separately. The open-circuit voltage $U_{OCV}$ of the cell was acquired by time-averaging the measured potential response. Furthermore, FFT analysis of the measured total heat generation rate was used to retrieve the entropic potential $\partial U_{OCV}/\partial T$ of the entire cell without having to measure the cell potential at several different temperatures. The procedure was the dominant processes occurring at the counter electrodes. Overall, these results demonstrate the capability of the novel microcalorimetry ETIS method to extract the partial entropy changes at each electrode, which has not been achieved by any other existing method.
first validated numerically and then demonstrated experimentally with battery cells consisting of P_nb_{9}O_{25} or TiNb_{2}O_{7} working electrodes and metallic lithium counter electrodes. The open-circuit voltage and the normalized entropic potential retrieved from the novel microcalorimetry ETIS measurements agreed well with those previously determined by potentiometric entropy measurements based on GITT at three different temperatures [27,28]. Finally, the partial entropy changes at each electrode were calculated from the individually measured heat generation rates. Compared to other state-of-the-art methods, this is the first method capable of retrieving the entropy evolution of LIB materials at each electrode.

CRediT authorship contribution statement

Yucheng Zhou: Conceptualization, Data curation, Formal analysis, Investigation, Visualization, Writing – original draft, Writing – review & editing. Yunkai Luo: Investigation, Writing – review & editing. Ashlea Patterson: Investigation, Writing – review & editing. Sun Woong Baek: Conceptualization, Writing – review & editing. Matevž Frajnkovič: Conceptualization, Writing – review & editing. Ram Se-shadri: Conceptualization, Supervision, Writing – review & editing. Bruce S. Dunn: Conceptualization, Supervision, Writing – review & editing. Laurent Pilon: Conceptualization, Funding acquisition, Project administration, Supervision, Writing – review & editing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request

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